## Appendices

## A Imputing the Change in Baseline Consumption from the LifeCycle Model

Consumption before winning the sweepstakes is imputed from income and an age-appropriate saving rate. Baseline consumption before winning the sweepstakes is then imputed from $B=C-\sum_{i} J_{i}$. Baseline consumption after winning the sweepstakes is imputed by adding the change to baseline consumption implied the life-cycle model:

$$
\Delta B=\hat{B}-B
$$

This appendix lays out how we impute $\Delta B$ from our data. We will use the fact that equations that hold before winning the sweepstakes hold after winning the sweepstakes once hats have been added to the appropriate variables.

If we use $B_{t}$ to designate baseline consumption $t$ years in the future and $B_{0}=B$ to designate baseline consumption now, equation (5) implies that

$$
B_{0}=\lambda_{0}^{\alpha-1} \psi\left(\nu_{0}\right)
$$

and

$$
B_{t}=\lambda_{t}^{\alpha-1} \psi\left(\nu_{t}\right)
$$

As mentioned above, $r=\rho$ and the fair annuity and life insurance markets imply that $\lambda_{t}=\lambda_{0}$. Therefore,

$$
\begin{equation*}
B_{t}=\frac{B_{0} \psi\left(\nu_{t}\right)}{\psi\left(\nu_{0}\right)} \tag{32}
\end{equation*}
$$

The fair annuity and life insurance markets allow one to focus on expected present values. But it is important not to double-count. Therefore we define $\Upsilon$ as non-labor, non-interest income. The lifetime budget constraint looks like

$$
\begin{aligned}
A_{0} & +E_{0} \int_{0}^{\infty} e^{-r t} \Upsilon\left(\nu_{t}\right) d t+\sum_{i} \int_{0}^{R_{i}-a_{i}} e^{-r t} \frac{p_{i}\left(a_{i}+t\right)}{p_{i}\left(a_{i}\right)} W_{i, t} N_{i, t} d t \\
& =E_{0} \int_{0}^{\infty} e^{-r t} C_{t} d t+Q \\
& =E_{0} \int_{0}^{\infty} e^{-r t}\left[B_{t}+\sum_{i} J_{i, t}\right] d t+Q \\
& =\frac{B_{0}}{\psi\left(\nu_{0}\right)} E_{0} \int_{0}^{\infty} e^{-r t} \psi\left(\nu_{t}\right) d t+\sum_{i} \int_{0}^{R_{i}-a_{i}} e^{-r t} \frac{p_{i}\left(a_{i}+t\right)}{p_{i}\left(a_{i}\right)} J_{i, t} d t+Q
\end{aligned}
$$

where $A_{0}$ is the current net worth of the household, $a_{i}$ is the current age of worker $i, R_{i}$ is the retirement age for worker $i$ (for now assumed exogenous), $p_{i}\left(a_{i}+t\right) / p_{i}\left(a_{i}\right)$ is the probability of living to age $a_{i}+t$ conditional on having lived to age $a_{i}, W_{i, t} N_{i, t}$ is labor income for worker $i$ conditional on living to time $t$,
and $Q$ is the expected present value of bequests and other gifts from the household. ${ }^{30}$
Now let us take the "first-difference" of the two extreme ends of equation (33): the after-sweepstakes values of each term minus the original values of each term. The only change to the sum of initial net worth and the expected present value of exogenous non-interest, non-labor income is the expected present value of the sweepstakes winnings. The text of the survey questions states that the sweepstakes pays an amount equal to last year's total family income as long as you [or your partner] live. Given the low rate of inflation during the relevant sample period, we assume that the respondents interpret this to mean that the sweepstakes pays the same real amount every year. Thus, denoting the expected present value of the sweepstakes winning by $\mathcal{L}$ and last year's total family income by $Y$,

$$
\begin{equation*}
\mathcal{L}=Y \int_{0}^{\infty} e^{-r t} \frac{p_{1}\left(a_{1}+t\right)}{p_{1}\left(a_{1}\right)} d t \tag{33}
\end{equation*}
$$

