#### Lecture 15

**Chemical Reaction Engineering** (CRE) is the field that studies the rates and mechanisms of chemical reactions and the design of the reactors in which they take place.

## Lecture 15 - Tuesday 3/12/2013

**Enzymatic Reactions** 

- Michealis-Menten Kinetics
- Lineweaver-Burk Plot
- Enzyme Inhibition
  - Competitive
  - Uncompetitive
  - Non-Competitive

# **Review Last Lecture** Active Intermediates and PSSH Energy Energy **Reaction Coordinate Reaction Coordinate** (a) (b)

Reaction coordinate. Courtesy Science News, 156, 247 (1999).

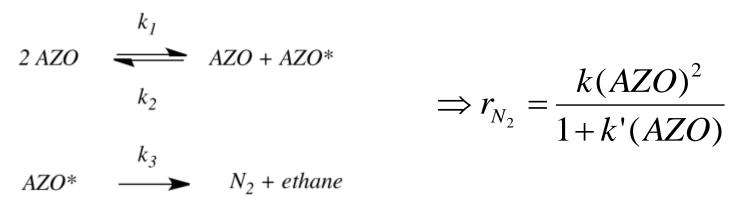
#### **Review Last Lecture**

## Active Intermediates and PSSH

1.In the PSSH, we set the rate of formation of the active intermediates equal to zero. If the active intermediate A\* is involved in m different reactions, we set it to:

$$r_{A^*.net} = \sum_{i=1}^m r_{A^*i} = 0$$

2. The azomethane (AZO) decomposition mechanism is



By applying the PSSH to AZO\*, we show the rate law, which exhibits first-order dependence with respect to AZO at high AZO concentrations and second-order dependence with respect to AZO at low AZO concentrations.

Enzymes are protein-like substances with catalytic properties.

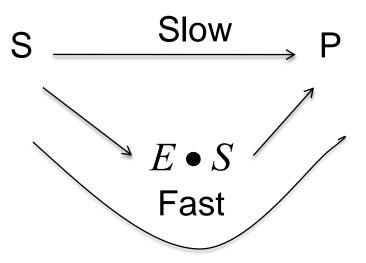


#### **Enzyme Unease**

[From Biochemistry, 3/E by Stryer, copywrited 1988 by Lubert Stryer. Used with permission of W.H. Freeman and Company.]

## Enzymes

Enzymes provide a pathway for the substrate to proceed at a faster rate. The substrate, S, reacts to form a product P.



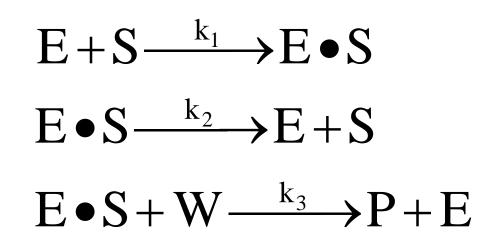
A given enzyme can only catalyze only one reaction. Example, Urea is decomposed by the enzyme urease.

## **Enzymes - Urease**

A given enzyme can only catalyze only one reaction. Urea is decomposed by the enzyme urease, as shown below.

 $NH_{2}CONH_{2} + UREASE \xrightarrow{H_{2}O} 2NH_{3} + CO_{2} + UREASE$  $S + E \xrightarrow{H_{2}O} P + E$ 

The corresponding mechanism is:



Enzymes - Michaelis-Menten Kinetics  

$$r_{p} = k_{3}(E \bullet S)(W)$$

$$r_{E \bullet S} = 0 = k_{1}(E)(S) - k_{2}(E \bullet S) - k_{3}W(E \bullet S)$$

$$(E \bullet S) = \frac{k_{1}(E)(S)}{k_{2} + k_{3}W}$$

$$E_{t} = (E) + (E \bullet S)$$

$$(E) = \frac{E_{t}}{1 + \left(\frac{k_{1}S}{k_{2} + k_{3}W}\right)}$$

$$r_{P} = k_{3} (E \bullet S)(W) = \frac{\overbrace{k_{3}WE_{t}S}^{k_{cat}}}{\underbrace{k_{2} + k_{3}W}_{K_{M}} + S} = \frac{\overbrace{k_{cat}E_{t}S}^{V_{max}}}{K_{M} + S}$$

