

# HERE BE DRAGONS: THE UNEXPLORED CONTINENTS OF THE CMSSM

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Timothy Cohen  
(SLAC)

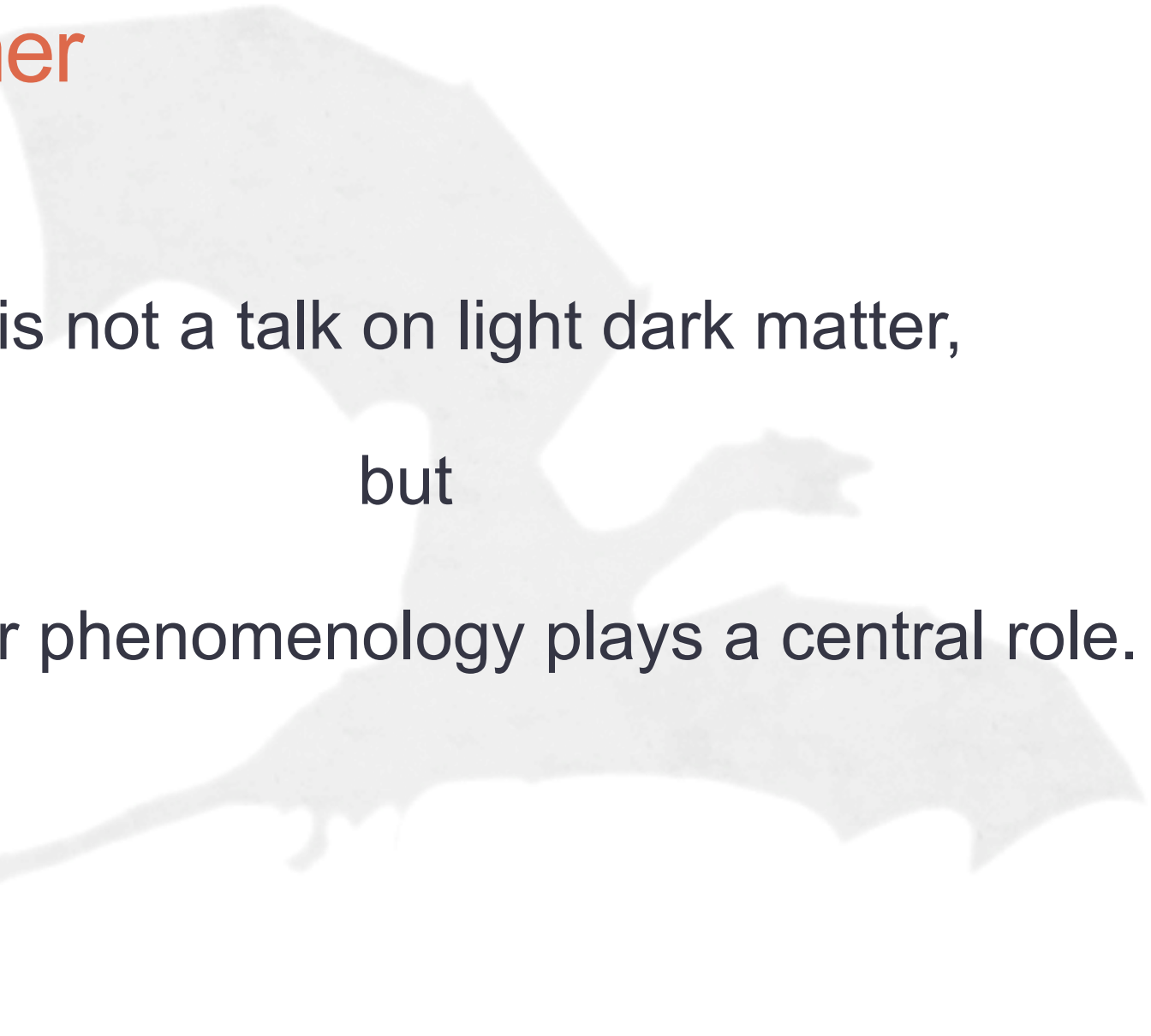
with Jay Wacker

[arXiv:13XX.soon](#)

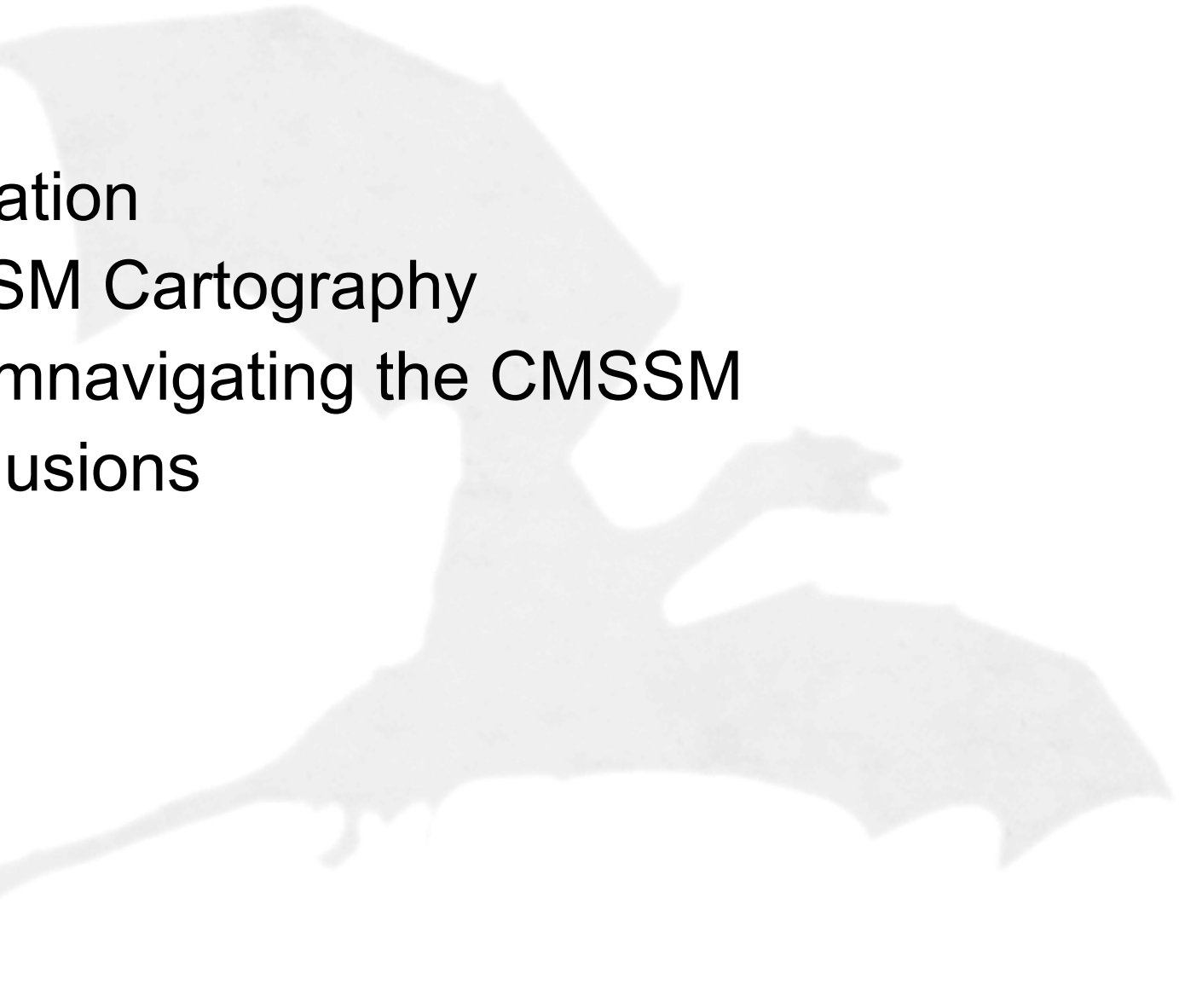
MCTP Light Dark Matter Workshop  
April 17, 2013

# Disclaimer

This is not a talk on light dark matter,  
but  
dark matter phenomenology plays a central role.



# Outline

- I) Motivation
  - II) CMSSM Cartography
  - III) Circumnavigating the CMSSM
  - IV) Conclusions
- 



# MOTIVATION

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# The MSSM in the Era of Higgs Discovery

- A SM-like Higgs has been discovered at 125 GeV.  
ATLAS [arXiv:1207.7214]  
CMS [arXiv:1207.7235]
- This measurement is “consistent” with the MSSM (and its extensions).
  - Stops can lie from  $O(100)$  GeV to  $O(100)$  TeV.

# The MSSM in the Era of Higgs Discovery

- A SM-like Higgs has been discovered at 125 GeV.  
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- This measurement is “consistent” with the MSSM (and its extensions).
  - Stops can lie from  $O(100)$  GeV to  $O(100)$  TeV.
- The motivation for weak-scale superpartners still stands:
  - Solves the hierarchy problem;
  - Explains the dark matter;
  - Predicts gauge coupling unification.

# The MSSM in the Era of Higgs Discovery

- The parameter space of the MSSM is enormous.
  - The soft supersymmetry breaking Lagrangian includes more than 120 new dimensionful terms.
- How can we map out all possible signatures?
  - Simplified models: isolate particles responsible for the signature of interest. The parameter space becomes tractable; there are typically only a few masses and branching ratios to specify.
    - [Alwall, Le, Listanti, Wacker \[arXiv:0809.3264\]](#); [Alwall, Schuster, Toro \[arXiv:0810.3921\]](#); [LHC New Physics Working Group \[arXiv:1105.2838\]](#)
  - pMSSM: phenomenologically motivated reduction to 19 parameters.
    - [Berger, Gainer, Hewett, Rizzo \[arXiv:0812.0980\]](#)
  - CMSSM/mSUGRA: 4 parameters.
    - [Chamseddine, Arnowitt, Nath \[PRL 49 \(1982\)\]](#); [Barbieri, Ferrara, Savoy \[PLB \(1982\)\]](#); [Hall, Lykken, Weinberg \[PRD \(1983\)\]](#)
- 4 parameters is potentially tractable.
- Can we understand all predictions of the CMSSM ansatz?

# A simple ansatz - a wide range of dynamics

- The CMSSM is a four dimensional subspace of the  $R$ -parity conserving MSSM.
- It is defined at the GUT scale by the following (real) inputs:
  - The unified scalar soft mass,  $M_0$ .
  - The unified gaugino mass:  $M_{1/2}$ .
  - The unified  $A$ -term:  $A_0$ .
  - The ratio of the Higgs vevs:  $\tan \beta$  (traded for the  $B_\mu$  term).

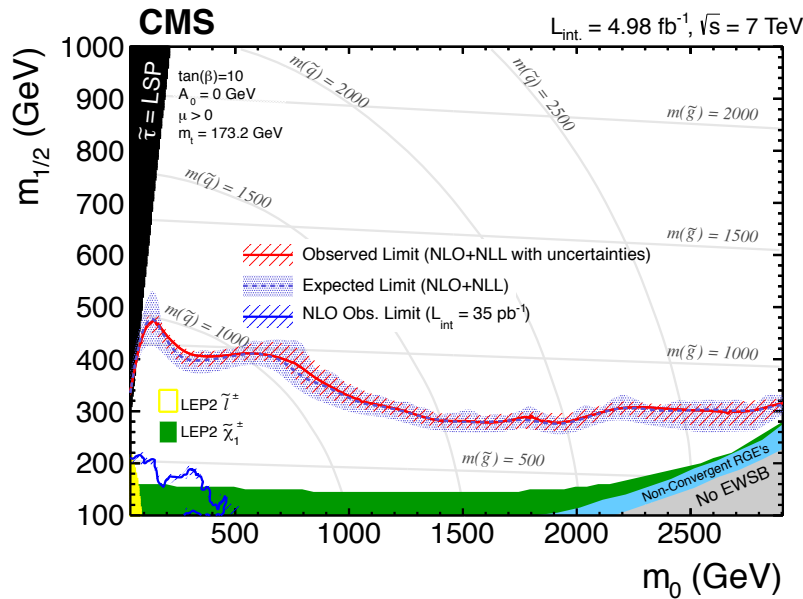


# A simple ansatz - a wide range of dynamics

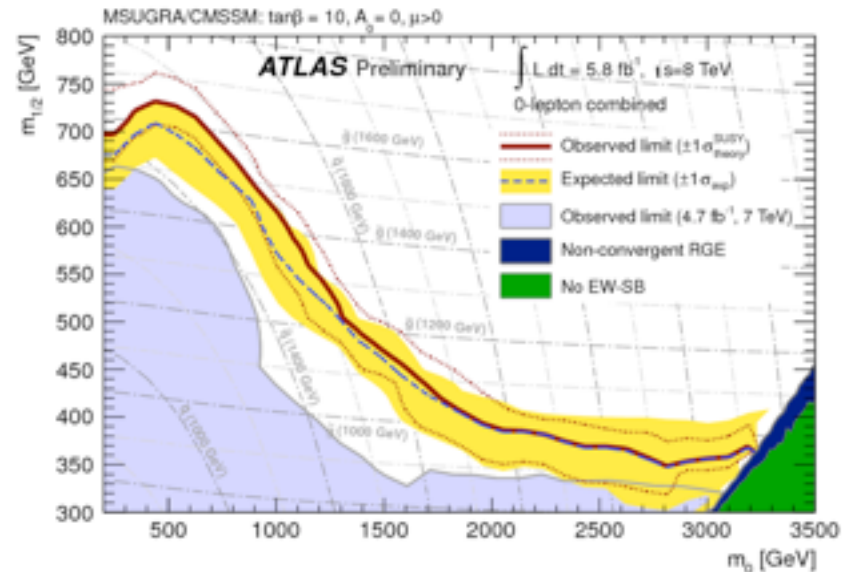
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  - The ratio of the Higgs vevs:  $\tan \beta$  (traded for the  $B_\mu$  term).
- These parameters are evolved to the weak scale using the renormalization group equations (RGEs).
- The  $\mu$ -term is determined by requiring that the  $Z$ -boson mass match the measured value.
- Since the RGEs are integrated over 14 orders of magnitude, the relation between the low energy parameters and the inputs is highly non-linear.