for a single respondent and

$$
\begin{equation*}
\mathcal{L}=Y \int_{0}^{\infty} e^{-r t}\left[\frac{p_{1}\left(a_{1}+t\right)}{p_{1}\left(a_{1}\right)}+\frac{p_{2}\left(a_{2}+t\right)}{p_{2}\left(a_{2}\right)}-\frac{p_{1}\left(a_{1}+t\right)}{p_{1}\left(a_{1}\right)} \frac{p_{2}\left(a_{2}+t\right)}{p_{2}\left(a_{2}\right)}\right] d t \tag{34}
\end{equation*}
$$

for a couple, using the approximation of independence in mortality.
Substituting in $\mathcal{L}$ for the change in $A_{0}+E_{0} \int_{0}^{\infty} \Upsilon\left(\nu_{t}\right) d t$

$$
\begin{aligned}
\mathcal{L} & +\sum_{i} \int_{0}^{R_{i}-a_{i}} e^{-r t} \frac{p_{i}\left(a_{i}+t\right)}{p_{i}\left(a_{i}\right)} W_{i, t}\left[\hat{N}_{i, t}-N_{i, t}\right] d t \\
& =\frac{\left(\hat{B}_{0}-B_{0}\right)}{\psi\left(\nu_{0}\right)} E_{0} \int_{0}^{\infty} e^{-r t} \psi\left(\nu_{t}\right) d t+\sum_{i} \int_{0}^{R_{i}-a_{i}} e^{-r t} \frac{p_{i}\left(a_{i}+t\right)}{p_{i}\left(a_{i}\right)}\left[\hat{J}_{i, t}-J_{i, t}\right] d t+[\hat{Q}-Q] .
\end{aligned}
$$

Solving for $\Delta B=\hat{B}_{0}-B_{0}$ using the notation $\Delta$ more generally for changes from the original situation to the after-sweepstakes situation,

$$
\begin{aligned}
\Delta B & =\frac{\psi\left(\nu_{0}\right)}{E_{0} \int_{0}^{\infty} e^{-r t} \psi\left(\nu_{t}\right) d t} \cdot\left\{\mathcal{L}+\sum_{i} \int_{0}^{R_{i}-a_{i}} e^{-r t} \frac{p_{i}\left(a_{i}+t\right)}{p_{i}\left(a_{i}\right)} W_{i, t}\left[\Delta N_{i, t}\right] d t\right. \\
& \left.-\sum_{i} \int_{0}^{R_{i}-a_{i}} e^{-r t} \frac{p_{i}\left(a_{i}+t\right)}{p_{i}\left(a_{i}\right)} \Delta J_{i, t} d t-\Delta Q\right\}
\end{aligned}
$$

The income effect of the sweepstakes is the impetus for any reduction in labor supply. Thus, for a given change in labor hours reported by the respondents, the larger is $\Delta B$, the smaller the estimate of the labor supply elasticity. This is important to keep in mind as we make the necessary assumptions to operationalize equation (35). For instance, we begin by assuming that $\Delta Q=0$ - no change in bequests. This biases the estimate of the labor supply elasticity downwards as compared to the likely increase in bequests as a result of winning the sweepstakes. The assumption of constant real sweepstakes payments also biases the labor supply elasticity downward if the respondent's interpretation of the survey question is constant nominal payments. The other rough and ready assumptions we make in order to operationalize (35) are $\Delta R_{i}=0$ and the simplifying pair of assumptions

[^0]$$
W_{i, t} \Delta N_{i, t}=W_{i, 0} \Delta N_{i, 0}=W_{i}\left[\hat{N}_{i}-N_{i}\right]
$$
and
$$
\Delta J_{i, t}=\Delta J_{i, 0}=\hat{J}_{i}-J_{i}
$$
for the years leading up to retirement. If the household would gradually adjust labor hours downward as retirement neared, the constant elasticity of labor supply assumption implies that $\Delta N$ and the closely linked but smaller value of $\Delta J$ would gradually get smaller instead of staying the same size - up to the point where the fixed costs led to retirement. In itself, this tends to bias the labor supply elasticity estimate upwards. But the earlier retirement due to winning the sweepstakes would result in increased values of $\Delta N$, coupled with smaller increases in $\Delta J$, and so tend to bias the labor supply elasticity estimate downwards. Modeling both of these factors precisely is beyond the scope of this paper, because it requires calibration of the evolution of the aversion to work parameter $M$ with age (the subject of related work, Kimball and Shapiro, 2003), but we believe that the bias from ignoring earlier retirement is larger than the bias from ignoring the smaller absolute reductions in hours as initial hours fall towards retirement. Thus, we defend the simpler calculations we make as reasonable conservative benchmarks, even though they are not precisely accurate.

