

# **Cold Polar Molecules and their Applications for Quantum Information**

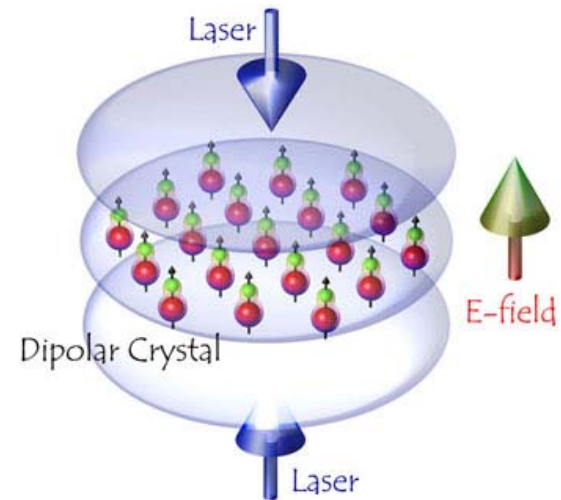
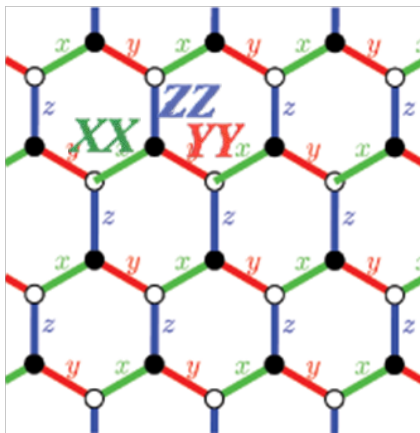
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# Outline

## Introduction to polar molecules

- quantum melting transition between a crystal of and a superfluid

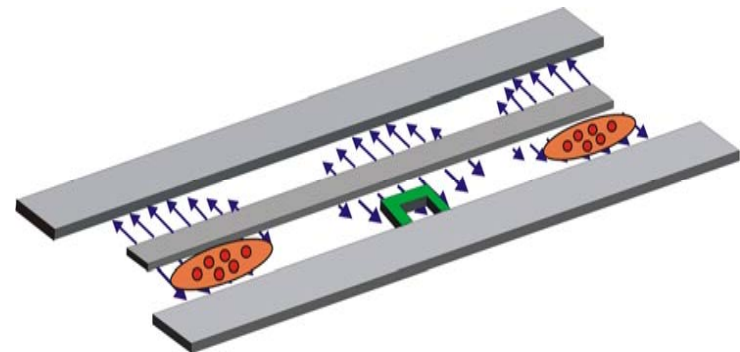


## Spin toolbox

- polar molecules with spin
- realization of Kitaev model
- three-body interactions

## AMO- solid state interface

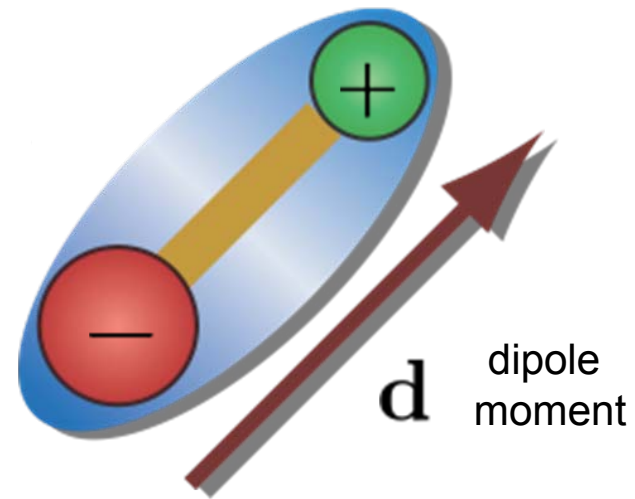
- solid state quantum processor
- molecular quantum memory



# Polar molecules

## Why heteronuclear polar molecules?

- coupling to optical and microwave fields
  - trapping/cooling
  - internal states
- permanent dipole moment
  - strong dipole-dipole interaction
  - long-range interaction