# The state of the art

- Both ATLAS and CMS put limits on the CMSSM:



CMS [arXiv:1205.6615]

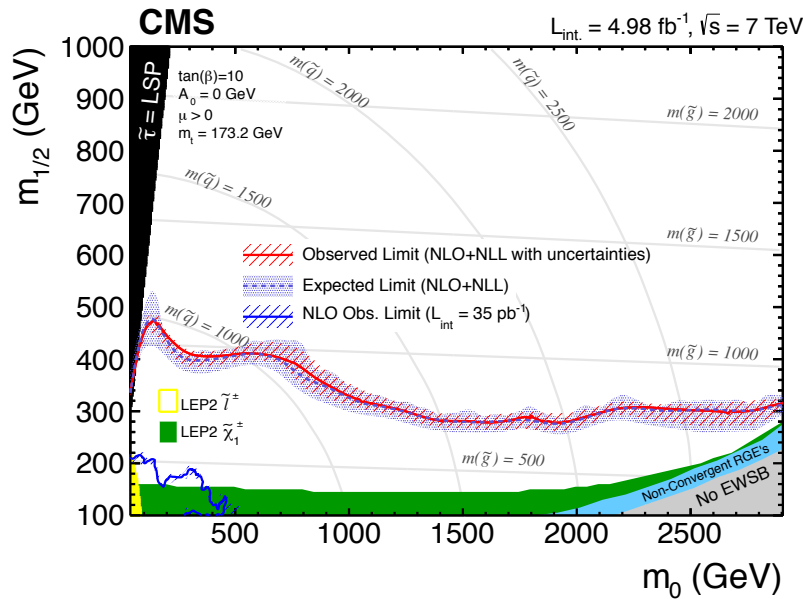


ATLAS-CONF-2012-109

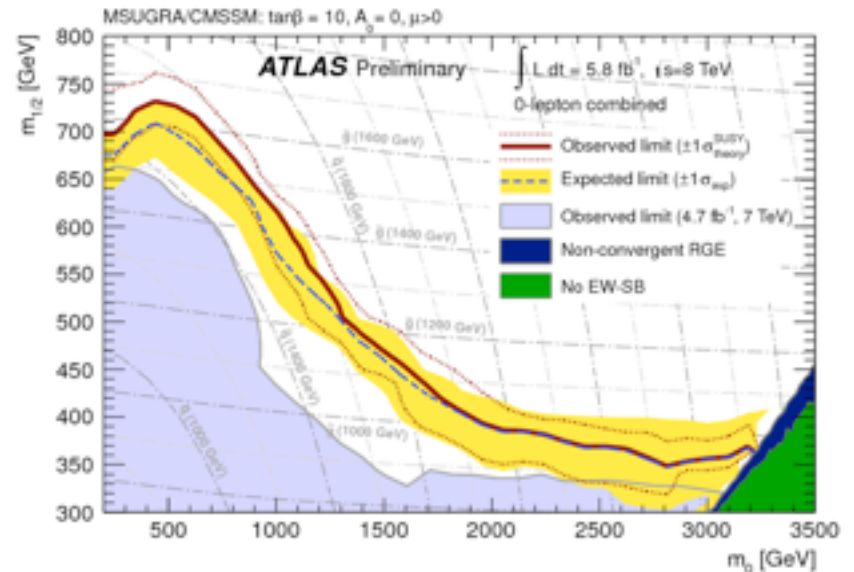
- They exclude a region of the  $M_{1/2}$  versus  $M_0$  plane for a fixed choice of  $A_0$  and  $\tan \beta$ .

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- They exclude a region of the  $M_{1/2}$  versus  $M_0$  plane for a fixed choice of  $A_0$  and  $\tan \beta$ .
- What is the Higgs mass?
- Does the neutralino overclose the Universe?

# Our approach to the CMSSM

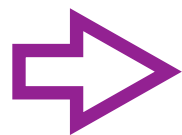
- We will require that the Higgs mass is  $\sim 125$  GeV and the neutralino comprises all of the dark matter.
- “Quadrants” are defined by the  $\text{sign}(A_0)$  and the  $\text{sign}(\mu)$ .
- Schematically, the RGEs for  $A$  and  $B$  terms are given by
$$16 \pi^2 \frac{d}{dt} A = A (|y|^2 - g^2) + y g^2 M,$$
$$16 \pi^2 \frac{d}{dt} B = B (|y|^2 - g^2) + \mu (A y^\dagger + g^2 M),$$
- The low energy behavior can be very different depending on these signs.

# Classification

- What process determines the relic abundance?
  - “light  $\tilde{\chi}^0$ ”: annihilation is dominated by the  $Z^0$  and  $h$  poles.
  - “well-tempered”: annihilation via Higgsino/Bino mixing to  $W^+ W^-$ .
  - “ $A^0$  pole”: annihilation is dominated by an s-channel  $A^0$  resonance.
  - “stau coannihilation”
  - “stop coannihilation”

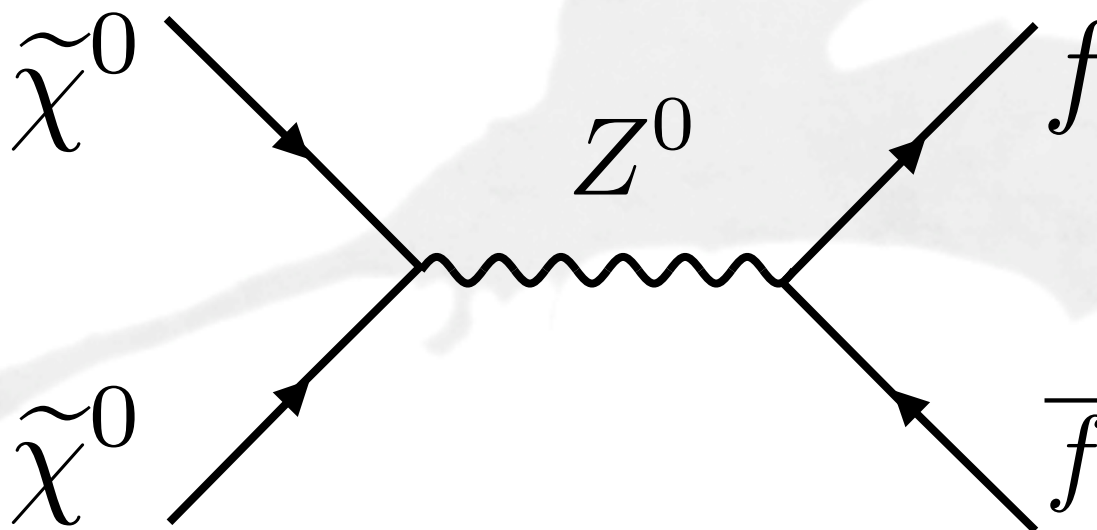
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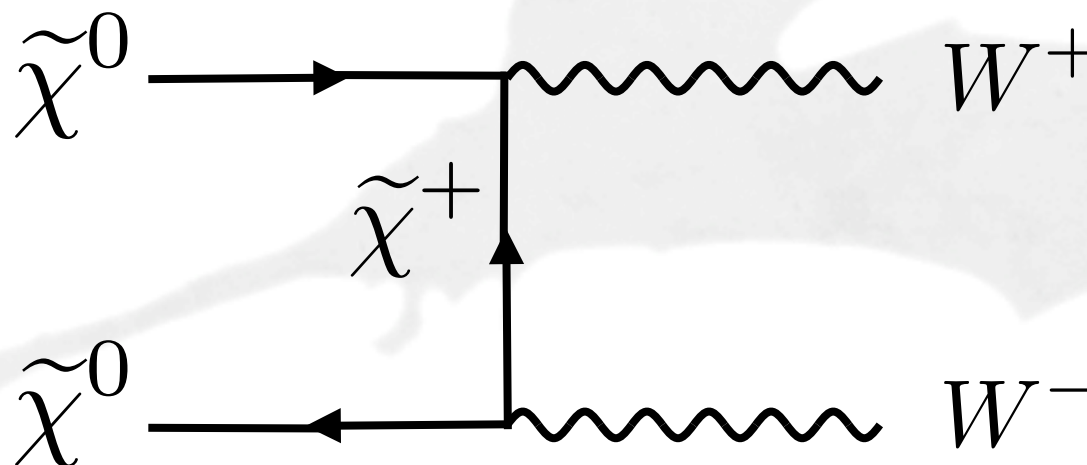
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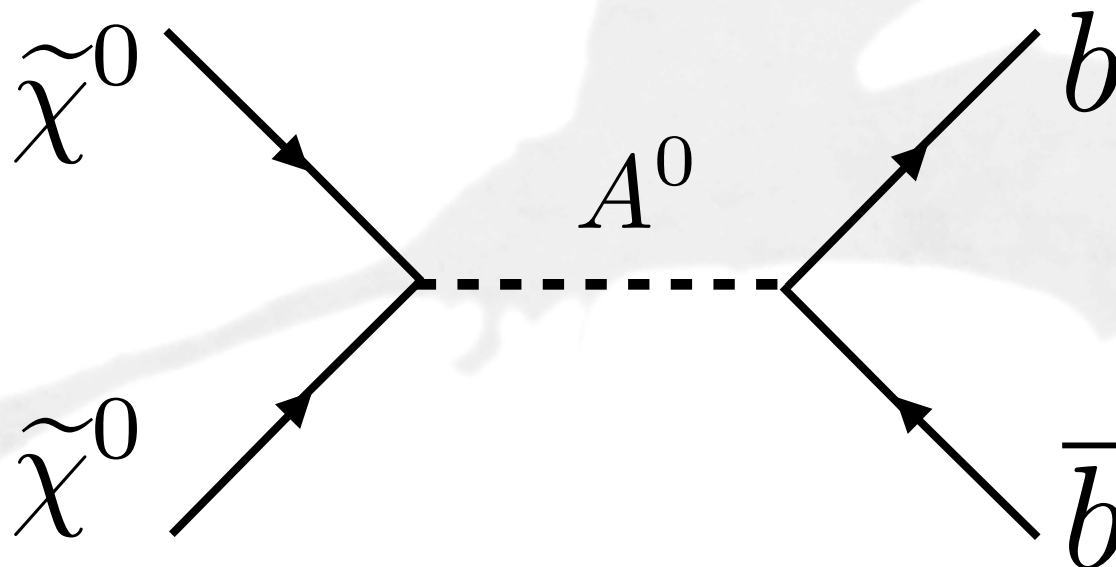
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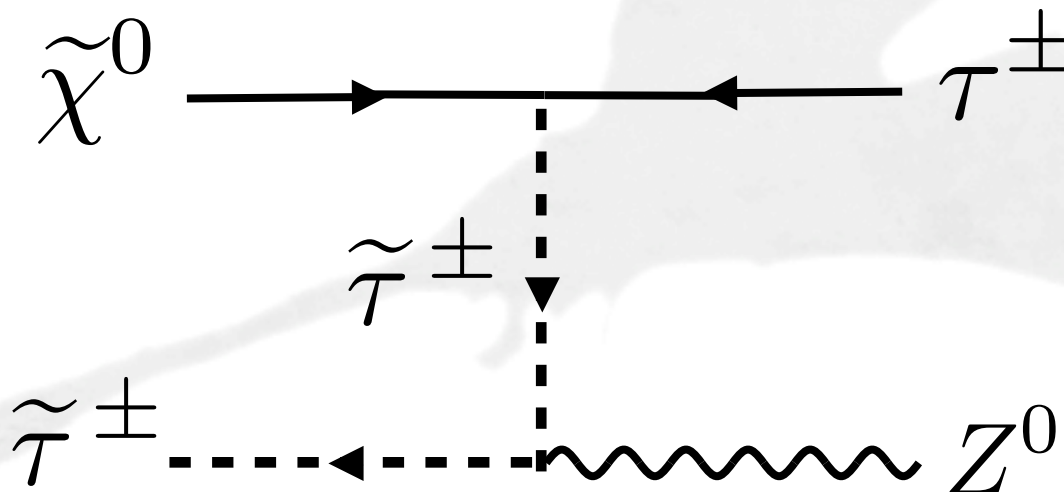
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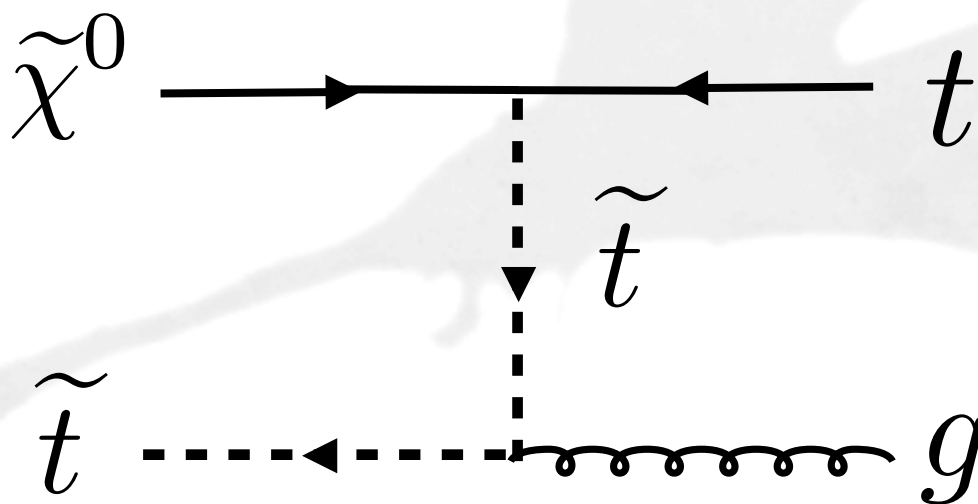
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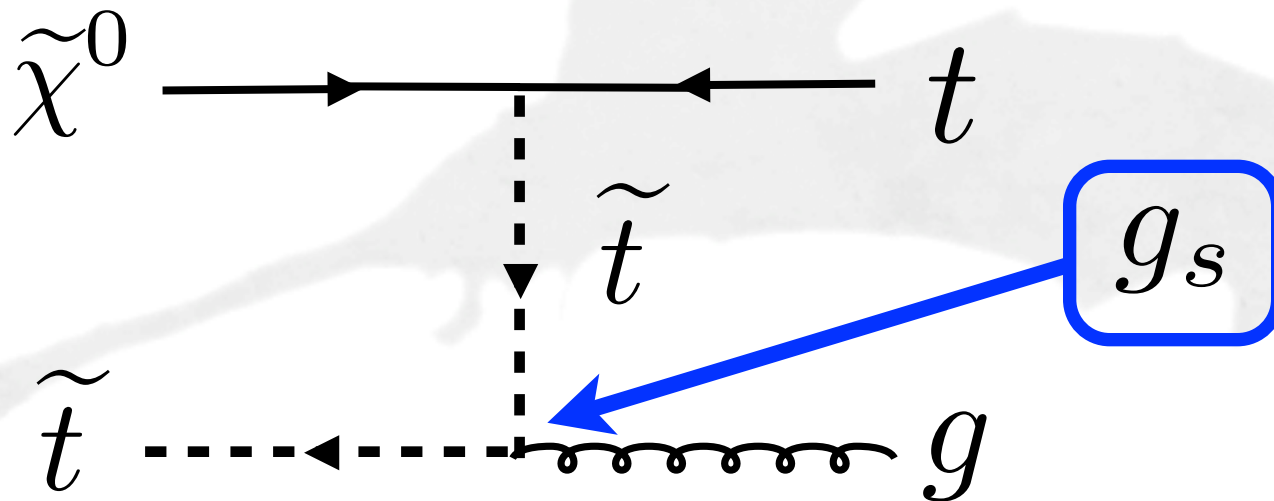
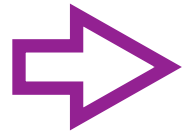
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# The CMSSM should be compact

- Requiring a 125 GeV Higgs boson implies that one can not take  $M_0$  to be arbitrarily large.
- Relic density
  - The pure Bino limit bounds  $M_{1/2}$ .
    - The lightest gaugino is the Bino.
    - As one decouples the scalars, the Bino becomes inert.
    - Its early Universe annihilation cross section goes to zero.
    - It freezes out with too large a relic density.
  - The pure Higgsino limit bounds  $M_0$ .
    - As one decouples the gauginos, the LSP becomes Higgsino like.
    - If the mass of a pseudo-Dirac Higgsino is greater than  $\sim 1$  TeV, it freezes out with too large a relic density.
- Requiring the lifetime of our vacuum be longer than the age of the Universe bounds  $A_0$ .
- Perturbativity of the bottom Yukawa coupling bounds  $\tan \beta$ .