$$r_P = k_3 (E \bullet S)(W) = \frac{V_{\max}S}{K_m + S}$$

$$V_{max} = k_{cat} E_t$$

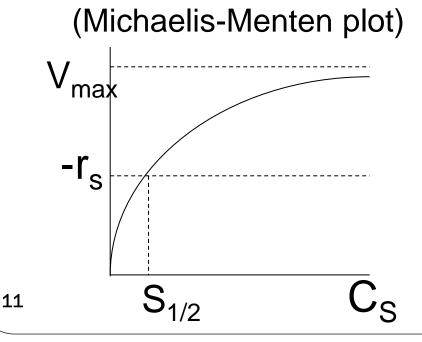
Turnover Number:  $k_{cat}$ Number of substrate molecules (moles) converted to product in a given time (s) on a single enzyme molecule (molecules/molecule/time)

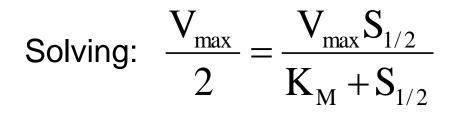
For the reaction: 
$$H_2O_2 + E \xrightarrow{k_{cat}} H_2O + O + E$$

40,000,000 molecules of  $H_2O_2$  converted to product per second on a single enzyme molecule.

**Michaelis-Menten Equation** 

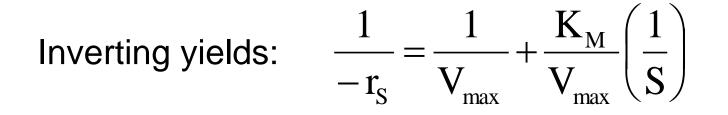
$$r_{\rm P} = -r_{\rm S} = \frac{V_{\rm max}S}{K_{\rm M} + S}$$



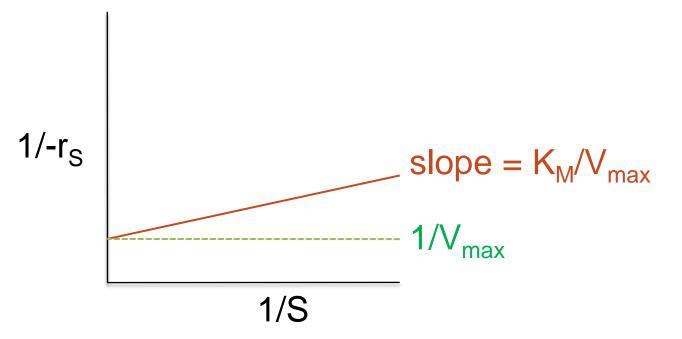


 $K_{M} = S_{1/2}$ 

therefore  $K_M$  is the concentration at which the rate is half the maximum rate.



Lineweaver-Burk Plot



## Types of Enzyme Inhibition

Competitive

 $E + I \Leftrightarrow I \bullet E$  (inactive)

Uncompetitive  $E \bullet S + I \Leftrightarrow I \bullet E \bullet S$  (inactive)





Non-competitive  $E \bullet S + I \Leftrightarrow I \bullet E \bullet S$  (inactive)  $I \bullet E + S \Leftrightarrow I \bullet E \bullet S$  (inactive)