The only other assumption necessary is a functional form for $\psi\left(\nu_{t}\right)$, the household equivalence scale at time $t$. Our households have only one or two adults. ${ }^{31}$ For single-person households, we normalize $\psi\left(\nu_{t}\right)=1$. For dual-person households, we set $\psi\left(\nu_{t}\right)=2^{0.7}$ based on the evidence on scale-economies in household consumption reviewed by Citro and Michael (1995, p. 176).

## B Relationships Among Local Labor Supply Elasticities

This appendix gives a very brief background for the equations for various elasticities in terms of the Frisch labor supply elasticity in the context of the functional form used in this paper. ${ }^{32}$ We will derive these equations for the dual-earner case. The single earner case is easy to obtain by setting one of the wages to zero.

One key equation for determining elasticities is (13):

$$
N_{i}^{*}=v^{\prime-1}\left(\frac{\lambda^{1-\alpha} W_{i}}{M_{i}}\right)
$$

Inverted, (13) implies

$$
\begin{equation*}
v^{\prime}\left(N_{i}\right)=\frac{\lambda^{\alpha-1} W_{i}}{M_{i}} \tag{35}
\end{equation*}
$$

Totally log-differentiated, (13) implies

$$
\begin{equation*}
d \ln \left(N_{i}\right)=\eta_{i}^{\lambda}\left[d \ln W_{i}+(1-\alpha) d \ln \lambda\right] \tag{36}
\end{equation*}
$$

where $d \ln M_{i}=0$ and

[^1]$$
\eta_{i}^{\lambda}=\frac{v^{\prime}\left(N_{i}\right)}{N_{i} v^{\prime \prime}\left(N_{i}\right)}
$$

Note that setting $d \ln \lambda=0$ yields

$$
d \ln \left(N_{i}\right)=\eta_{i}^{\lambda} d \ln W_{i}
$$

Also, combining equations (4), (10) and (16),

$$
\begin{equation*}
C=\lambda^{\alpha-1}\left\{\psi(\nu)+\alpha \sum_{j}\left[v\left(N_{j}\right)-v\left(N^{\#}\right)+N^{\#} v^{\prime}\left(N^{\#}\right)\right]\right\} \tag{37}
\end{equation*}
$$

Totally differentiating (37) and using (35) yields

$$
\begin{equation*}
d \ln C=-(1-\alpha) d \ln \lambda+\alpha \lambda^{\alpha-1} \sum_{j} \frac{M_{j} v^{\prime}\left(N_{j}\right)}{C} d N_{j}=-(1-\alpha) d \ln \lambda+\alpha \sum_{j} \frac{W_{i} N_{i}}{C} d \ln N_{i} \tag{38}
\end{equation*}
$$

Treating $W_{1}, W_{2}$ and the initial level of $C, N_{1}$ and $N_{2}$ as data, and $\alpha, \eta_{1}^{\lambda}$ and $\eta_{2}^{\lambda}$ as known parameters, the objective is to calculate the size of $d \ln N_{i}$ in response to particular changes in $d \ln W_{1}, d \ln W_{2}$ and $d \ln \lambda$. Equations (36) and (38) are used in calculating every elasticity below.