# Polar molecules

## Heteronuclear Molecules

- electronic excitations

$$\sim 10^{10} \text{ Hz}$$

- vibrational excitations

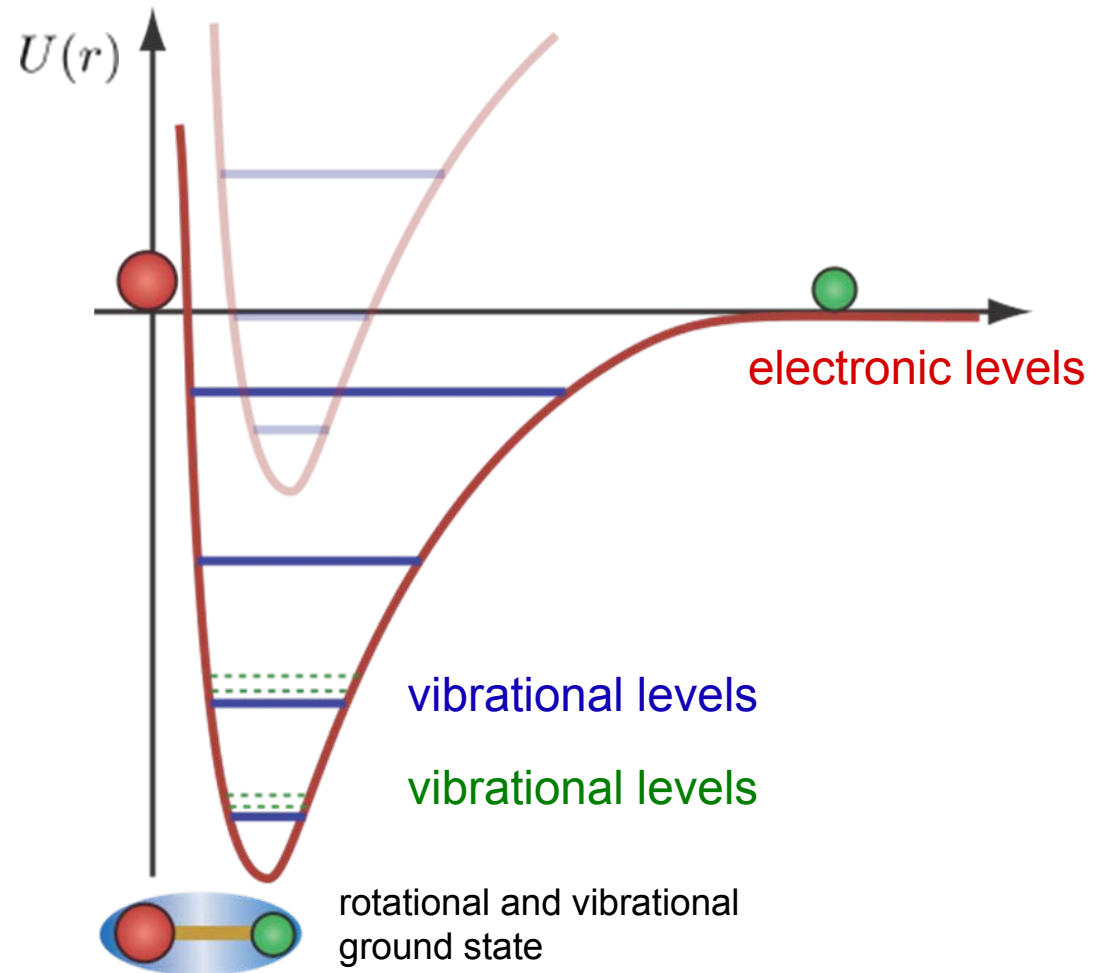
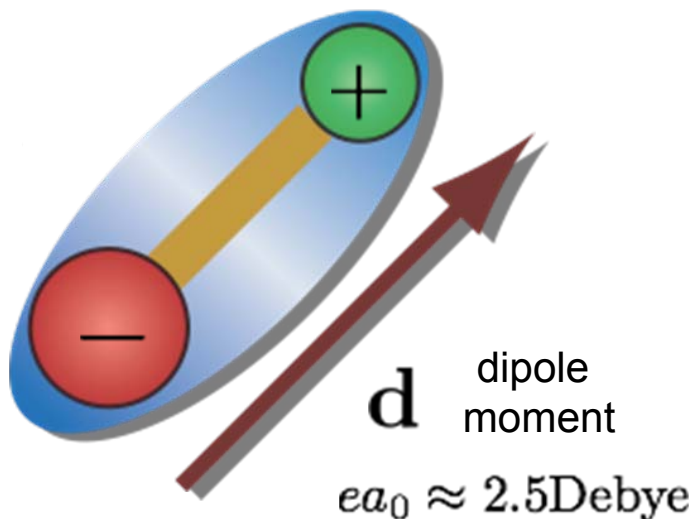
$$\sim 10^{13} \text{ Hz}$$

- rotational excitations  
(microwave fields)