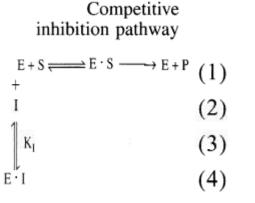


## **Competitive Inhibition**

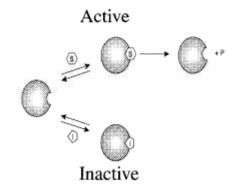
Reaction Steps



Competitive Inhibition Pathway

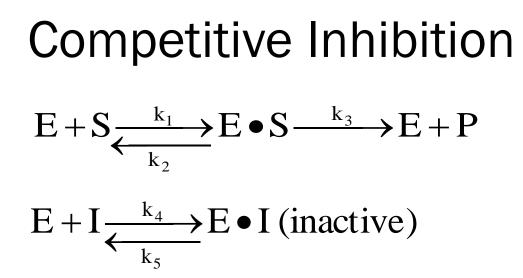


(1)  $E + S \xrightarrow{k_1} E \bullet S$ (2)  $E \bullet S \xrightarrow{k_2} E + S$ (3)  $E \bullet S \xrightarrow{k_3} P + E$ (4)  $I + E \xrightarrow{k_4} E \bullet I$  (inactive) (5)  $E \bullet I \xrightarrow{k_5} E + I$ 



(a) Competitive inhibition. Courtesy of D. L. Nelson and M. M. Cox, *Lehninger Principles of Biochemistry*, 3rd ed. (New York: Worth Publishers, 2000), p. 266.





#### 1) Mechanisms:

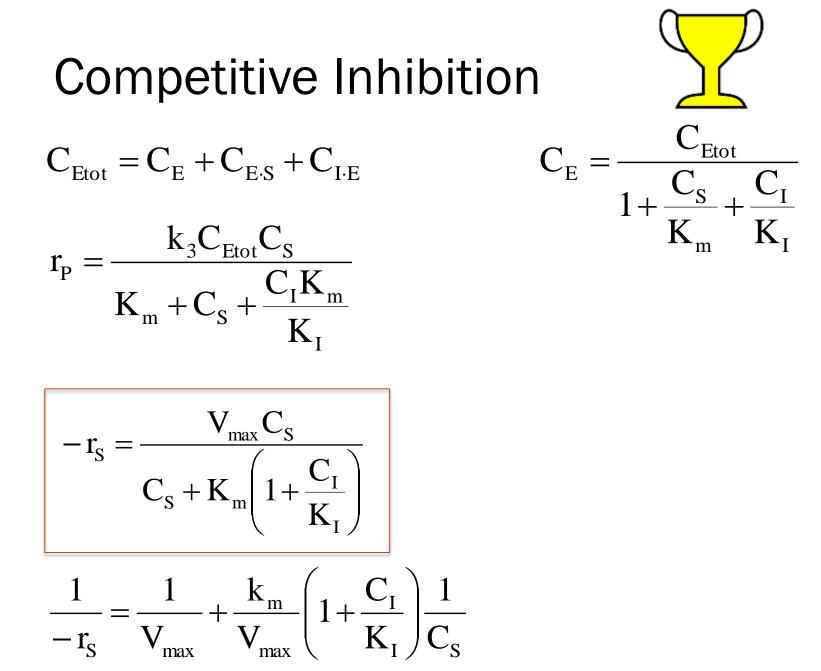
 $E + S \rightarrow E \cdot S \qquad E \cdot S \rightarrow E + S$  $E \cdot S \rightarrow P + E \qquad E + I \rightarrow E \cdot I$  $E \cdot I \rightarrow E + I$ 

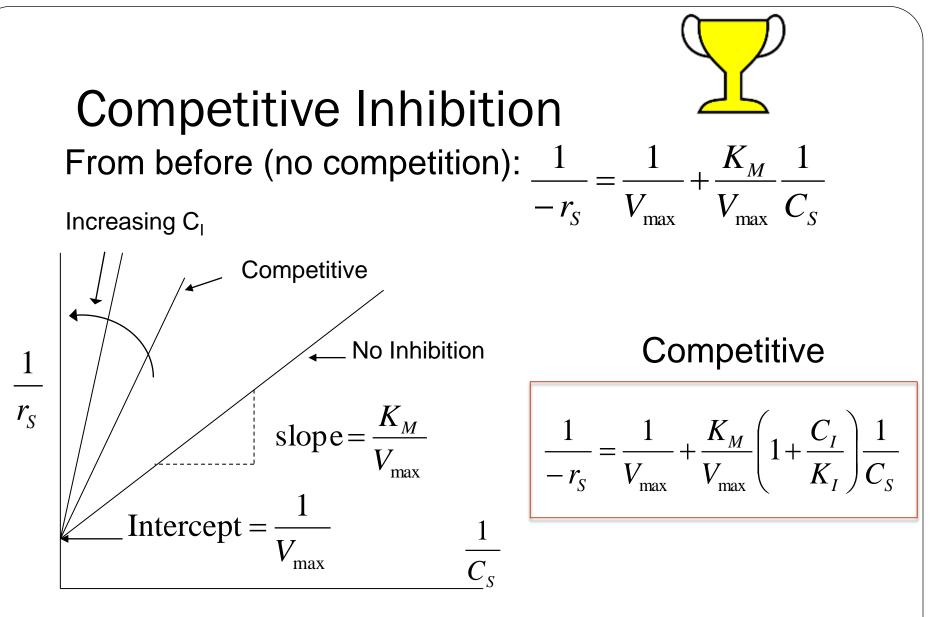
$$\mathbf{r}_{\mathrm{P}} = \mathbf{k}_{3} \mathbf{C}_{\mathrm{E} \cdot \mathrm{S}}$$