To find $\ell_{i}$, set $d \ln W_{1}=d \ln W_{2}=0$ in (36) and calculate

$$
\begin{equation*}
\ell_{i}=\frac{-W_{i} d N_{i}}{d C-\sum_{j} W_{j} d N_{j}}=\eta_{i}^{\lambda}\left(\frac{W_{i} N_{i}}{C+(1-\alpha) \sum_{j} \eta_{j}^{\lambda} W_{j} N_{j}}\right) \tag{39}
\end{equation*}
$$

In finding both $\eta^{U}$ and $\eta^{C}$, we set $d \ln W_{1}=d \ln W_{2}=d \ln W$. This equal proportional change in both wages gives an elasticity concept appropriate for thinking about the macroeconomic labor supply elasticity. The Technical Appendix C discusses other elasticity concepts. For $\eta_{i}^{U}$, the additional equation is

$$
\begin{equation*}
d C=W_{1} d N_{1}+W_{2} d N_{2} \tag{40}
\end{equation*}
$$

In words, (40) says that the household moves along an indifference surface. For $\eta_{i}^{C}$, the additional equation is

$$
d C=0
$$

In both cases, straightforward but tedious algebra yields the expressions for $\eta_{i}^{U}$ and $\eta_{i}^{C}$ given above in the main text.

Finally, to find $\eta_{11}^{\mathrm{X}}$, set $d \ln W_{2}=0$ and use the additional equation

$$
d C=d\left(W_{1} N_{1}+W_{2} N_{2}\right)=N_{1} d W_{1}+W_{1} d N_{1}+W_{2} d N_{2}
$$

Again, straightforward but tedious algebra yields the expression given in the text for $\eta_{11}^{X}$.

## C Technical Appendix: General Relationships Among Local Labor Supply Elasticities

This appendix serves two purposes. First, it examines what happens if the assumption of scale symmetry in consumption holds only approximately. The empirical literature often finds non-zero $\eta^{X}$ or long-run elasticities, but since these estimates are generally close to zero, it is important to show what happens when our restriction holds approximately. Second, it uses this more general assumption to derive the expressions among the local labor elasticities discussed in brief in the paper.

At an interior solution to the household's problem, it is convenient to use the Frisch dual problem to study relationships among local labor supply elasticities. Defining

$$
\mu=\frac{1}{\lambda}
$$

let

$$
\Phi\left(\mu, W_{1}, W_{2}\right)=\max _{C, N_{1}, N_{2}} \mu U\left(C, N_{1}, N_{2}\right)+W_{1} N_{1}+W_{2} N_{2}-C
$$

(The single and single earner cases can be seen as special cases of this dual earner case in which the share of labor income for one household member is zero.) By the envelope theorem,

$$
\begin{aligned}
\frac{\partial \Phi}{\partial \mu} & =U\left(\mu, W_{1}, W_{2}\right) \\
\frac{\partial \Phi}{\partial W_{i}} & =N_{i}\left(\mu, W_{1}, W_{2}\right)
\end{aligned}
$$

Define "net expenditure" $X$ by

$$
X=C-W_{1} N_{1}-W_{2} N_{2}
$$

Then

$$
C\left(\mu, W_{1}, W_{2}\right)=\mu \frac{\partial \Phi}{\partial \mu}+W_{1} \frac{\partial \Phi}{\partial W_{1}}+W_{2} \frac{\partial \Phi}{\partial W_{2}}-\Phi
$$

and

$$
X\left(\mu, W_{1}, W_{2}\right)=\mu \frac{\partial \Phi}{\partial \mu}-\Phi
$$

We will begin by expressing elasticities in terms of the labor income ratios

$$
h_{i}=\frac{W_{i} N_{i}}{C}
$$

and the standardized second derivatives of $\Phi$ defined by

$$
\phi_{\mu \mu}=\frac{\mu^{2}}{C} \frac{\partial^{2} \Phi}{\partial^{2} \mu}
$$

$$
\begin{gathered}
\phi_{\mu i}=\phi_{i \mu}=\frac{\mu W_{i}}{C} \frac{\partial^{2} \Phi}{\partial \mu \partial W_{i}} \\
\phi_{i j}=\frac{W_{i} W_{j}}{C} \frac{\partial^{2} \Phi}{\partial W_{i} \partial W_{j}} .
\end{gathered}
$$