# CMSSM CARTOGRAPHY

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# Tools

- SoftSUSY v3.3.7 computes the low energy spectrum from the CMSSM inputs. [Allanach \[arXiv:hep-ph/0104145\]](#)
  - The two loop MSSM RGEs are included (leading log decoupling is accounted for by the inclusion of all 1-loop finite terms).
  - The two loop contributions to the Higgs potential are included.
- DarkSUSY v5.1.1 computes the relic density and direct detection cross sections.
  - All 2-2 scattering processes are included. [Gondolo, Edsjo, Ullio, Bergstrom, Schelke \[arXiv:astro-ph/0406204\]](#)
- SUSY-HIT v1.3 computes the decay tables. [Djouadi, Muhlleitner, Spira \[arXiv:hep-ph/0609292\]](#)
- We have had 186+ cores running for roughly 4 continuous months.

# Constraints

- We take a 3 GeV error for the theoretical prediction for the Higgs mass:

$$122 \text{ GeV} < m_h < 128 \text{ GeV}$$

Allanach, Djuadi, Kneur, Porod, Slavich [arXiv:hep-ph/0406166]

- We require the relic density be in the range:

$$0.08 < \Omega h^2 < 0.14$$

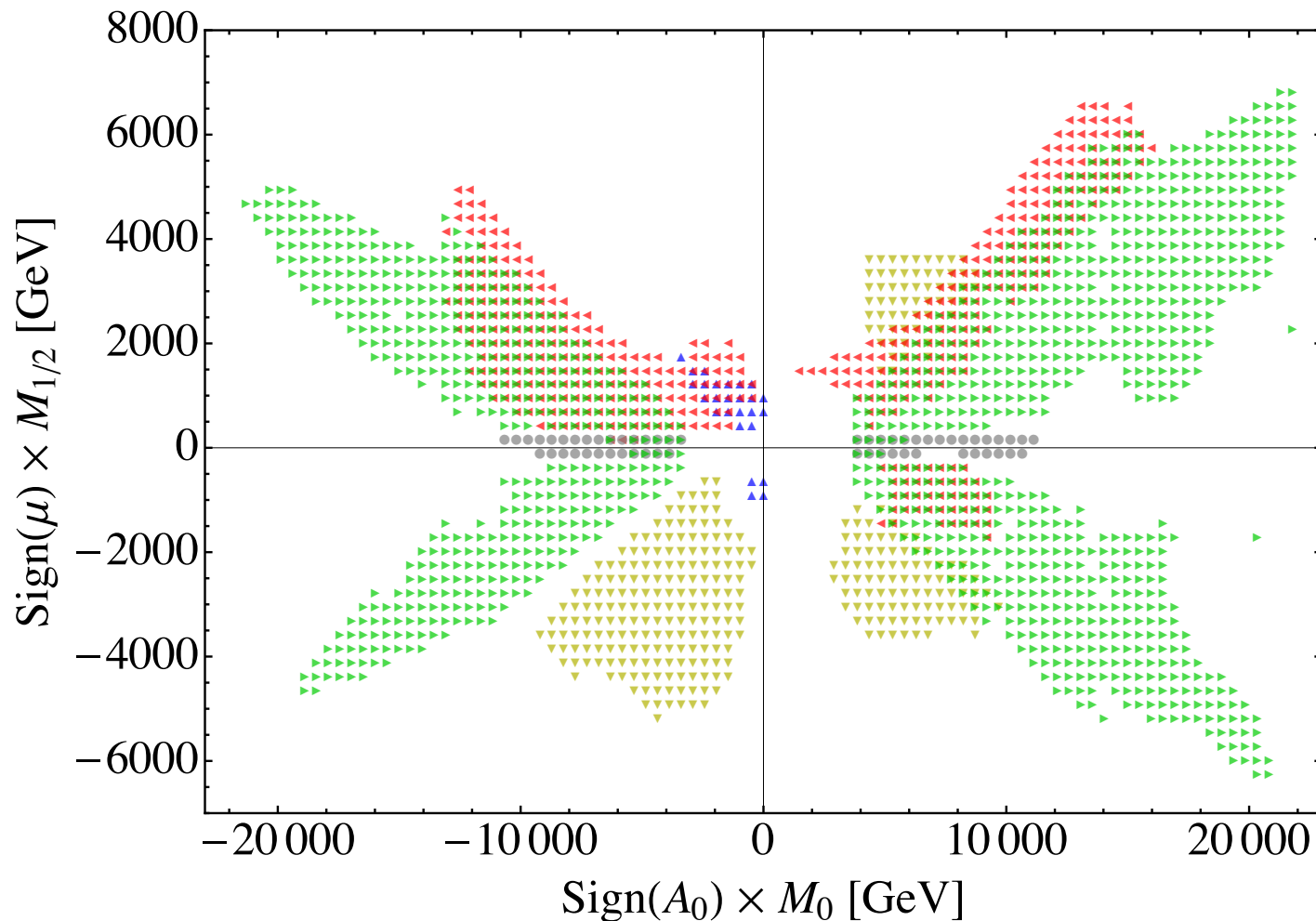
- We require that the lifetime for the vacuum to decay to a charge/color breaking minimum be longer than the age of the Universe:

$$|a_t|^2 < (7.5 m_{q_3}^2 + 7.5 m_{u_3^c}^2 + 3 (m_{H_u}^2 + |\mu|^2))$$

- with a similar condition for staus. [Kusenko, Langacker, Segre \[arXiv:hep-ph/9602414\]](#)
- We require that the chargino mass satisfy a naive LEP bound:

$$\tilde{m}_{\chi^+} > 100 \text{ GeV}$$

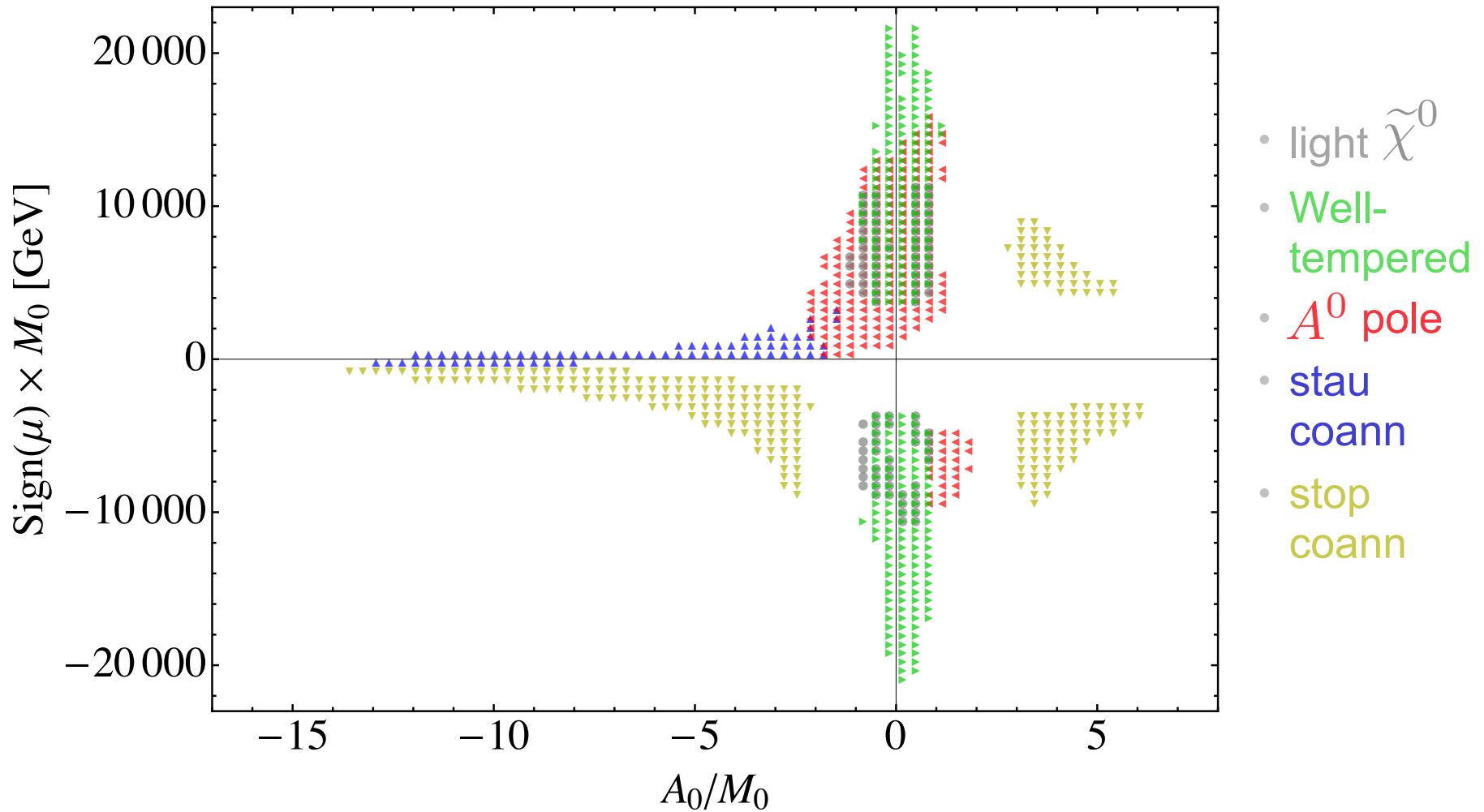
# Charting the CMSSM



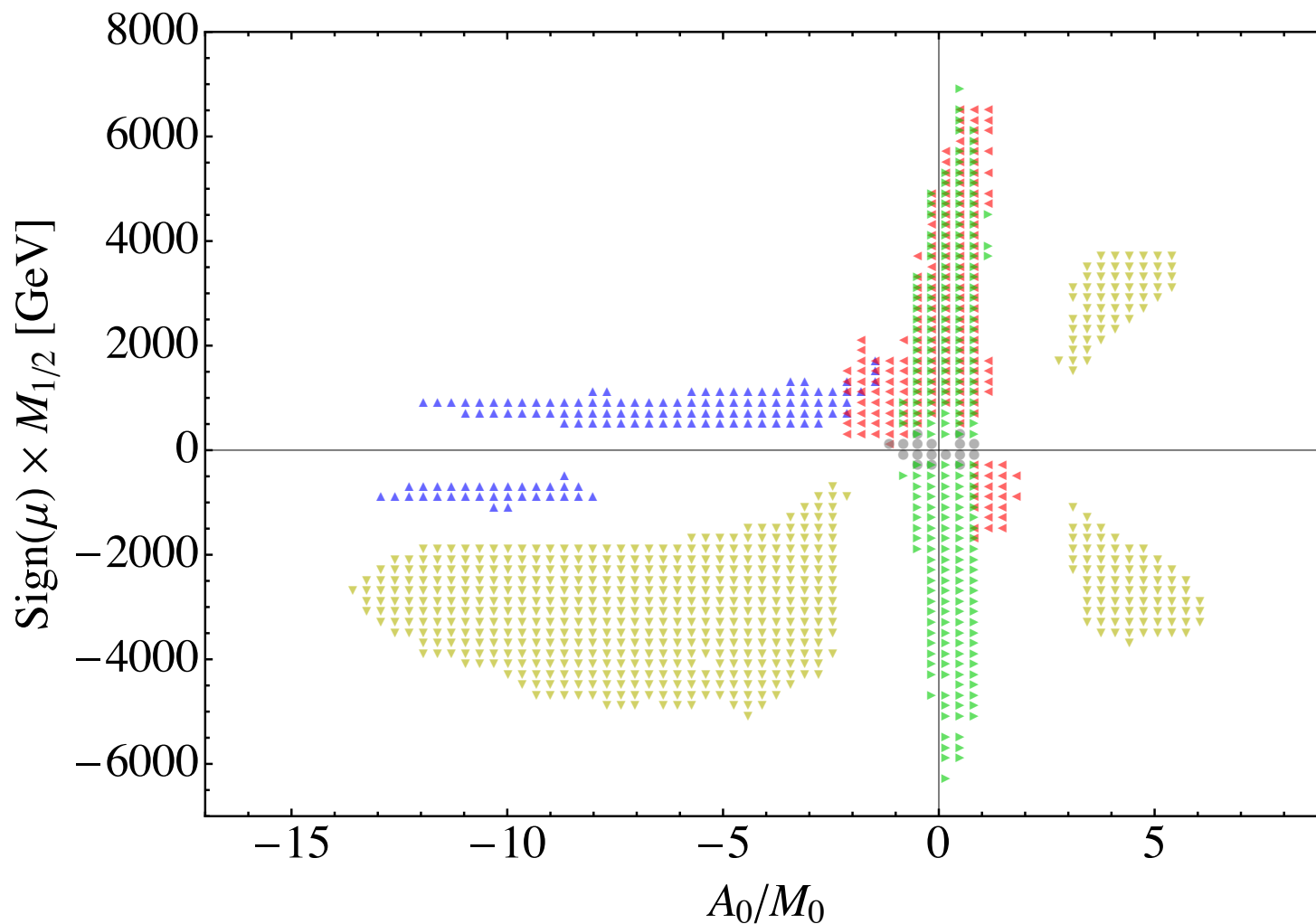
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- Well-tempered
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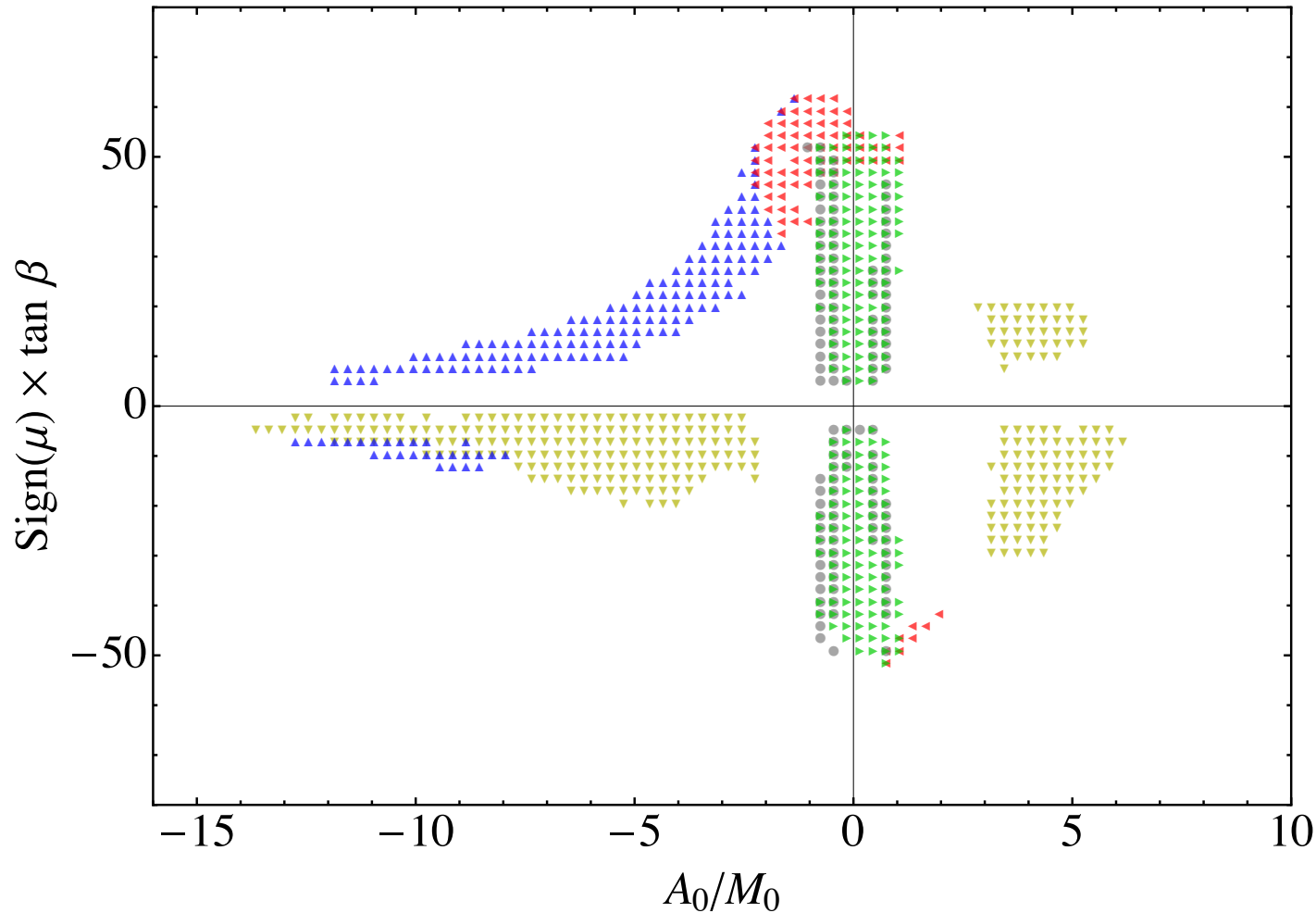