## Competitive Inhibition 2) Rate Laws:

$$\begin{aligned} r_{E\cdot S} &= 0 = k_1 C_S C_E - k_2 C_{E\cdot S} - k_3 C_{E\cdot S} \\ C_{E\cdot S} &= \frac{k_1 C_S C_E}{k_2 + k_3} = \frac{C_S C_E}{K_m} \\ r_P &= \frac{k_3 C_S C_E}{K_m} \\ r_{I\cdot E} &= 0 = k_4 C_I C_E - k_5 C_{I\cdot E} \\ C_{I\cdot E} &= \frac{C_I C_E}{K_I} \qquad K_I = \frac{k_5}{k_4} \end{aligned}$$

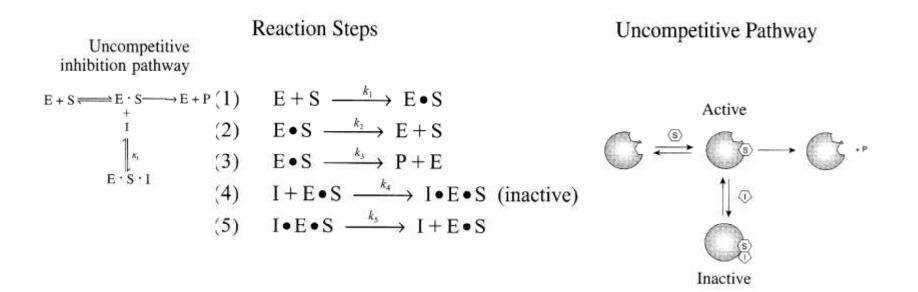




Intercept does not change, slope increases as inhibitor concentration increases

### **Uncompetitive Inhibition**





## **Uncompetitive Inhibition**



Inhibition only has affinity for enzyme-substrate complex

$$E + S \xrightarrow[k_{2}]{k_{2}} E \bullet S \xrightarrow[k_{3}]{k_{3}} P$$

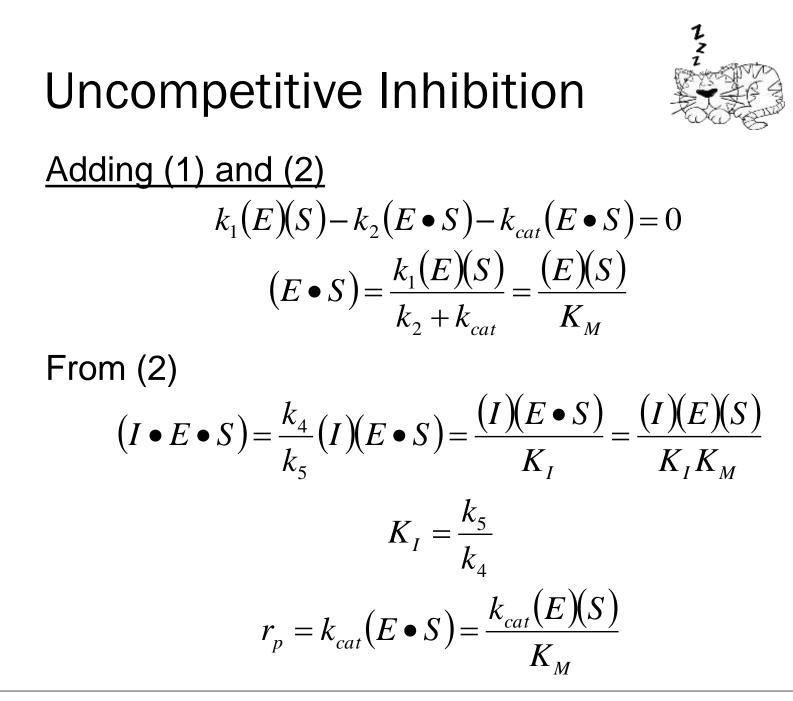
$$I + E \bullet S \xrightarrow[k_{4}]{k_{4}} I \bullet E \bullet S \text{ (inactive)}$$