With $X$ as one alternative out of $X, \lambda, C, U$ A general notation for the wage elasticities we are interested in is

$$
\begin{gathered}
\eta_{i j}^{X}=\left.\frac{\partial \ln N_{i}}{\partial \ln W_{j}}\right|_{X=\text { constant, } W_{k}=\text { constant for } k \neq j}, \\
\eta_{i}^{X}=\eta_{i 1}^{X}+\eta_{i 2}^{X}=\left.\frac{\partial \ln N_{i}}{\partial \ln W}\right|_{X=\text { constant, } W_{2} / W_{1}=\text { constant }} . \\
\eta^{X}=\frac{h_{1} \eta_{1}^{X}+h_{2} \eta_{2}^{X}}{h_{1}+h_{2}} .
\end{gathered}
$$

Thus, $\eta_{i}^{X}$ is an elasticity with respect to a proportional increase in both wages, while $\eta^{X}$ is a labor income weighted average of the individual $\eta_{i}^{X}$ elasticities.

These definitions and the fact that $\mu=$ constant is the same thing as $\lambda=$ constant allow one to lay out the following:

$$
\begin{equation*}
\frac{\partial \ln N_{i}\left(\mu, W_{1}, W_{2}\right)}{\partial \ln \mu}=\frac{\phi_{\mu i}}{h_{i}} \tag{41}
\end{equation*}
$$

$$
\begin{gather*}
\frac{\partial \ln N_{i}\left(\mu, W_{1}, W_{2}\right)}{\partial \ln W_{j}}=\eta_{i j}^{\lambda}=\frac{\phi_{i j}}{h_{i}}  \tag{42}\\
\eta_{i}^{\lambda}=\frac{\phi_{i 1}+\phi_{i 2}}{h_{i}}  \tag{43}\\
\eta^{\lambda}=\frac{\phi_{11}+2 \phi_{12}+\phi_{22}}{h_{1}+h_{2}} \tag{44}
\end{gather*}
$$

$$
\begin{equation*}
\frac{\partial \ln C\left(\mu, W_{1}, W_{2}\right)}{\partial \ln \mu}=\phi_{\mu \mu}+\phi_{\mu 1}+\phi_{\mu 2} \tag{45}
\end{equation*}
$$

$$
\begin{equation*}
\frac{\partial \ln C\left(\mu, W_{1}, W_{2}\right)}{\partial \ln W_{i}}=\phi_{i \mu}+\phi_{i 1}+\phi_{i 2} \tag{46}
\end{equation*}
$$

$$
\begin{equation*}
\frac{1}{C} \frac{\partial X}{\partial \ln \mu}=\phi_{\mu \mu} \tag{47}
\end{equation*}
$$

$$
\begin{equation*}
\frac{1}{C} \frac{\partial X}{\partial \ln W_{i}}=\phi_{\mu i}-h_{i} . \tag{48}
\end{equation*}
$$

$$
\begin{equation*}
\frac{\mu}{C} \frac{\partial U}{\partial \ln \mu}=\phi_{\mu \mu} \tag{49}
\end{equation*}
$$

$$
\begin{equation*}
\frac{\mu}{C} \frac{\partial U}{\partial \ln W_{i}}=\phi_{\mu i} . \tag{50}
\end{equation*}
$$

The absolute values of the local marginal propensities to earn are given by the fraction of extra net expenditure devoted to reduced work hours when $\mu$ varies, holding $W_{1}$ and $W_{2}$ constant:

$$
\begin{equation*}
\ell_{i}=\frac{-W_{i} \frac{\partial N_{i}}{\partial \ln \mu}}{\frac{\partial X}{\partial \ln \mu}}=\frac{-h_{i} \frac{\partial \ln N_{i}}{\partial \ln \mu}}{\frac{1}{C} \frac{\partial X}{\partial \ln \mu}}=-\frac{\phi_{\mu i}}{\phi_{\mu \mu}} . \tag{51}
\end{equation*}
$$