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# Lessons

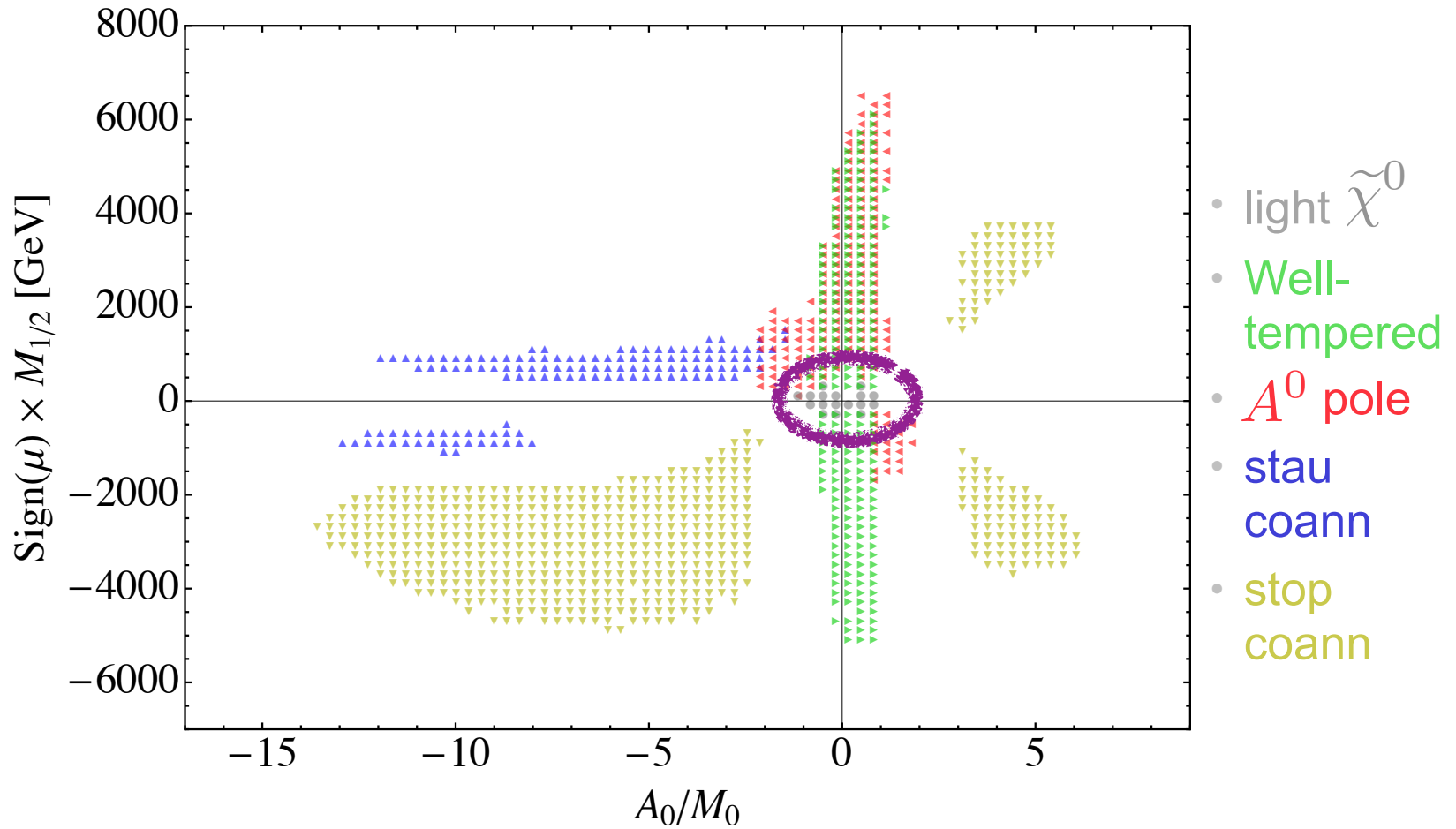
- The CMSSM is compact.
- The size of the allowed parameter space is huge!
- Our classification scheme is a useful way to organize the CMSSM.
- There is a range of possible low energy signatures.
- The rest of this talk will be devoted to exploring them.

# CIRCUMNAVIGATING THE CMSSM

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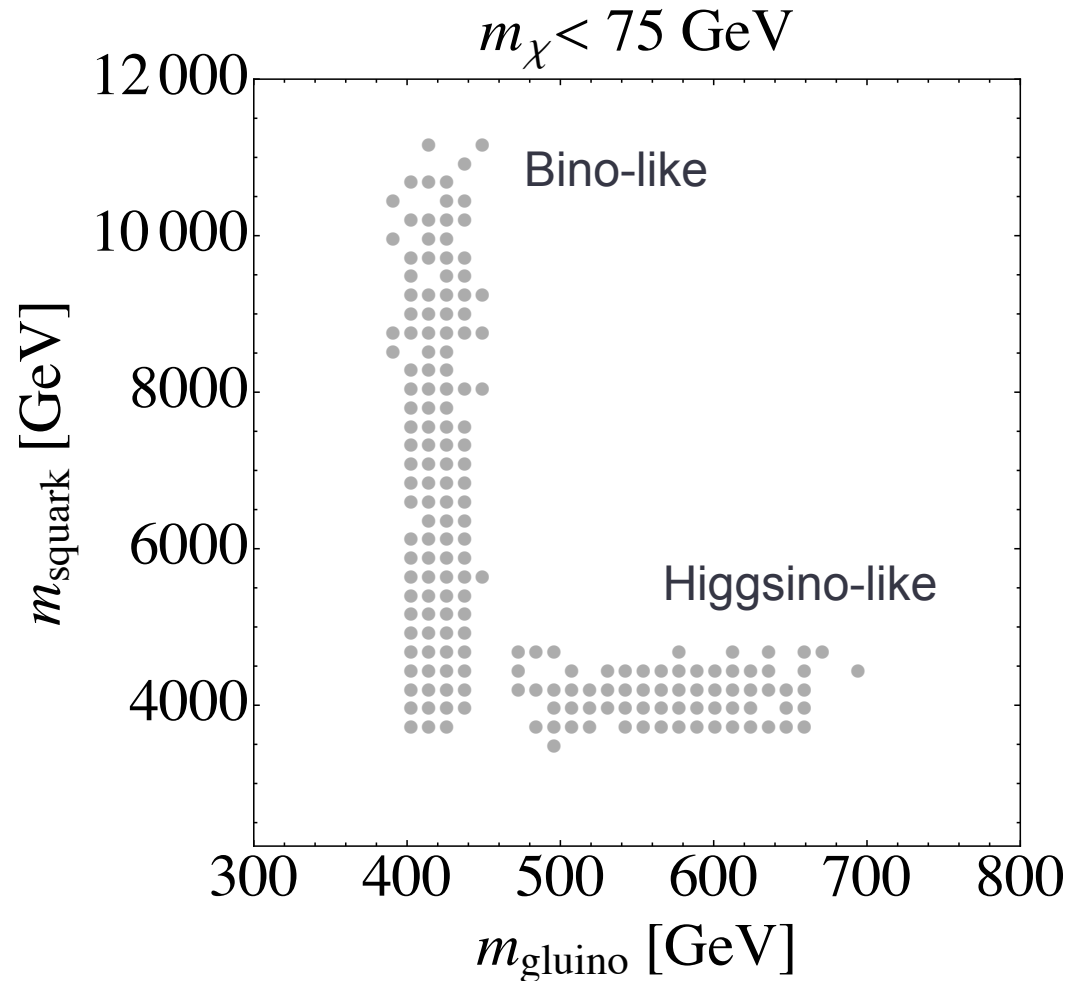
Light  $\tilde{\chi}^0$

# Setting sail for light $\tilde{\chi}^0 \iff \tilde{m}_{\chi^0} < 75 \text{ GeV}$



- $2 \text{ TeV} \lesssim M_0 \lesssim 12 \text{ TeV}$
- $5 \lesssim \tan \beta \lesssim 50$

# Light $\tilde{\chi}^0$ implies light gluinos



# Has the LHC excluded this region?

- Take as a benchmark:

$M_0$	$M_{1/2}$	$A_0$	$\tan \beta$	$\text{sign}(\mu)$	$ \mu $	$B_\mu$
5455.8	132.315	-3480.24	15.5977	1	301.773	$2.01762 \times 10^8$

- Squarks and sleptons are heavier than 5 TeV.
- The gluino is 409 GeV and the LSP is 57 GeV.
- $\tilde{g} \rightarrow q + \bar{q} + Z^0 + \tilde{\chi}_0$ 
  - The 7 TeV CMS search yields  $\sigma \times \text{BR} \lesssim 1$ . [CMS \[arXiv:1204.3774\]](#)
  - The 7 TeV prediction is  $\sigma \times \text{BR} \simeq 1.0$  pb.
- $\tilde{g} \rightarrow q + \bar{q} + \tilde{\chi}^0$ 
  - The 7 TeV CMS Razor search does not exclude this channel. [CMS \[CMS-PAS-SUS-12-005\]](#)
- $\tilde{g} \rightarrow q + \bar{q}' + W^\pm + \tilde{\chi}_0$ 
  - The 7 TeV ATLAS search for (requiring same sign  $W^\pm$ ) does not exclude this channel. [ATLAS \[arXiv:1208.0949\]](#)
- So the exclusion is borderline at 7 TeV without performing any combinations.
- Likely excluded at 8 TeV (unless efficiency drops for low masses; no detailed efficiency plots are public yet).