$$\sim 10^{10} \text{ Hz}$$

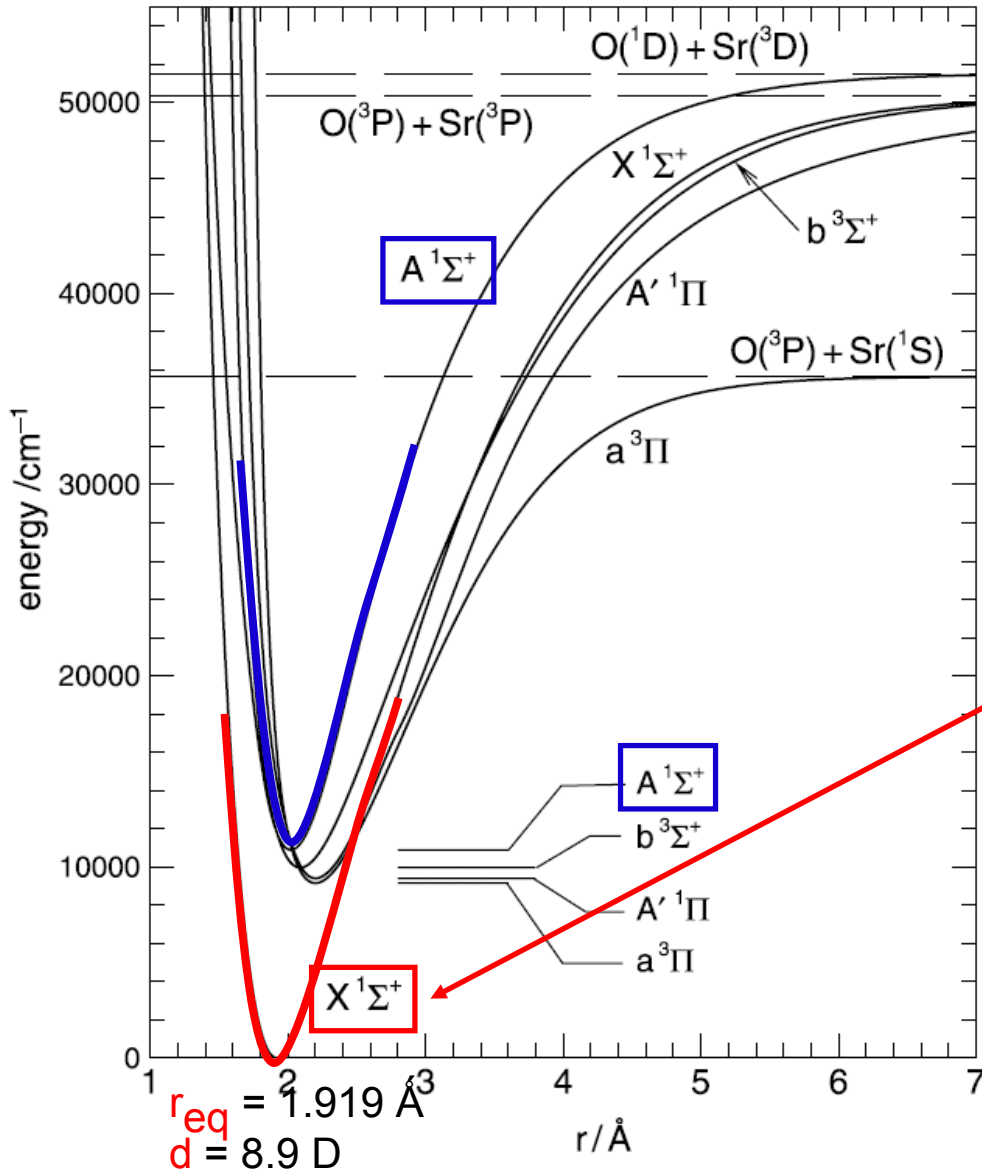
- electron spin

- nuclear spin



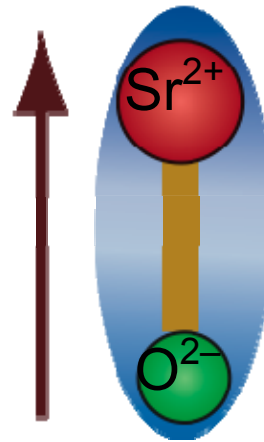
# Polar molecule

Rydberg-Klein-Rees (RKR)-potentials  
(R. Skelton *et al.*, 2003)



heteronuclear molecule with strong persistent dipole moment in electronic groundstate.

Sr<sup>2+</sup>O<sup>2-</sup> ... ionic binding



<sup>38</sup> Sr	[Kr]5s <sup>2</sup>	
<sup>88</sup> Sr	I <sup>p</sup> = 0 <sup>+</sup>	(83%)
<sup>86</sup> Sr	I <sup>p</sup> = 0 <sup>+</sup>	(10%)
<sup>87</sup> Sr	I <sup>p</sup> = 3/2 <sup>+</sup>	(7%)
<sup>8</sup> O	1s2s <sup>2</sup> p <sup>4</sup>	
<sup>16</sup> O	I <sup>p</sup> = 0 <sup>+</sup>	(99.76%)
<sup>18</sup> O	I <sup>p</sup> = 0 <sup>+</sup>	(0.20%)

X¹Σ⁺ ... electronic groundstate:

S=0 ... closed shell (..9σ<sup>2</sup> 10σ<sup>2</sup> 4π<sup>4</sup>)

r<sub>eq</sub> = 1.919 Å ... equilibrium distance

d = 8.900 D ... dipole-moment

ω<sub>eq</sub> = 19.586 THz ... vibrational const.