The marginal propensity to consume out of an increase in net expenditure $X$ is

$$
\begin{equation*}
1-\ell_{1}-\ell_{2}=\frac{\phi_{\mu \mu}+\phi_{\mu 1}+\phi_{\mu 2}}{\phi_{\mu \mu}}=\frac{\frac{\partial \ln C}{\partial \mu}}{\frac{1}{C} \frac{\partial X}{\partial \ln \mu}}=\left.\frac{\partial C}{\partial X}\right|_{W_{1}, W_{2}=\text { constant }} \tag{52}
\end{equation*}
$$

Given the nature of our evidence, which is first and foremost about income effects, it is reasonable to think of the marginal propensities to earn $\ell_{1}$ and $\ell_{2}$ as the most robustly identified of all the local elasticities if the functional form is loosened up. Therefore, we focus on deriving equations that determine other quantities in terms of $\ell_{1}$ and $\ell_{2}$, among other fundamentals. In particular, hereafter we will routinely write $-\ell_{i} \phi_{\mu \mu}$ in place of $\phi_{\mu i}$ :

$$
\begin{equation*}
\phi_{\mu i}=-\ell_{i} \phi_{\mu \mu} \tag{53}
\end{equation*}
$$

Given $h_{1}$ and $h_{2}$, knowing $\ell_{1}$ and $\ell_{2}$ determine two of the six dimensions of the standardized second derivatives $\phi$. We need four more restrictions to pin down the other four dimensions. The degree of departure from scale symmetry in consumption, or alternatively the value of the overall uncompensated labor supply elasticity $\eta^{X}$ will provide one more restriction. Two more restrictions will come from imposing the degree of additive nonseparability between consumption and each of the two types of labor. The last restriction will come from imposing either the value of $\phi_{12}$ or the closely related elasticity of substitution between $N_{1}$ and $N_{2}$. But in the leading case the elasticity of substitution between $N_{1}$ and $N_{2}$ does not affect the elasticities $\eta_{i}$ with respect to proportional increases in both wages.

A convenient way to measure the degree of nonseparability between consumption and the two type of labor by $\alpha_{1}$ and $\alpha_{2}$ in the definition

$$
\begin{equation*}
d \ln C=s d \ln \mu+\alpha_{1} h_{1} d \ln N_{1}+\alpha_{2} h_{2} d \ln N_{2} \tag{54}
\end{equation*}
$$

Literally, the parameter $s$ is the labor-constant elasticity of intertemporal substitution for consumption. Ultimately we will use $\alpha_{1}, \alpha_{2}$ and the degree of departure from scale symmetry in consumption to eliminate $s$ since in our context where the interest rate is constant and always equal to $\rho$ it cannot be functioning as the elasticity of intertemporal substitution for consumption. To relate $\alpha_{i}$ to the standardized second derivatives $\phi$, substitute

$$
\begin{equation*}
d \ln N_{i}=\frac{1}{h_{i}}\left[-\ell_{i} \phi_{\mu \mu} d \ln \mu+\phi_{i 1} d \ln W_{1}+\phi_{i 2} d \ln W_{2}\right] \tag{55}
\end{equation*}
$$

into (54):

$$
\begin{align*}
d \ln C=[s- & \left.\left(\alpha_{1} \ell_{1}+\alpha_{2} \ell_{2}\right) \phi_{\mu \mu}\right] d \ln \mu+\left[\alpha_{1} \phi_{11}+\alpha_{2} \phi_{12}\right] d \ln W_{1} \\
& +\left[\alpha_{1} \phi_{12}+\alpha_{2} \phi_{22}\right] d \ln W_{2} \tag{56}
\end{align*}
$$

Comparing (56) to (45) and (46), it is clear after using (53) and rearranging that

$$
\begin{gather*}
{\left[1-\ell_{1}\left(1-\alpha_{1}\right)-\ell_{2}\left(1-\alpha_{2}\right)\right] \phi_{\mu \mu}=s}  \tag{57}\\
\phi_{\mu \mu}\left[\begin{array}{l}
\ell_{1} \\
\ell_{2}
\end{array}\right]=\left[\begin{array}{ll}
\phi_{11} & \phi_{12} \\
\phi_{12} & \phi_{22}
\end{array}\right]\left[\begin{array}{l}
1-\alpha_{1} \\
1-\alpha_{2}
\end{array}\right] \tag{58}
\end{gather*}
$$