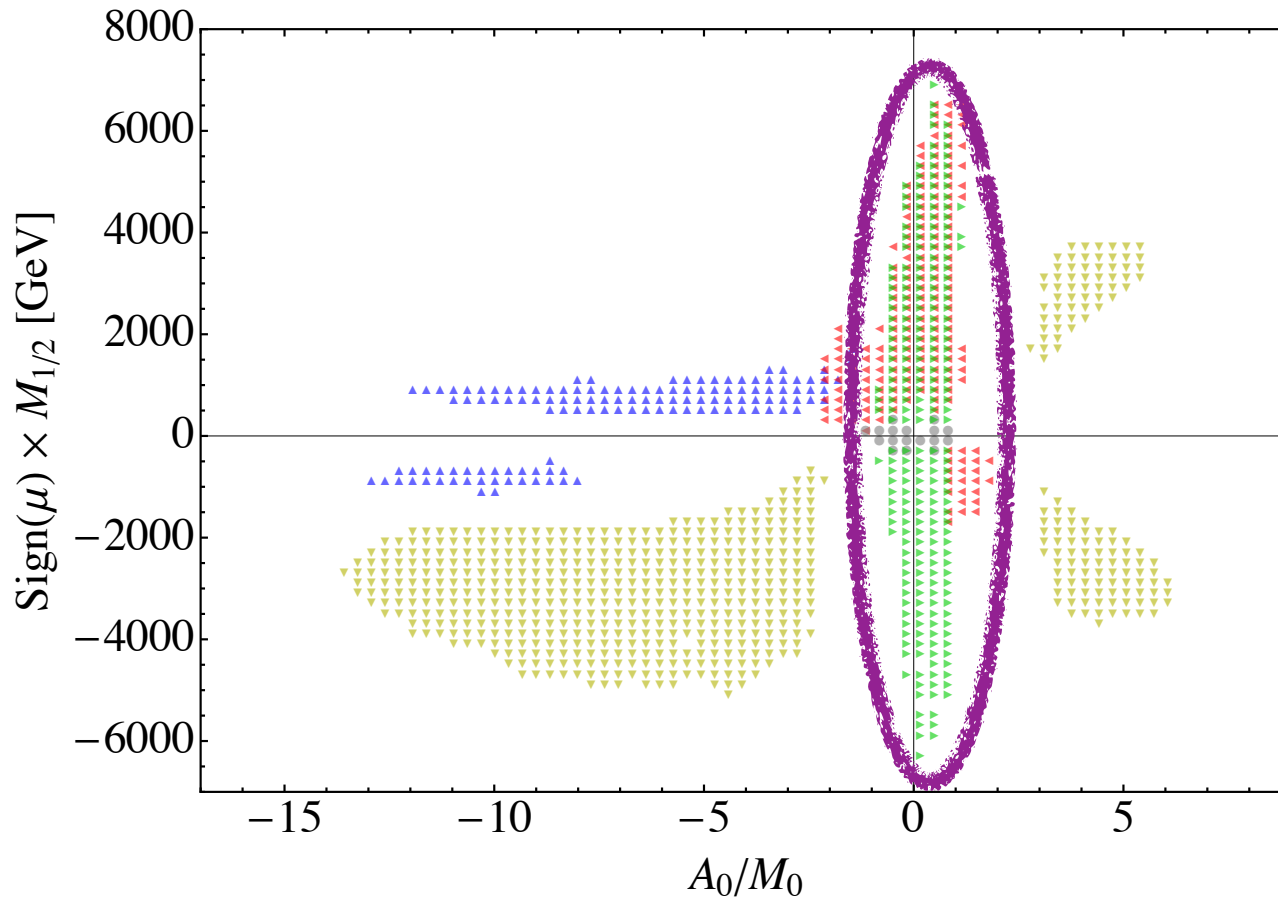


# CIRCUMNAVIGATING THE CMSSM

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Well-tempered

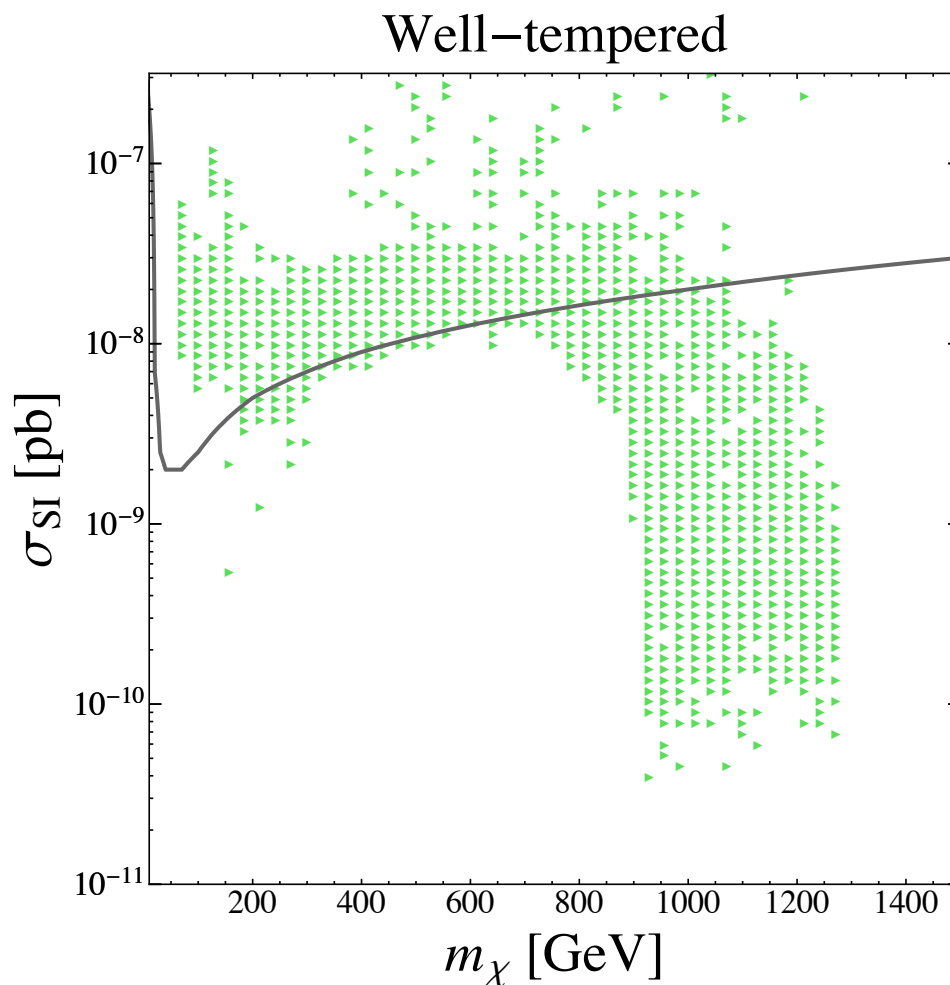
# Setting sail for well-tempered



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- Well-tempered
- $A^0$  pole
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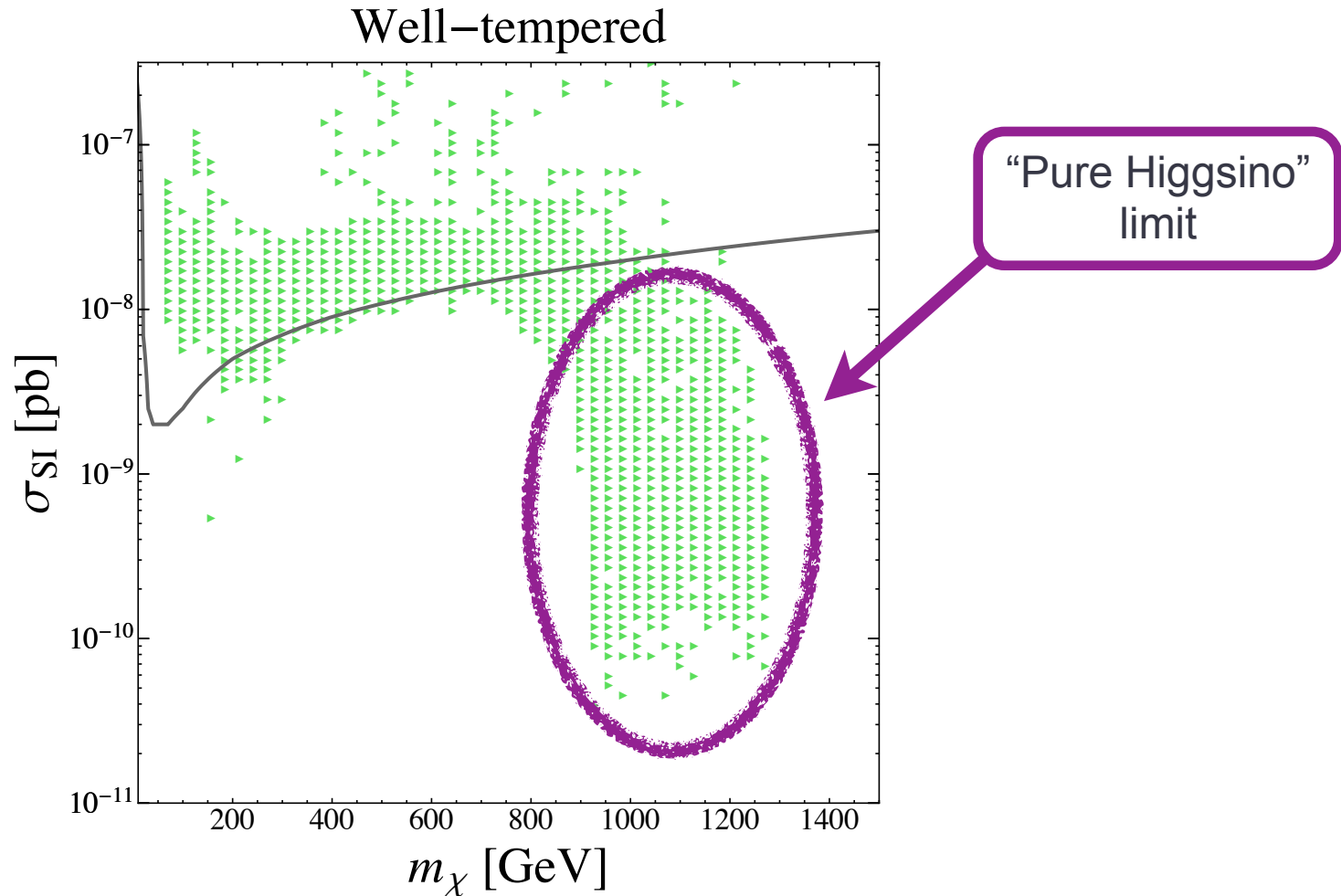
- $4 \text{ TeV} \lesssim M_0 \lesssim 20 \text{ TeV}$
- $5 \lesssim \tan \beta \lesssim 50$

# Will direct detection exclude this region?



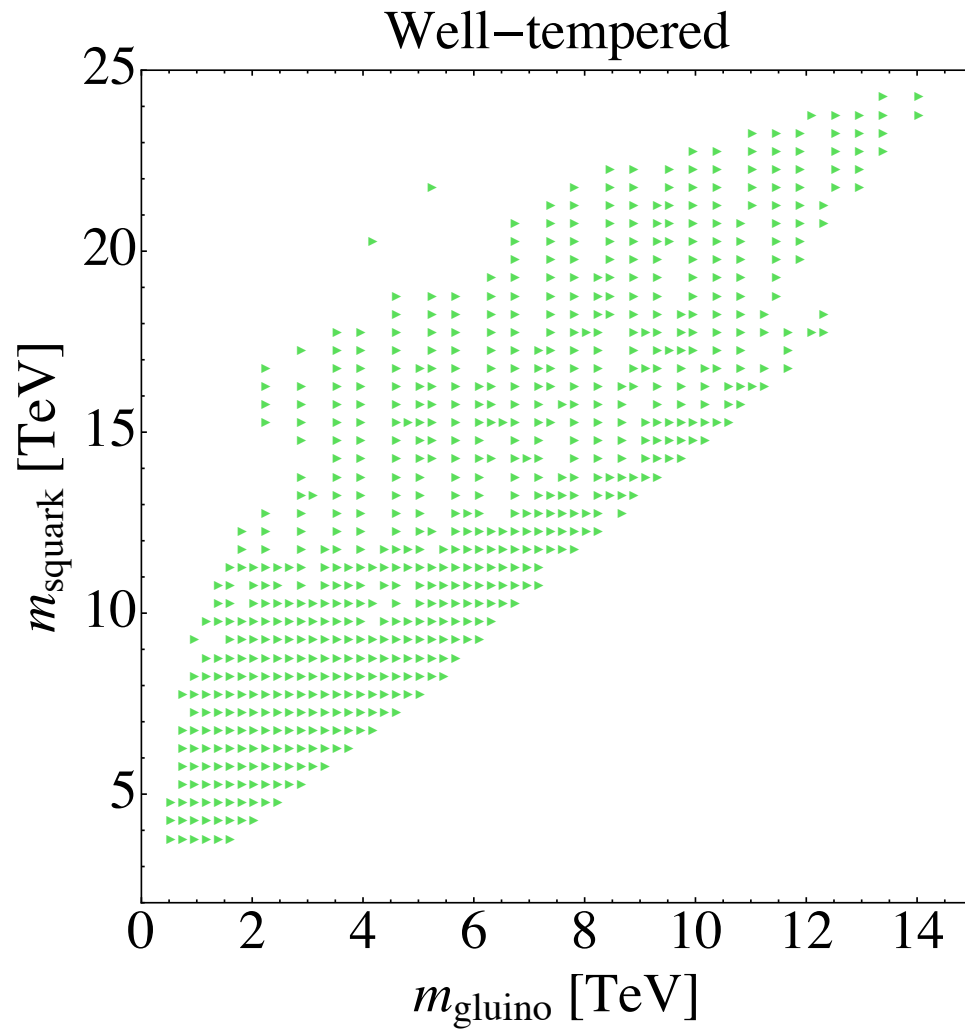
- A 1-ton Xenon experiment can reach spin-independent cross sections of  $5 \times 10^{-12}$  pb at 300 GeV.

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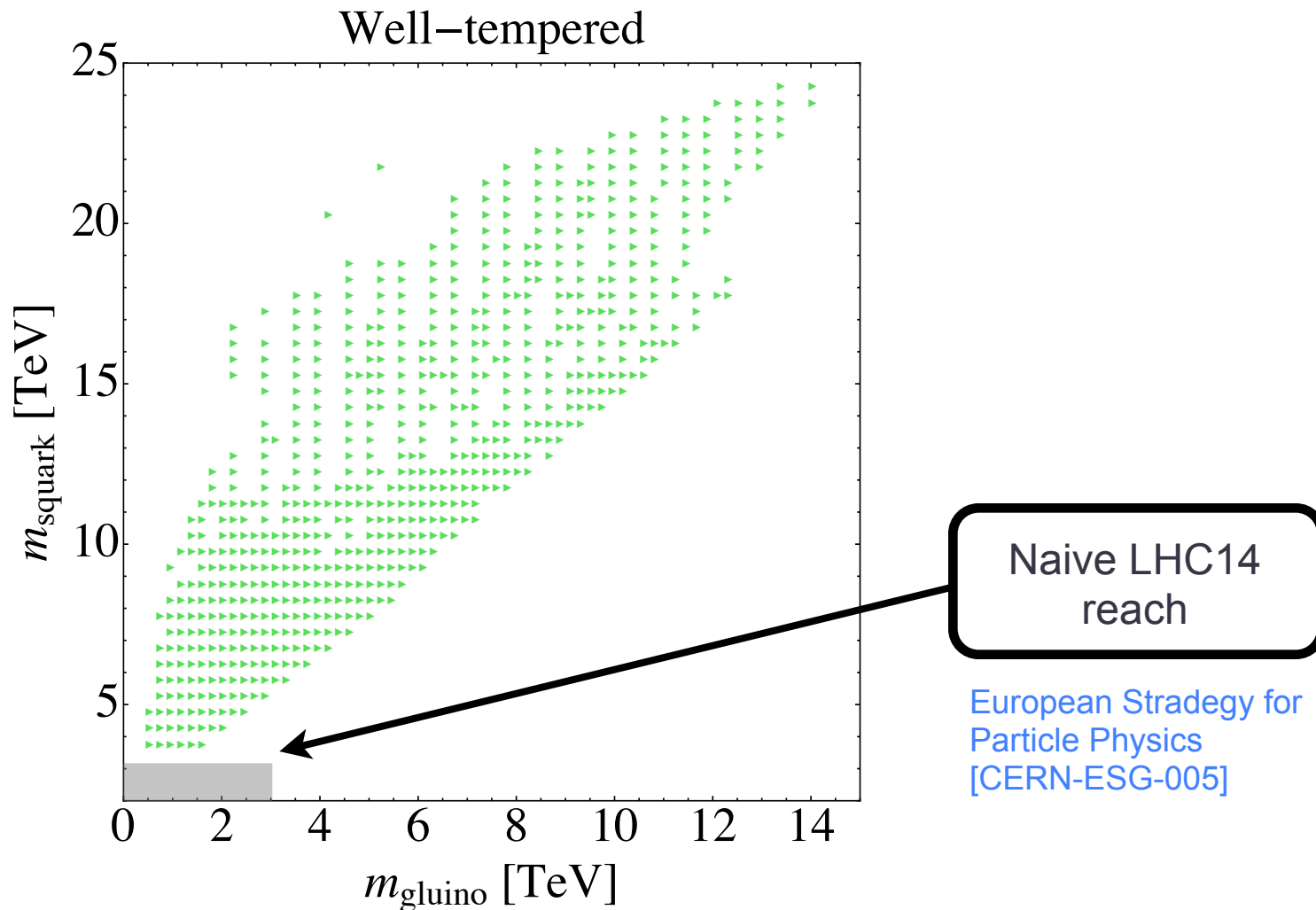


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# What about the LHC?