Developing the rate law:

$$r_P = -r_S = k_{cat} (E \bullet S)$$

 $r_{E \bullet S} = 0 = k_1(E)(S) - k_2(E \bullet S) - k_{cat}(E \bullet S) - k_4(I)(E \bullet S) + k_5(I \bullet E \bullet S)$ (1)

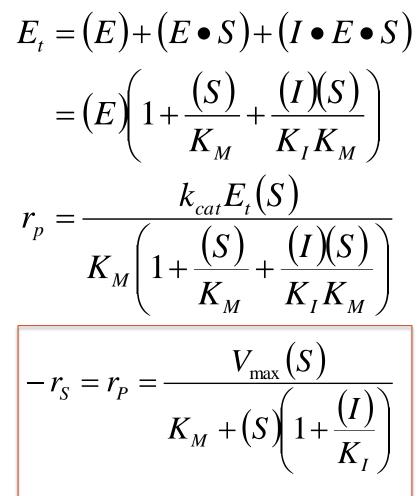
$$r_{I \bullet E \bullet S} = 0 = k_4 (I) (E \bullet S) - k_5 (I \bullet E \bullet S)$$
(2)



# Uncompetitive Inhibition

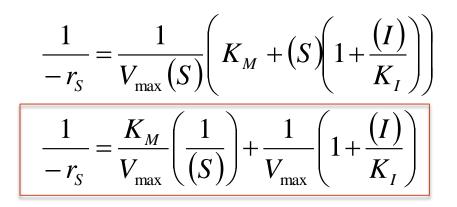


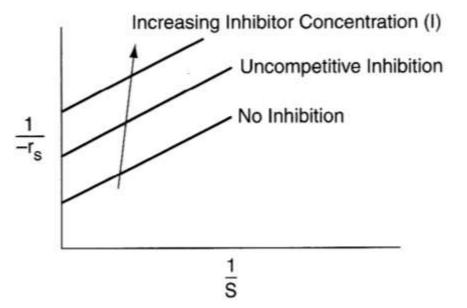
Total enzyme