B<sub>eq</sub> = 10.145 GHz ... rotational

l=0 ... no nuclear momenta for <sup>88</sup>SrO, <sup>86</sup>SrO

# Polar molecules

Polar molecules in the electronic, vibrational, and rotational ground state

- permanent dipole moment:

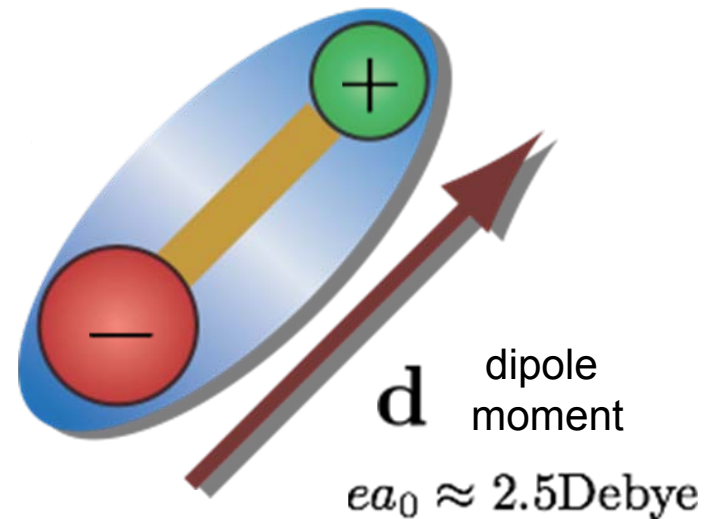
$$d \sim 1 - 9 \text{ Debye}$$

- polarizable with static electric field, and microwave fields

- interactions are increased by

$$1/\alpha^2 \sim 137^2$$

compared to magnetic dipole interactions



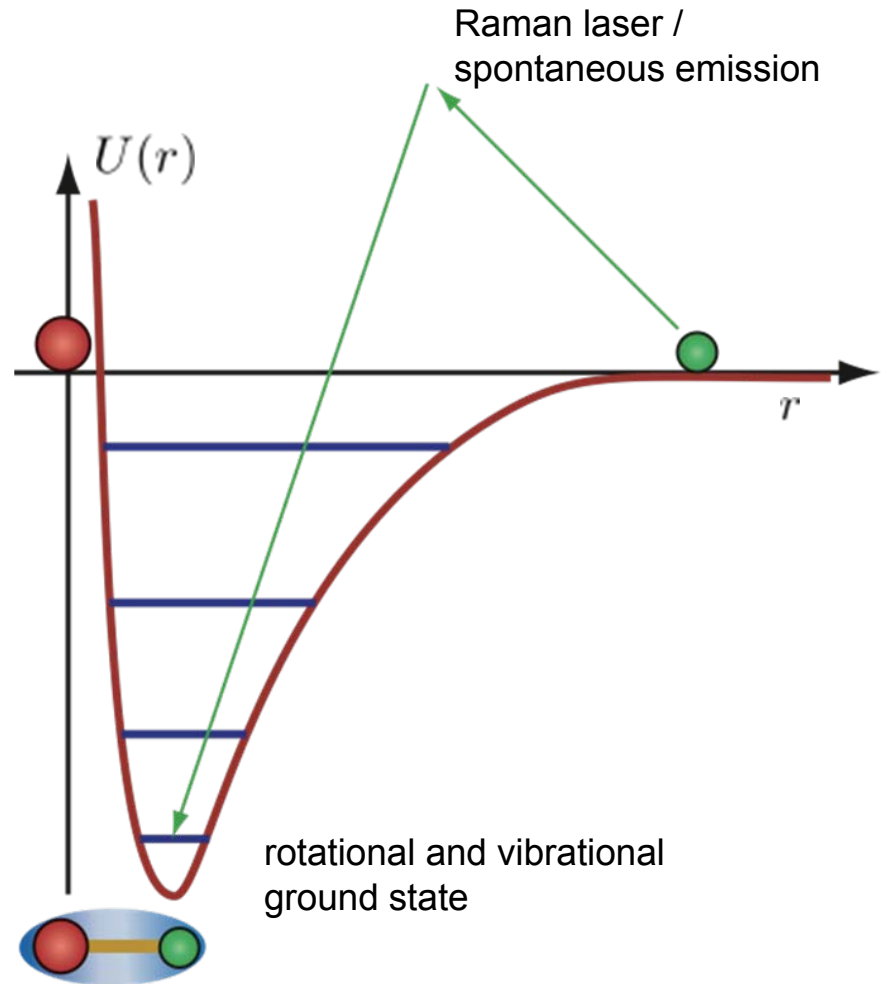
Strong dipole-dipole interactions tunable with external fields

$$V(\mathbf{r}) = \frac{\mathbf{d}_1 \mathbf{d}_2}{r^3} - 3 \frac{(\mathbf{d}_1 \mathbf{r})(\mathbf{d}_2 \mathbf{r})}{r^5}$$