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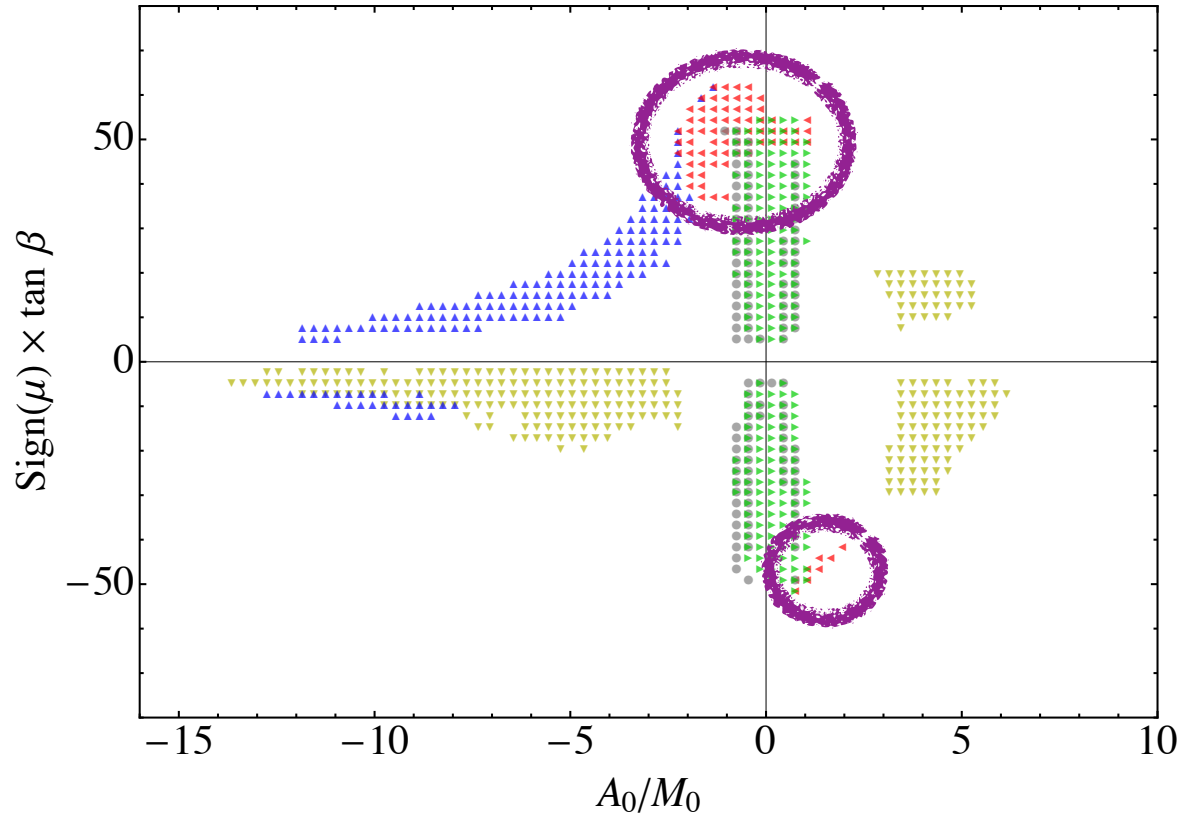
- The LHC will have little impact on the well-tempered spectra.

# CIRCUMNAVIGATING THE CMSSM

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$A^0$  pole annihilation

# Setting sail for $A^0$ pole annihilation

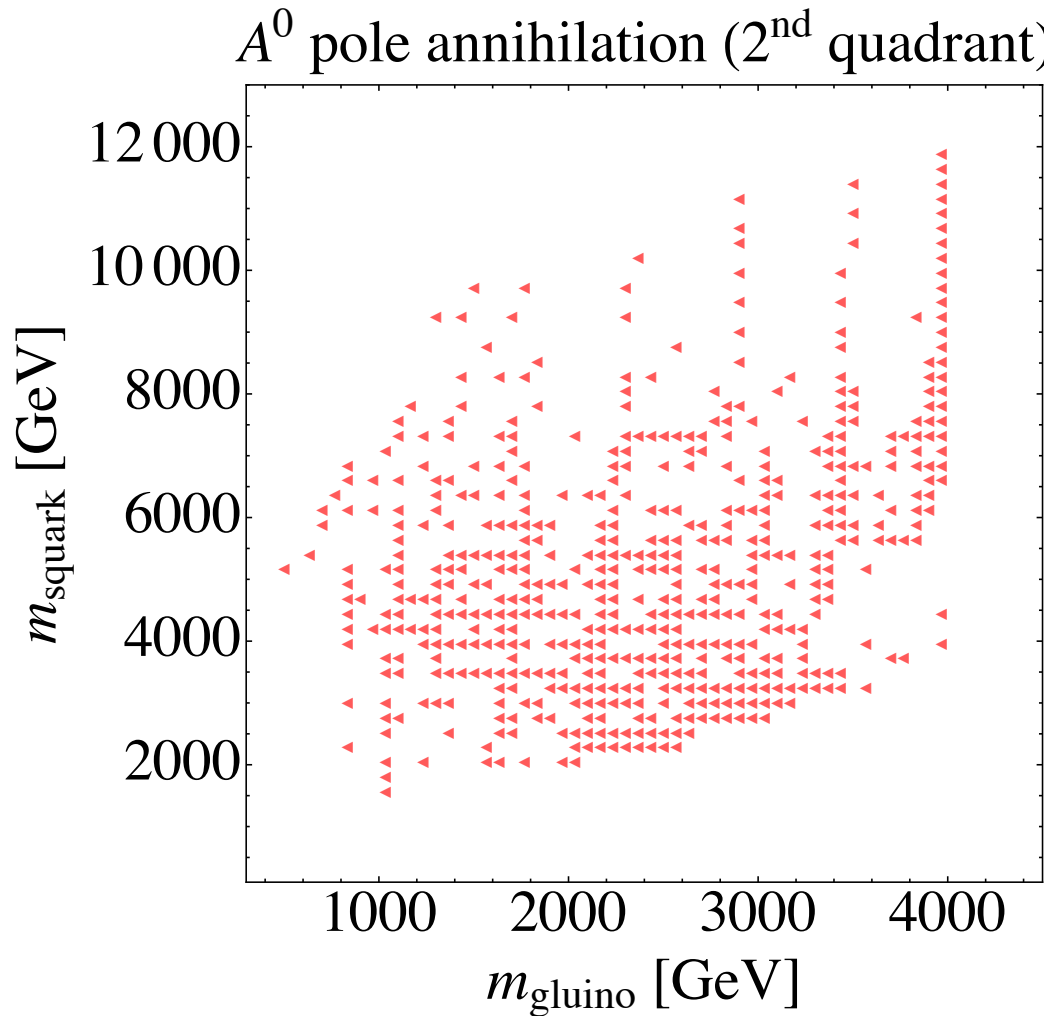


- light  $\tilde{\chi}^0$
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- $500 \text{ GeV} \lesssim M_0 \lesssim 16 \text{ TeV} \quad [\mu > 0]$
- $200 \text{ GeV} \lesssim M_{1/2} \lesssim 7 \text{ TeV} \quad [\mu > 0]$
- $5 \text{ TeV} \lesssim M_0 \lesssim 10 \text{ TeV} \quad [\mu < 0]$
- $300 \text{ GeV} \lesssim M_{1/2} \lesssim 2 \text{ TeV} \quad [\mu < 0]$

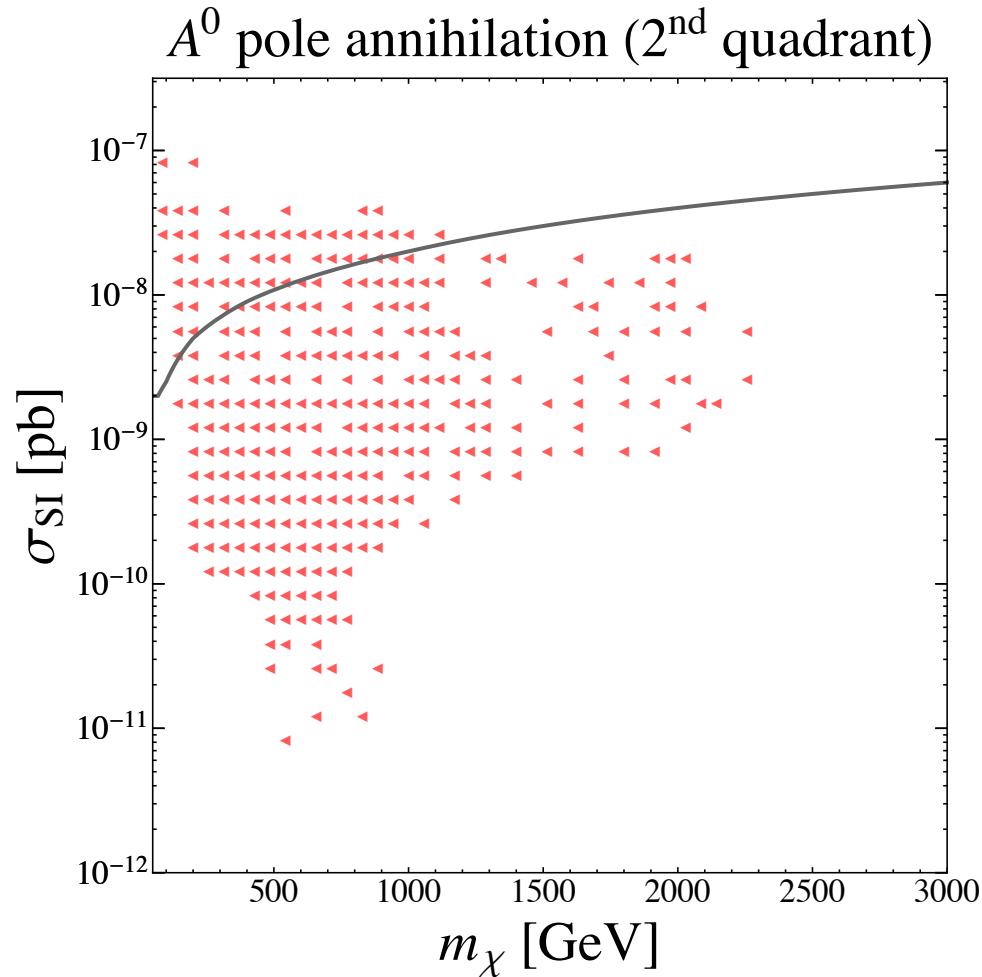


# The squark-gluino plane



- 1<sup>st</sup> quadrant is similar.

# Direct detection



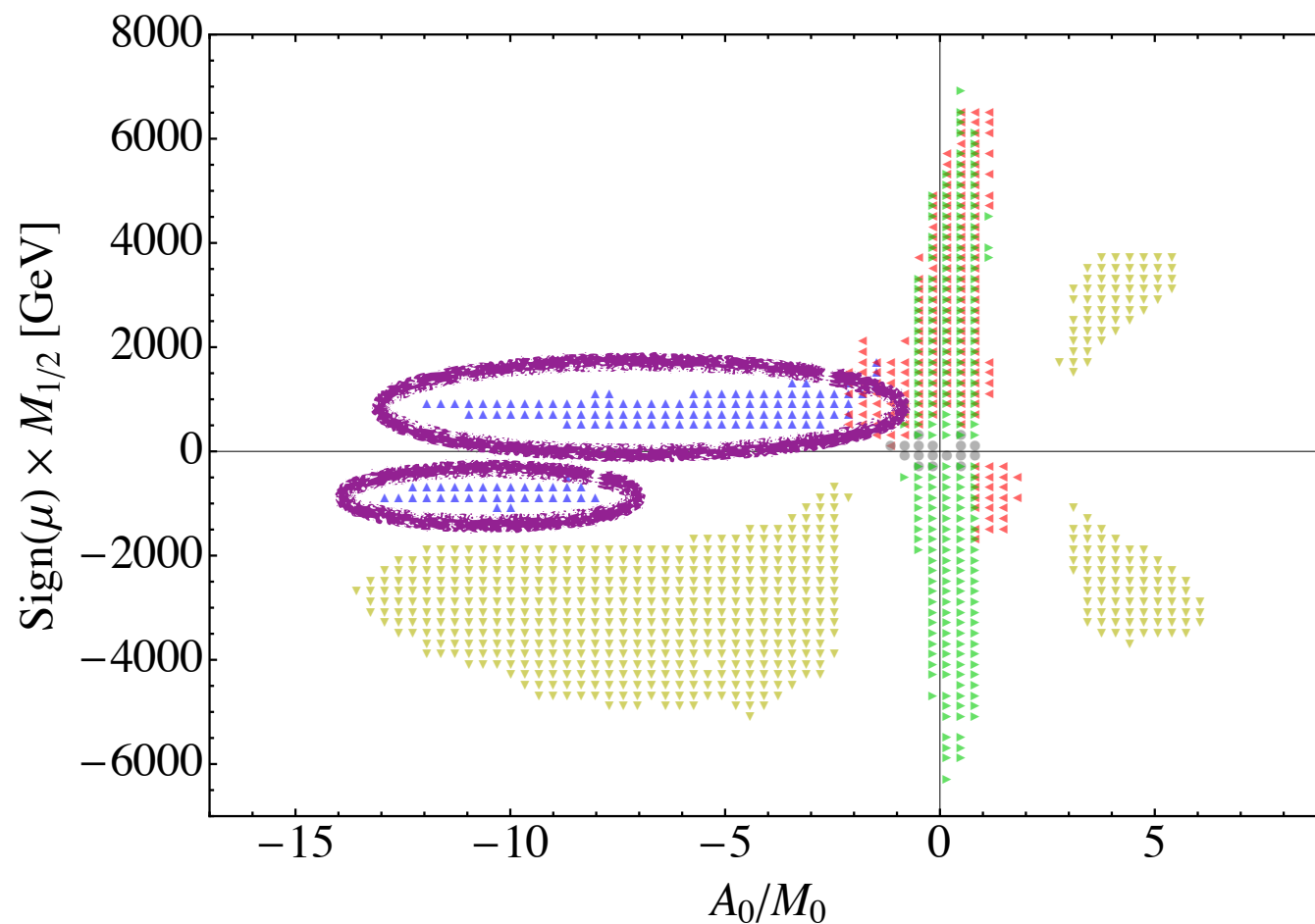
- 1<sup>st</sup> quadrant is similar but 4<sup>th</sup> quadrant extends below  $10^{-14}$  pb .