## **Uncompetitive Inhibition**







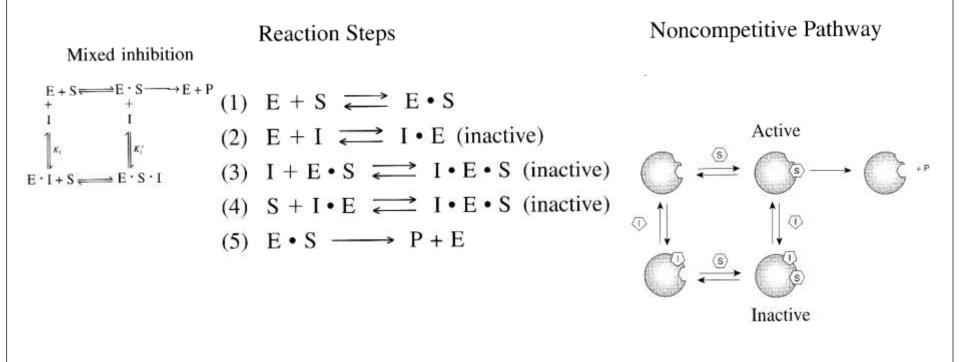
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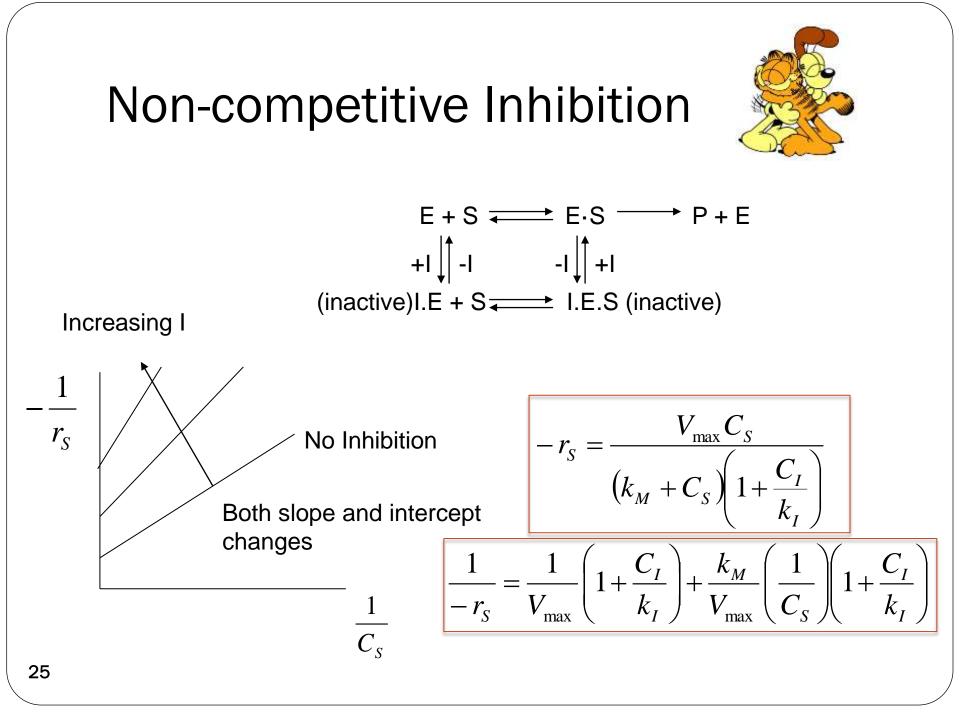
Slope remains the same but intercept changes as inhibitor concentration is increased

Lineweaver-Burk Plot for uncompetitive inhibition

## Non-competitive Inhibition

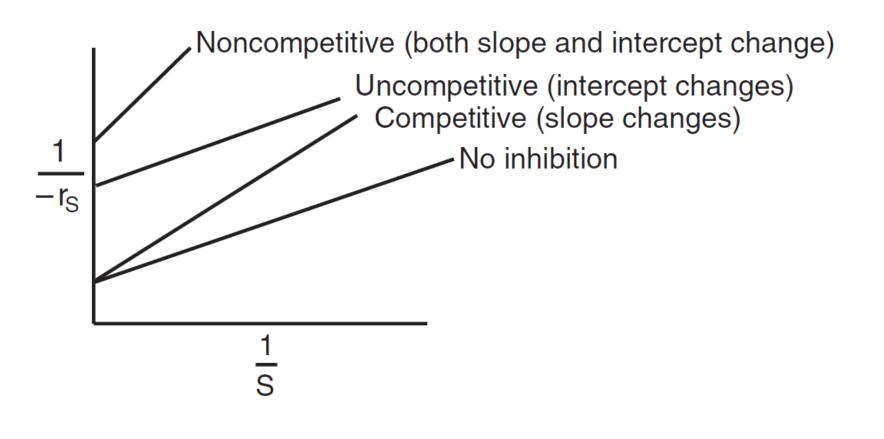






### Summary: Types of Enzyme Inhibition

#### Lineweaver–Burk plots for three types of enzyme inhibition.



## End of Lecture 15