# Polar molecules

## Experimental status

- Polar molecules in the rotational and vibrational ground state
- cooling and trapping techniques beeing developement:
  - cooling of polar molecules:
    - D. De Mille, Yale
    - J. Doyle, Harvard
    - G. Rempe, Munich
    - G. Meijer, Berlin
    - J. Ye, JILA
  - photo association  
(all cold atom labs)
- hetronuclear molecules, e.g.,  
SrO, RbCs, LiCs, Sr F







# Polar molecule

## Dipole matrix elements

- basis states  $|N, m\rangle$

- dipole operator:  $d_0 = d_z$        $d_{\pm 1} = \mp(d_x \pm id_y)/\sqrt{2}$

- matrix elements

$$\langle N + 1, m + q | d_q | N, m \rangle = d(N, m; 1, q | N + 1, m + q) \sqrt{\frac{N + 1}{2N + 3}}$$

Clebsch Gordan coefficient

## Static electric field

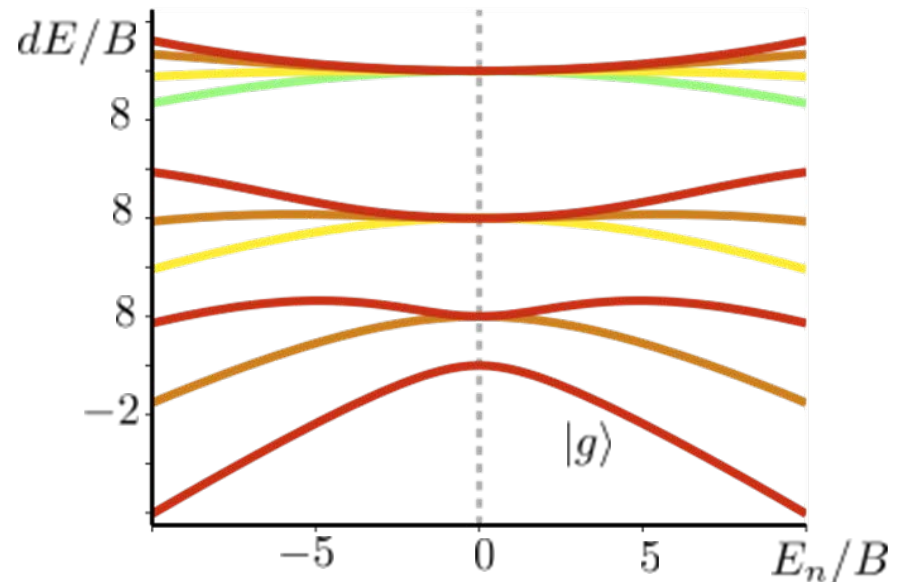
- internal Hamilton

$$H_{\text{rot}}^{(i)} = B\mathbf{N}_i^2 - \mathbf{d}_i \mathbf{E}$$

- finite averaged dipole moment