# CIRCUMNAVIGATING THE CMSSM

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Stau coannihilation

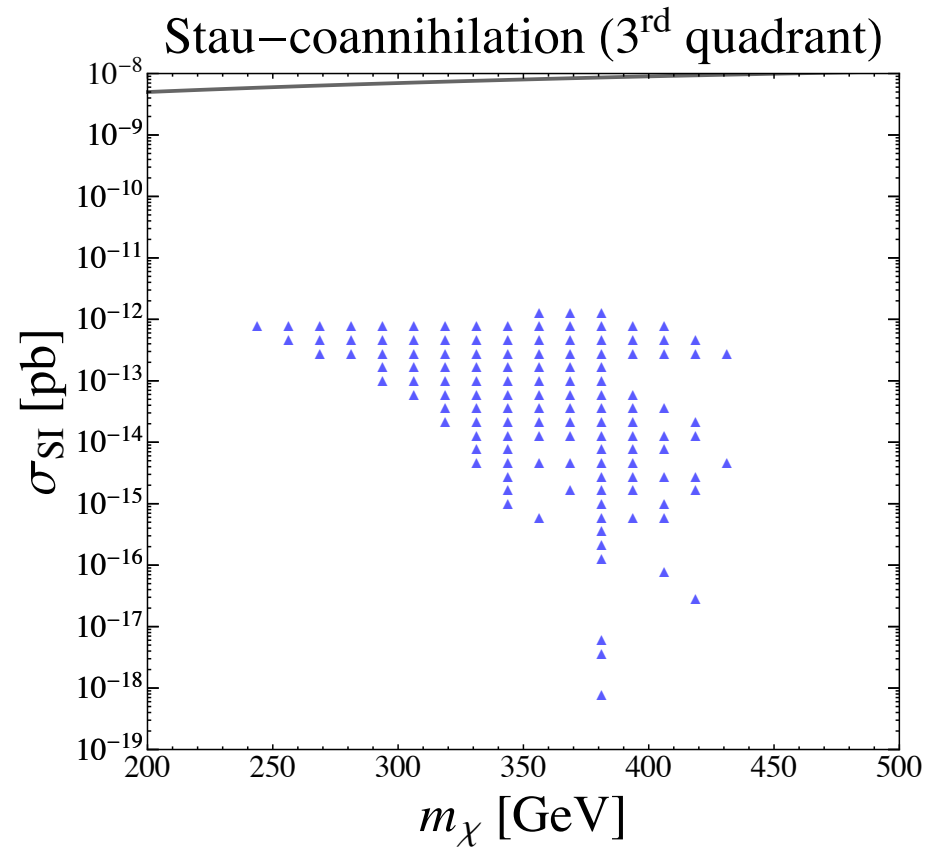
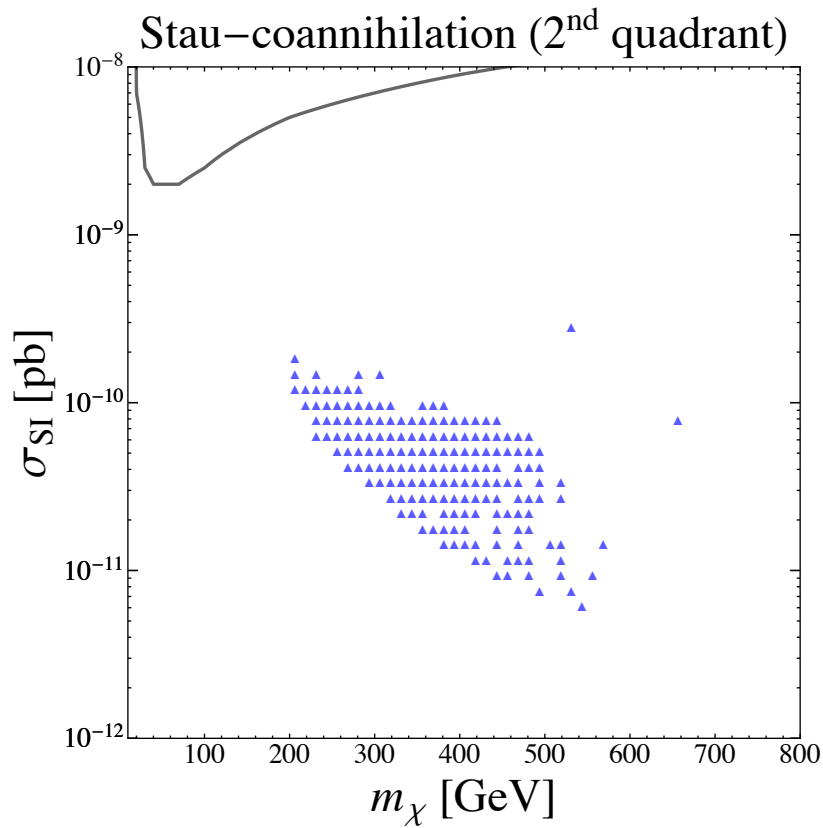
# Setting sail for stau coannihilation



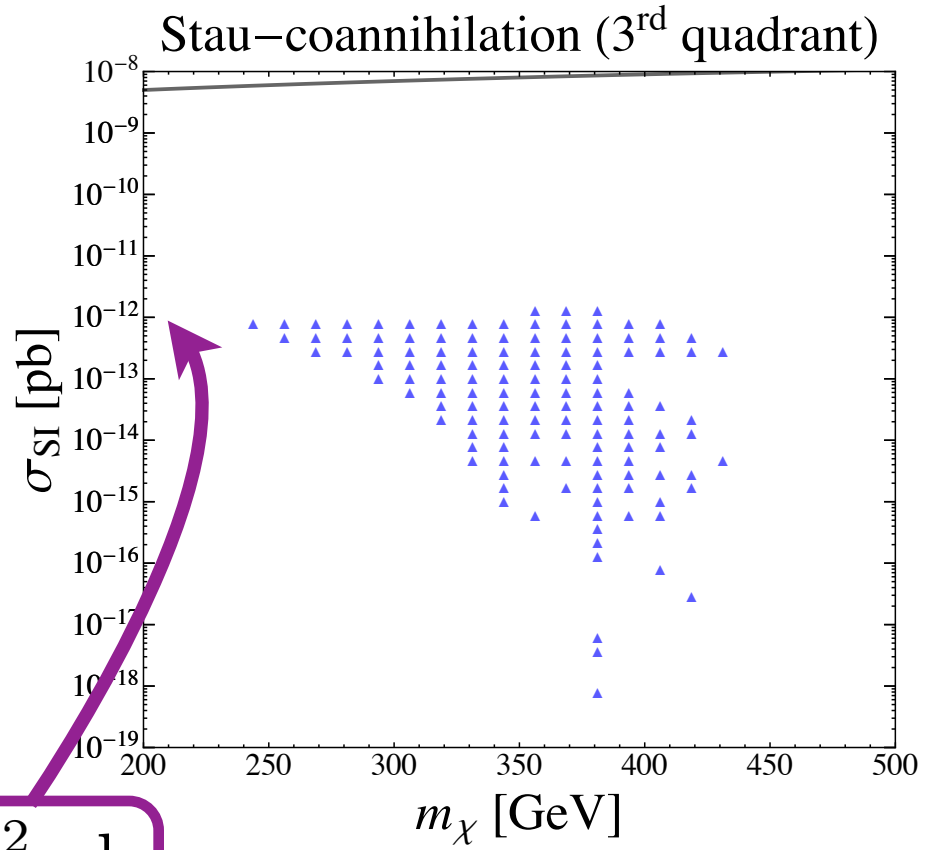
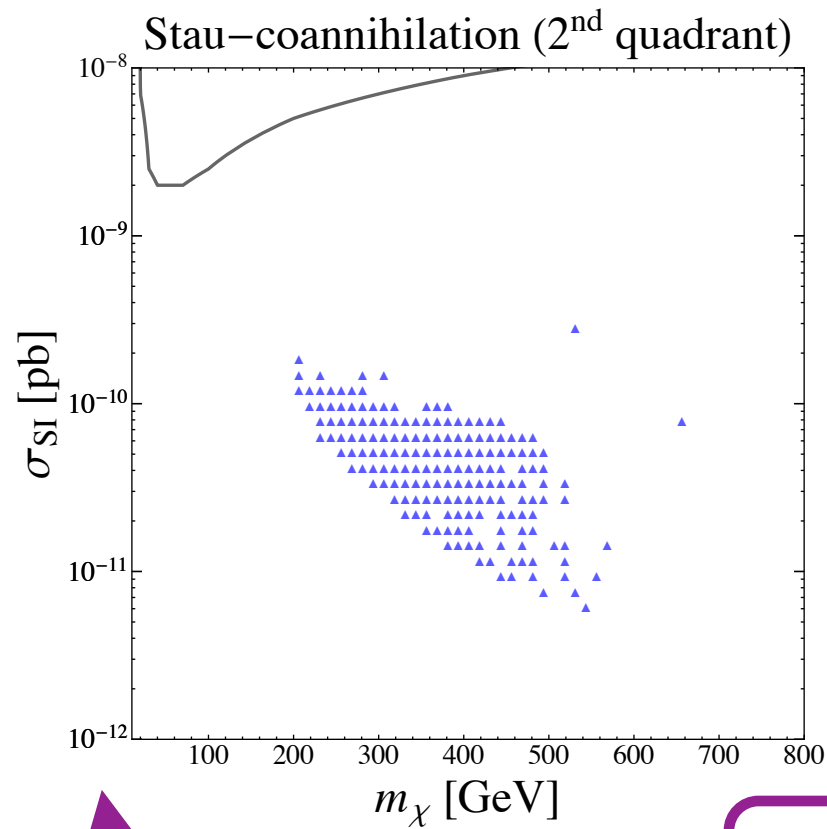
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- $200 \text{ GeV} \lesssim M_0 \lesssim 3 \text{ TeV}$
- $5 \lesssim \tan \beta \lesssim 60$

# Stau-coann: direct detection



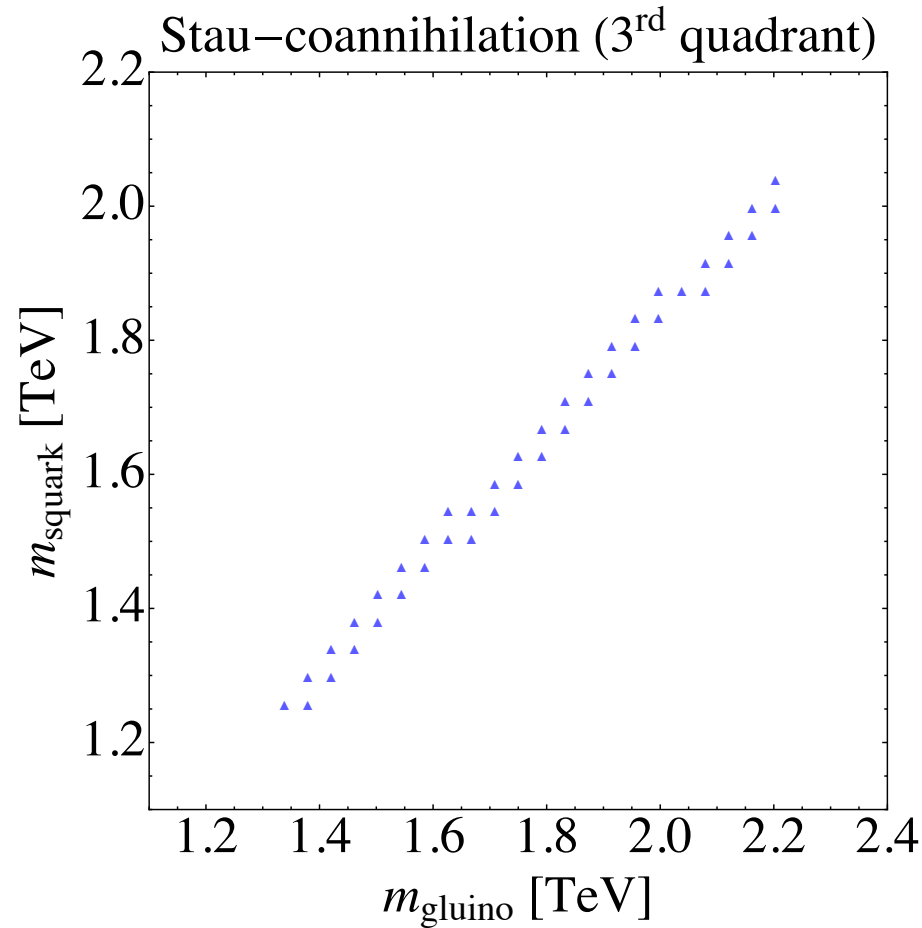
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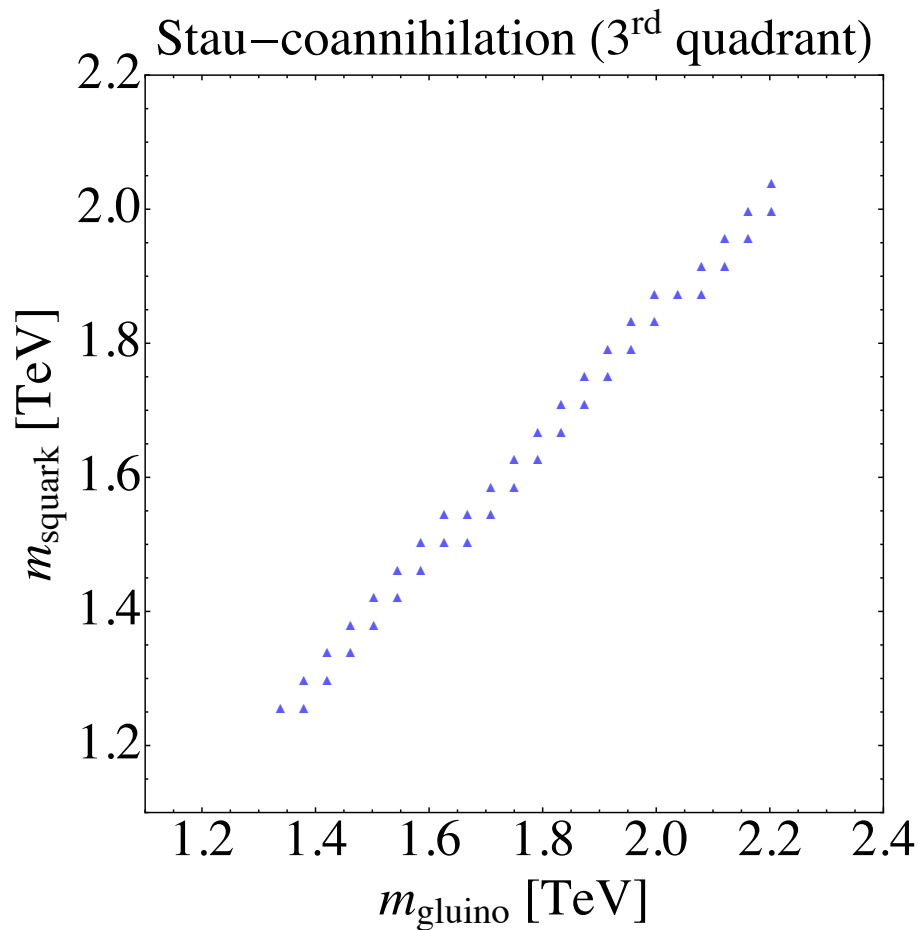
$10^{-12}$  pb

- A 1-ton Xenon experiment can reach spin-independent cross sections of  $5 \times 10^{-12}$  pb at 300 GeV. [Dark matter limit plotter \[http://dmtools.brown.edu/\]](http://dmtools.brown.edu/)
- Direct detection can probe all of the 2<sup>nd</sup> quadrant.

# Stau-coann: squark-gluino plane



# Stau-coann: squark-gluino plane



Are these spectra discoverable at the 14 TeV LHC?



# A stau-coann benchmark (3<sup>rd</sup> quad)

Input parameters						
$M_0$	$M_{1/2}$	$A_0$	$\tan \beta$	$\text{sign}(\mu)$	$ \mu $	$B_\mu$
259.515	900.862	-2296.71	9.23077	-1	-1555.68	$7.574 \times 10^7$

- The LSP is 383.52 GeV; the lighter stau is 383.8 GeV.
  - The stau lifetime is  $O(10^{-2} \text{ s})$ . Probed via long-lived stau searches?

[Citron, Ellis, Luo, Marrouche, Olive, Vries \[arXiv:1212.2886\]](#)

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- The gluino is 1980 GeV.
- The squark masses are

	$\tilde{q}$	$\tilde{b}_1$	$\tilde{b}_2$	$\tilde{t}_1$	$\tilde{t}_2$
$m$ [GeV]	1780.8	1529.9	1715.3	1067.2	1562.9

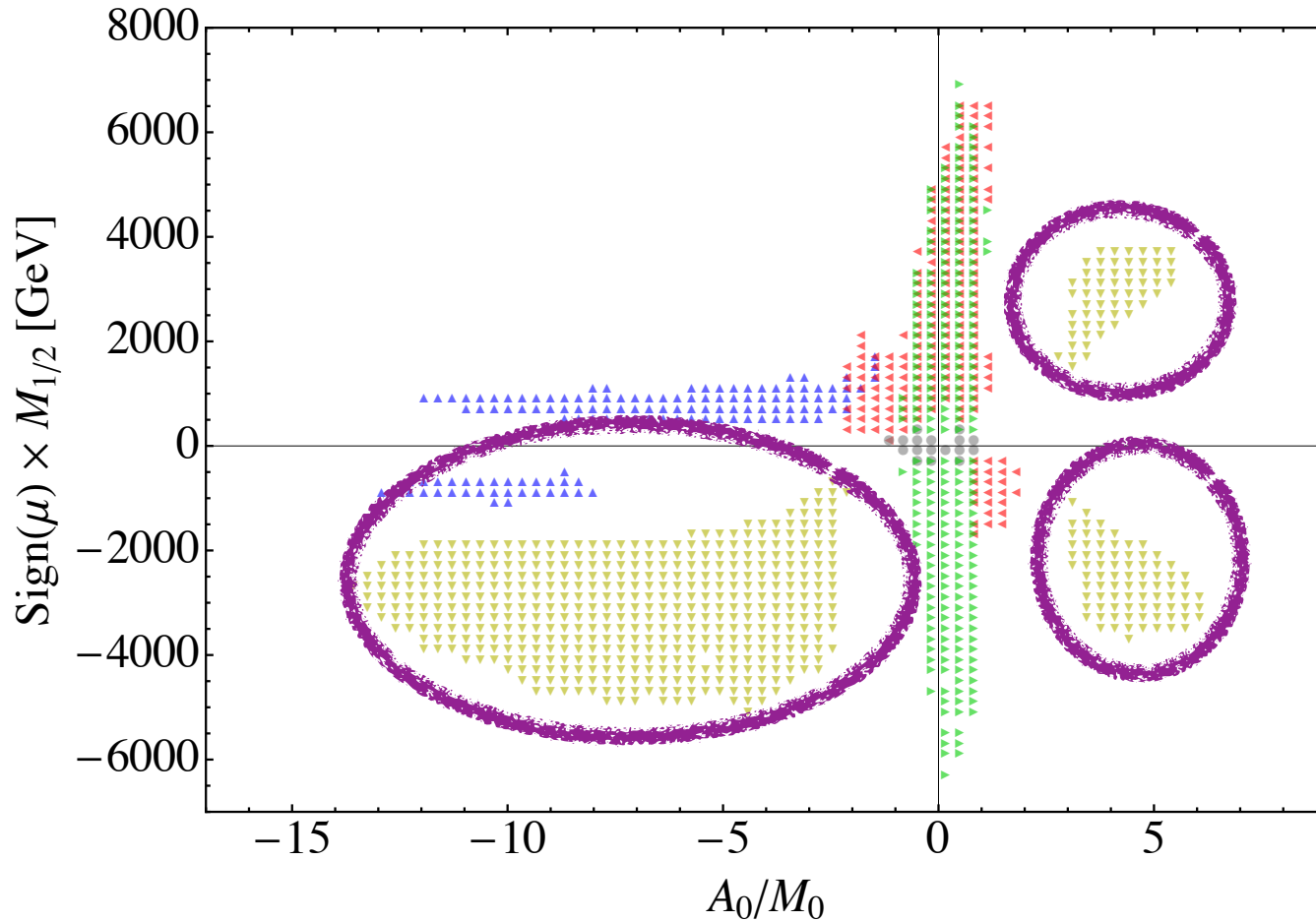
- The gluino branching ratios are
  - $\tilde{g} \rightarrow \tilde{t}_{1,2} + \bar{t}$  [52%]
  - $\tilde{g} \rightarrow \tilde{b}_{1,2} + \bar{b}$  [20%]
  - $\tilde{g} \rightarrow \tilde{q} + \bar{q}$  [28%]
- Probed via gluino pair production?

# CIRCUMNAVIGATING THE CMSSM

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Stop coannihilation

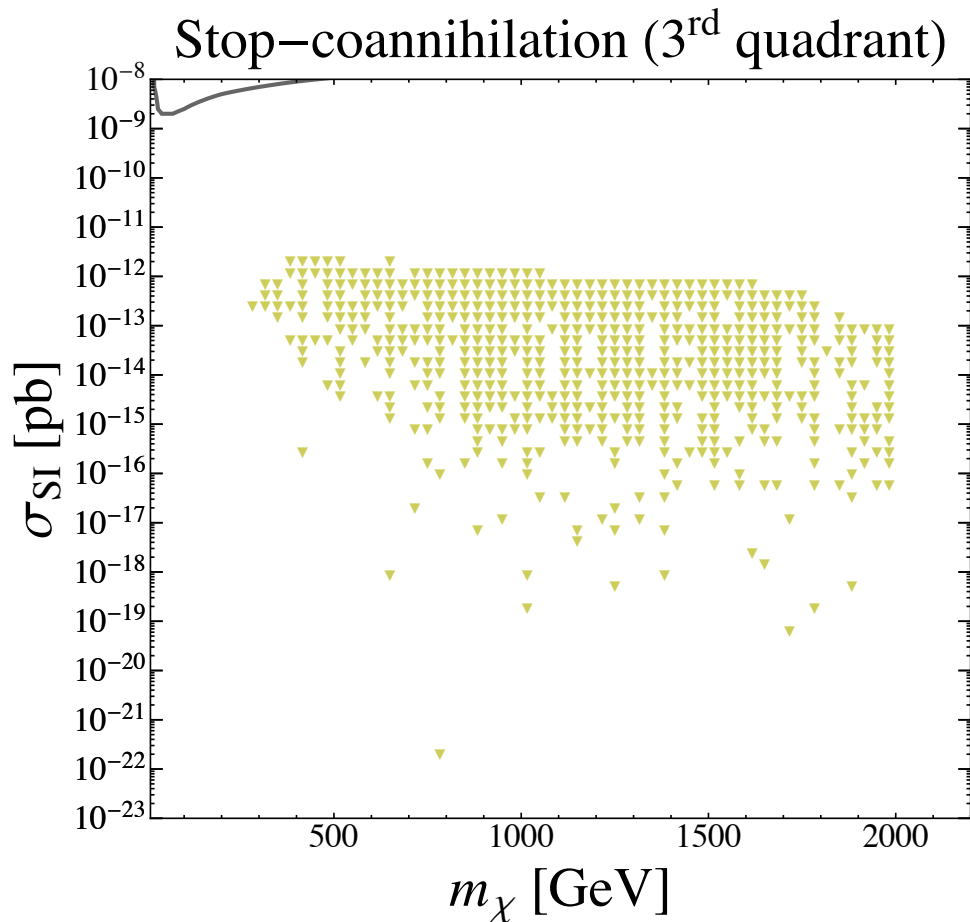
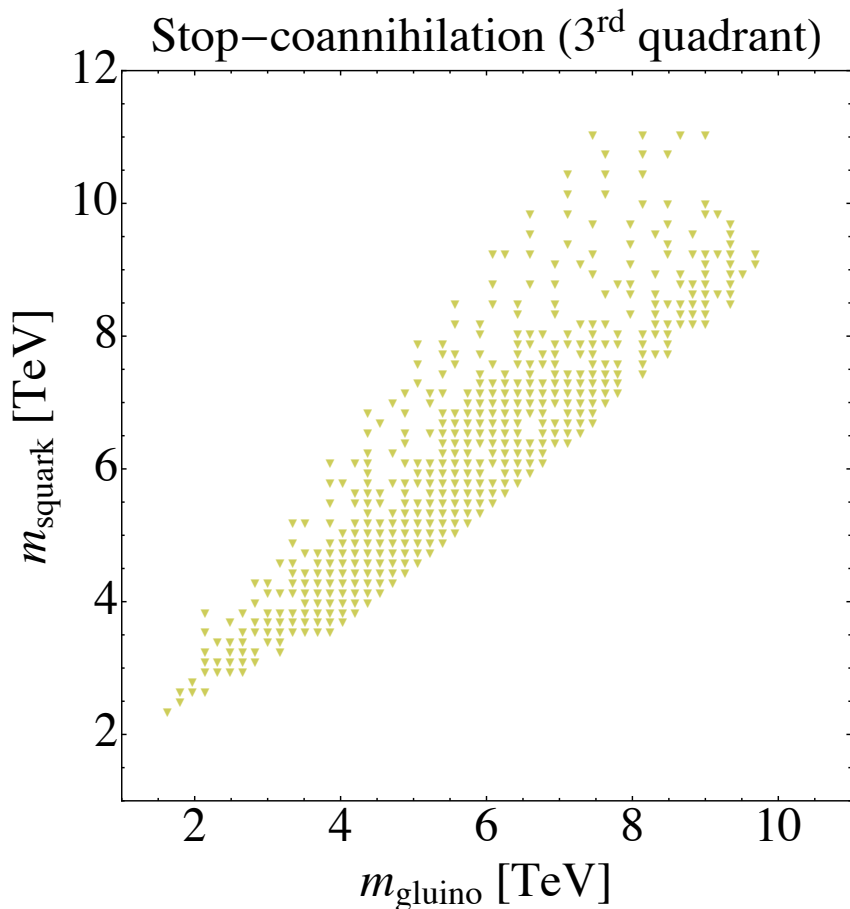
# Setting sail for stop coannihilation



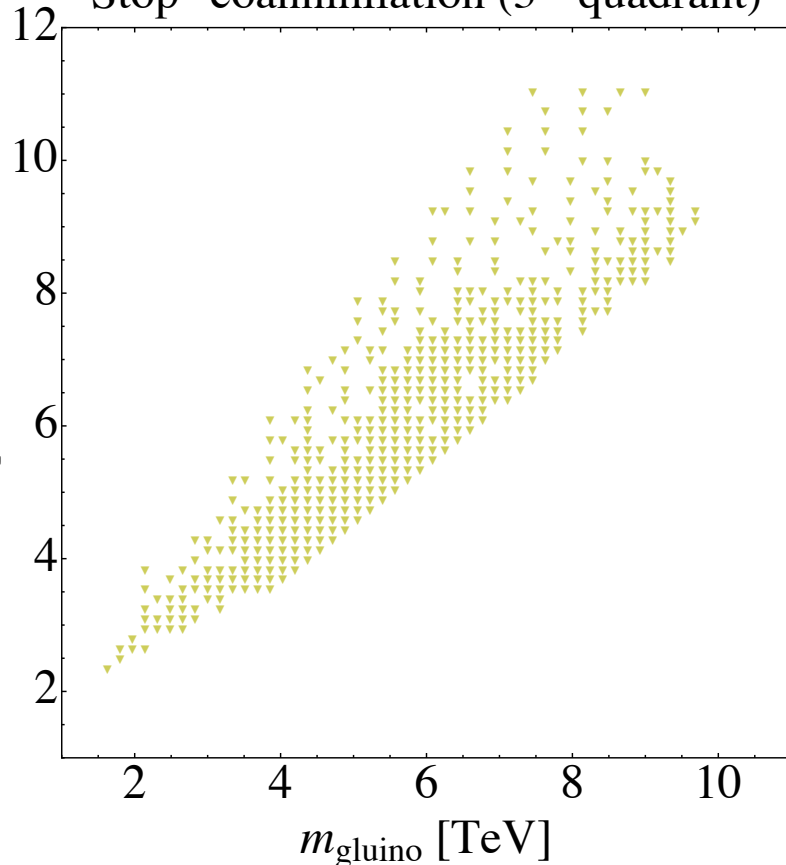
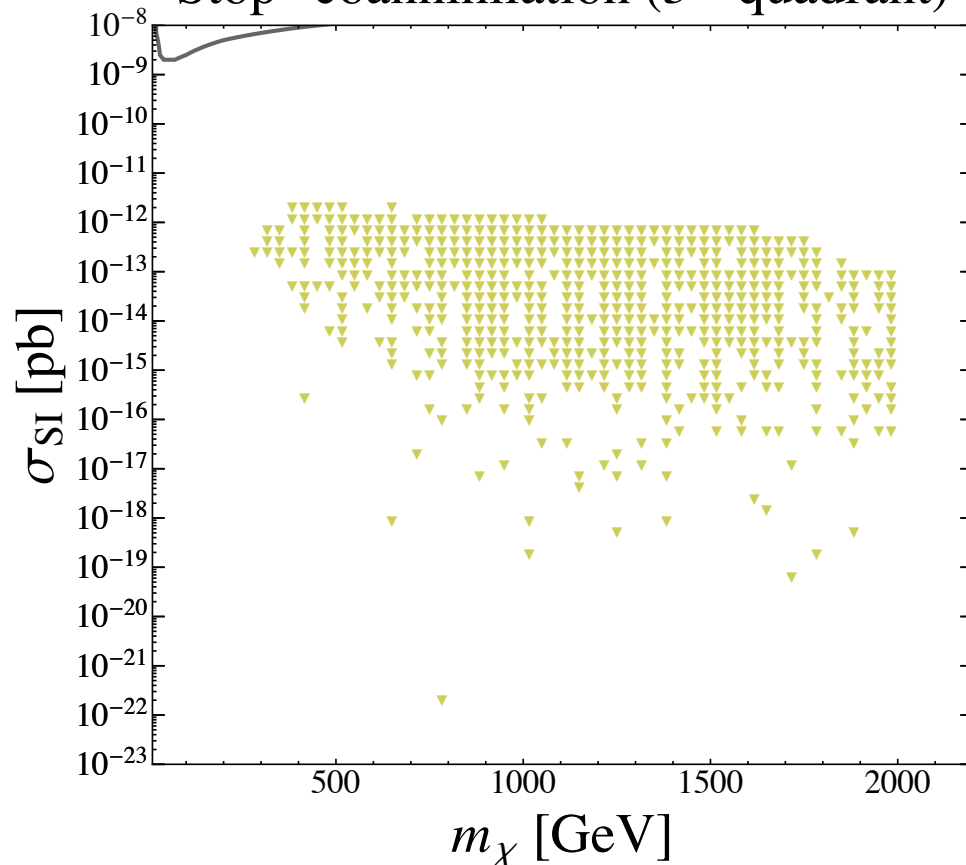
- light  $\tilde{\chi}^0$
- Well-tempered
- $A^0$  pole
- stau coann
- stop coann

- $2 \text{ TeV} \lesssim M_0 \lesssim 12 \text{ TeV}$
- $\tan \beta \lesssim 50$

# Stop-coannihilation phenomenology



# Stop-coannihilation phenomenology

Stop-coannihilation (3<sup>rd</sup> quadrant)Stop-coannihilation (3<sup>rd</sup> quadrant)

A large portion of these spectra will require a machine beyond the 14 TeV LHC.



# ALMOST HOME

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## Conclusions

# Conclusions

- The CMSSM provides a simple ansatz which allows one to explore the phenomenology of the full parameter space.
- We provide a map of the CMSSM which is consistent with a Higgs at 125 GeV and thermal dark matter comprised of neutralinos.
- We demonstrate that the parameter space is compact.
- What regions will remain unconstrained after LHC14 and 1 Ton scale spin-independent direct detection?
  - The 4th quadrant of  $A^0$ -pole annihilation;
  - Large portions of the stop coannihilation regions.
- Note we need LHC results to be presented as generally as possible so it is easy to interpret bound for non-trivial models.