$$|\langle g | \mathbf{d} | g \rangle| = -\frac{\partial E_g}{\partial E}$$

$$D = |\langle g | \mathbf{d}_i | g \rangle|^2 \leq d^2$$



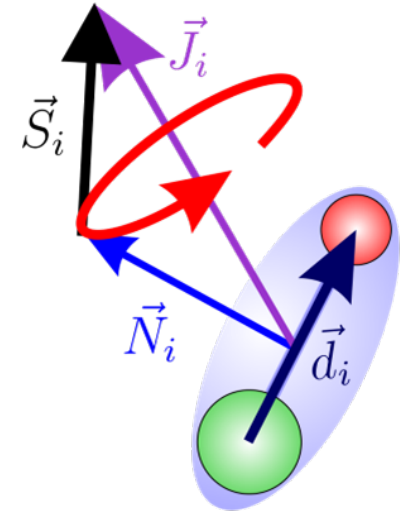
# Polar molecule

Polar molecules with spin CaF

- electronic spin  $S = 1/2$

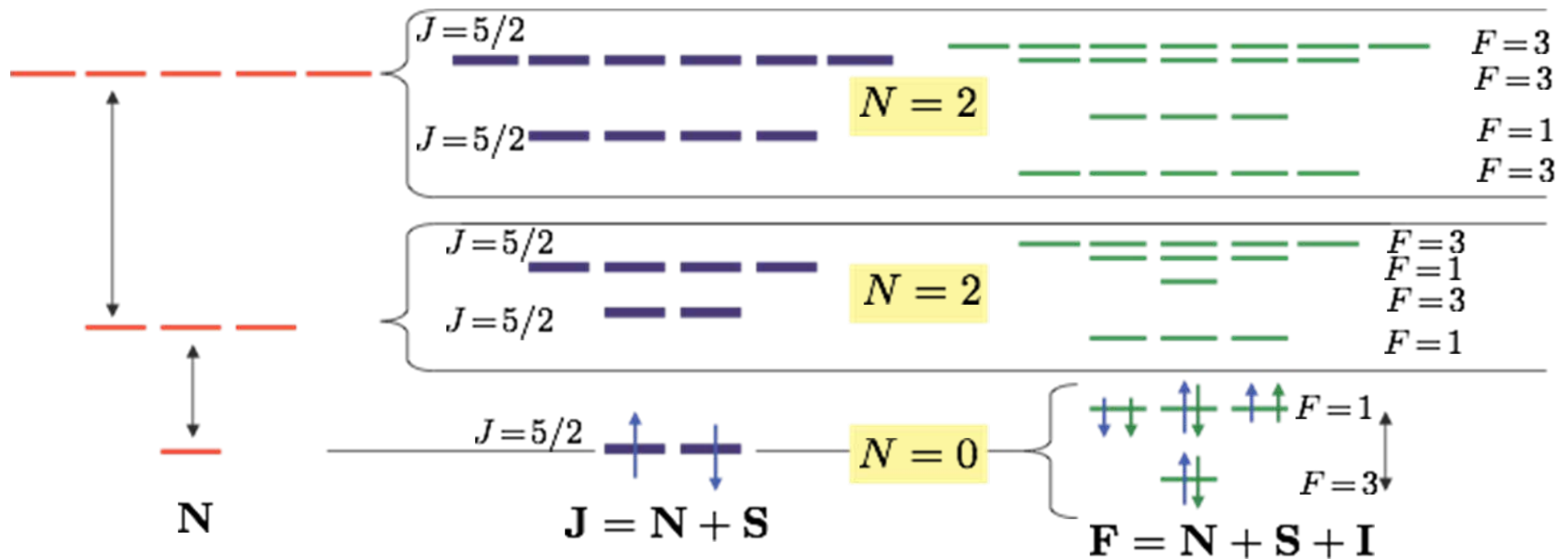
- nuclear spin  $I = 1/2$

spin along  
molecular axes



$$H = BN^2 + \gamma \mathbf{N} \cdot \mathbf{S} + (b\mathbf{S} \cdot \mathbf{I} + cS_\xi I_\xi) + CNI$$

rigid rotor	spin- rotation	hyperfine	$c = 40\text{MHz}$
$B = 10\text{GHz}$	$\gamma = 40\text{MHz}$	$b = 109\text{MHz}$	$C = 30\text{kHz}$



# Interaction between polar molecules

Hamiltonian

$$H^{(1,2)} = \sum_{i=1}^2 \left[ \frac{\mathbf{p}_i^2}{2m} + V_{\text{trap}}(\mathbf{r}_i) + B\mathbf{N}_i^2 - \mathbf{d}_i \mathbf{E} \right] + \frac{\mathbf{d}_1 \mathbf{d}_2 - 3(\mathbf{d}_1 \mathbf{n})(\mathbf{d}_2 \mathbf{n})}{r^3}$$

kinetic energy

trapping potential

rigid rotor

electric field

interaction potential

Without external drive

- van der Waals attraction

$$V_{\text{vdW}}(\mathbf{r}) = -\frac{C_6}{r^6} \quad C_6 \approx d^4/6B$$

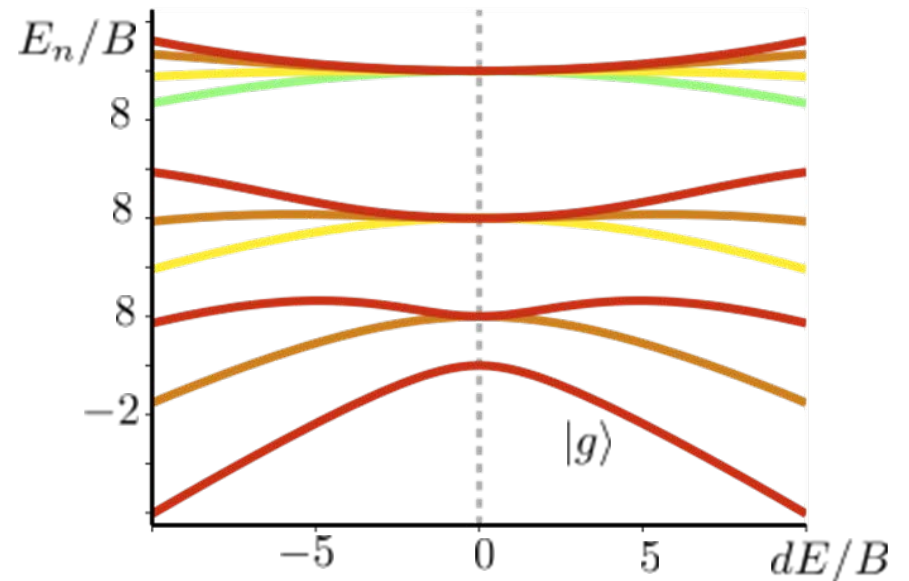
Static electric field

- internal Hamiltonian

$$H_{\text{rot}}^{(i)} = B\mathbf{N}_i^2 - \mathbf{d}_i \mathbf{E}$$

- finite averaged dipole moment

$$D = |\langle g | \mathbf{d}_i | g \rangle|^2 \leq d^2$$

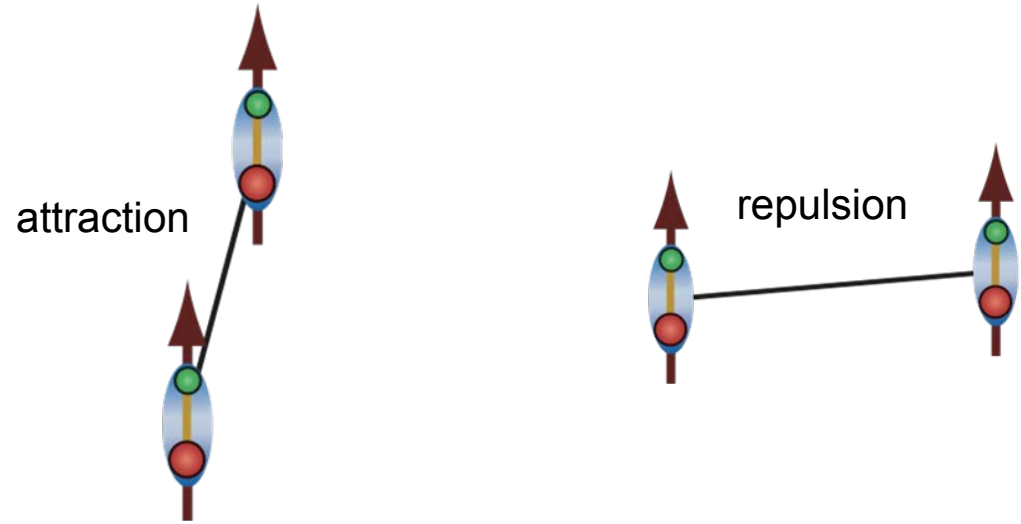


# Dipole-dipole interaction

## Dipole-dipole interaction

- anisotropic interaction
- long-range

$$V_{d-d}(\mathbf{r}) = D \left[ \frac{1}{r^3} - \frac{3z^2}{r^5} \right]$$



## Weak Dipole-dipole interaction

- short-range interaction:
  - pseudo-potential
  - s-wave scattering length
- long range part via dipole-dipole interaction

$$V(\mathbf{r}) = g\delta(\mathbf{r}) + D \left[ \frac{1}{r^3} - \frac{3z^2}{r^5} \right]$$

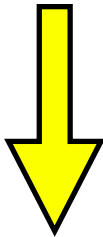
# Dipole-dipole interaction

## Dipole-dipole interaction

- anisotropic interaction
- long-range

$$V(\mathbf{r}) = D \left[ \frac{1}{r^3} - 3 \frac{z^2}{r^5} \right]$$

attraction



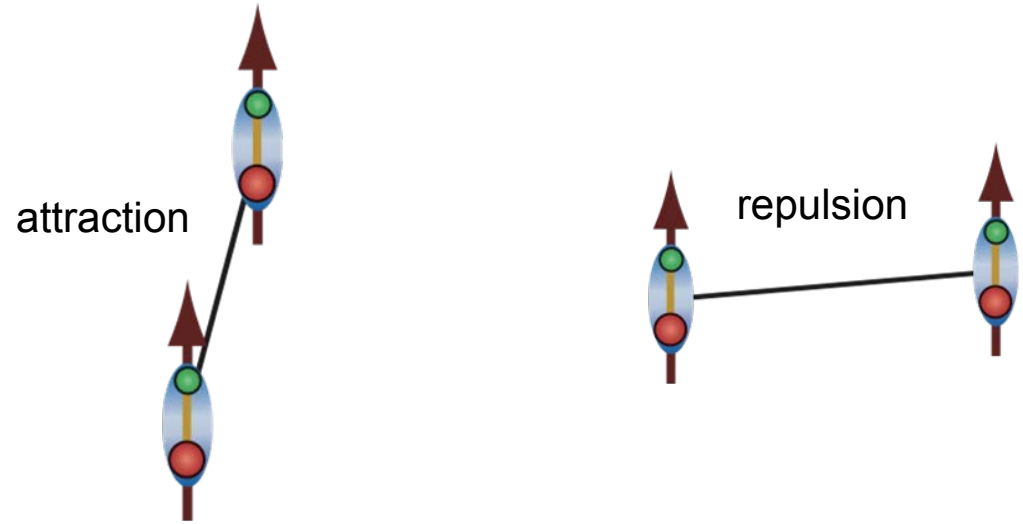
Instability in the many-body system

- collapse of the system for increasing dipole interaction (Pfau '07)

- roton softening
- supersolids?

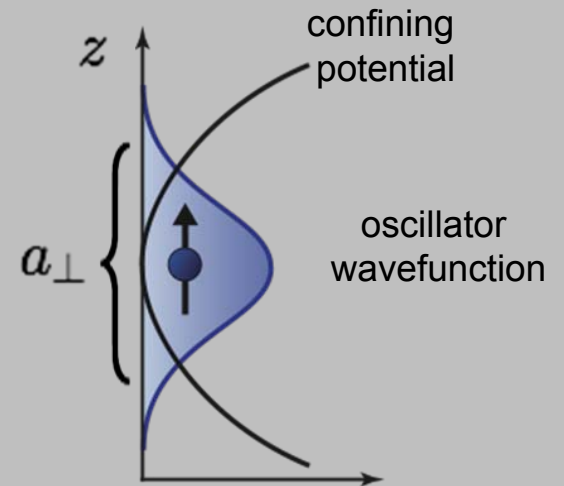
(Goral et. al. '02, L. Santos et al. '03, Shlyapnikov '06)

$$\frac{Dm}{\hbar^2 a_s} \gtrsim 1$$



## Stability:

- strong interactions
- confining into 2D by an optical lattice



# Stability via transverse confining

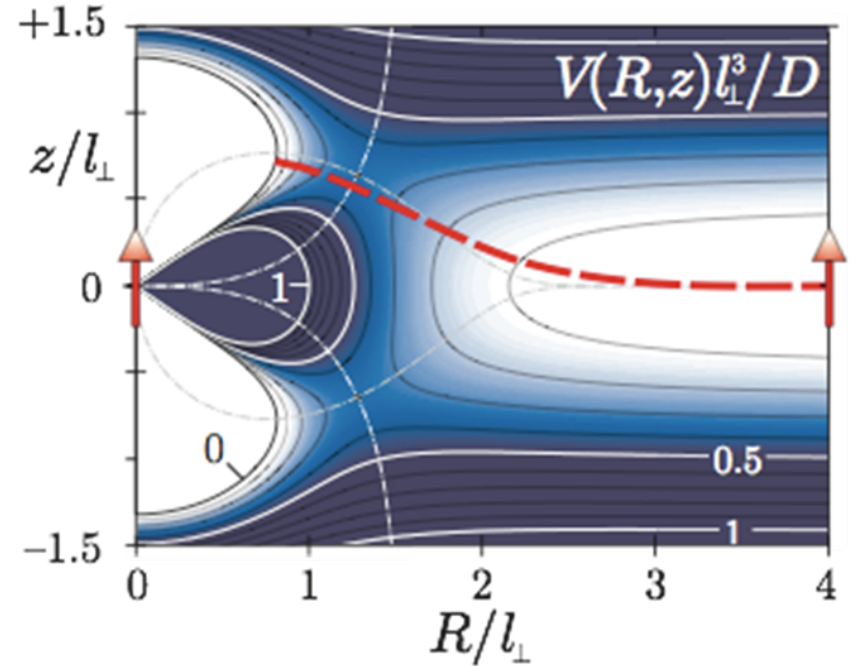
## Effective interaction

- interaction potential with transverse trapping potential

$$V(\mathbf{r}) = D \left[ \frac{1}{r^3} - 3 \frac{z^2}{r^5} \right] + \frac{m\omega_z^2}{2} z^2$$

- characteristic length scale  $l_{\perp} = \left( \frac{Dm}{\hbar^2 a_{\perp}} \right)^{1/5} a_{\perp}$

- potential barrier: larger than kinetic energy



## Tunneling rate: attempt frequency

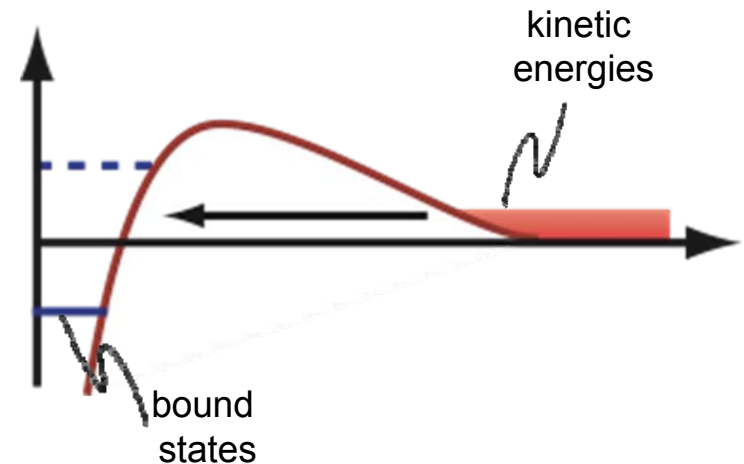
- semi-classical rate (instanton techniques)

$$\Gamma = A \exp(-S_E/\hbar)$$

- Euclidean action of the instanton trajectory

$$S_E = \hbar \left( \frac{Dm}{\hbar^2 a_{\perp}} \right)^{2/5} C$$

numerical factor:  $C \approx 5.8$



# Crystalline phase