There is a close relationship between the degree of nonseparability between consumption and labor indicated by $\alpha_{1}$ and $\alpha_{2}$ and how closely the utility function comes to scale symmetry in consumption. Define

$$
\theta_{i}=\left.\frac{\partial \ln W_{i}}{\partial \ln C}\right|_{N_{1}, N_{2}=\text { constant }} .
$$

Scale symmetry in consumption implies $\theta_{1}=\theta_{2}=1$. More generally, weak separability between consumption and an aggregate of the two types of labor implies $\theta_{1}=\theta_{2}=\theta$, since weak separability means that a change in $C$ holding $N_{1}$ and $N_{2}$ constant should not change the slope of the indifference curve between $N_{1}$ and $N_{2}$, which is $W_{1} / W_{2}$. From equation (55), one can see that $d \ln N_{1}=d \ln N_{2}=0$ requires

$$
\phi_{\mu \mu}\left[\begin{array}{l}
\ell_{1}  \tag{59}\\
\ell_{2}
\end{array}\right] d \ln \mu=\left[\begin{array}{ll}
\phi_{11} & \phi_{12} \\
\phi_{12} & \phi_{22}
\end{array}\right]\left[\begin{array}{l}
d \ln W_{1} \\
d \ln W_{2}
\end{array}\right]
$$

As long as

$$
\left[\begin{array}{ll}
\phi_{11} & \phi_{12} \\
\phi_{12} & \phi_{22}
\end{array}\right]
$$

is nonsingular (equivalent to the reasonable assumption of a nonzero Frisch labor supply elasticity for any linear combination of $N_{1}$ and $N_{2}$ ), (58) and (59) together imply that

$$
\begin{equation*}
\left.\frac{\partial \ln W_{i}}{\partial \ln \mu}\right|_{N_{1}, N_{2}=\text { constant }}=1-\alpha_{i} \tag{60}
\end{equation*}
$$

Combining (60) with the definition in (54) that

$$
\begin{equation*}
\left.\frac{\partial C}{\partial \ln \mu}\right|_{N_{1}, N_{2}=\text { constant }}=s \tag{61}
\end{equation*}
$$

one can solve for $\theta_{i}$ :

$$
\begin{equation*}
\theta_{i}=\left.\frac{\partial \ln W_{i}}{\partial \ln C}\right|_{N_{1}, N_{2}=\mathrm{constant}}=\frac{1-\alpha_{i}}{s} \tag{62}
\end{equation*}
$$

One consequence of equation (62) is that weak separability between consumption and a labor aggregate implies not only $\theta_{1}=\theta_{2}=\theta$, but also $\alpha_{1}=\alpha_{2}=\alpha$. Another consequence is that $s$ can be eliminated by substituting

$$
\begin{equation*}
s=\frac{1-\alpha_{i}}{\theta_{i}} \tag{63}
\end{equation*}
$$

Also, given (57),

$$
\begin{equation*}
\phi_{\mu \mu}=\frac{1-\alpha_{i}}{\theta_{i}\left[1-\ell_{1}\left(1-\alpha_{1}\right)-\ell_{2}\left(1-\alpha_{2}\right)\right]} \tag{64}
\end{equation*}
$$

The assumption of weak separability between consumption and a labor aggregate (or equivalently between consumption and a leisure aggregate) is attractive. We will focus on that case from here on. With weak separability between consumption and a labor aggregate, equation (64) becomes

$$
\begin{equation*}
\phi_{\mu \mu}=\frac{1-\alpha}{\theta\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]} \tag{65}
\end{equation*}
$$

Also, substituting $\alpha_{1}=\alpha_{2}=\alpha$ into (58),

$$
\begin{equation*}
\phi_{i 1}+\phi_{i 2}=\frac{\ell_{i} \phi_{\mu \mu}}{1-\alpha}=\frac{\ell_{i}}{\theta\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]} \tag{66}
\end{equation*}
$$

One obvious consequence is that

$$
\begin{equation*}
\frac{\phi_{11}+\phi_{12}}{\phi_{12}+\phi_{22}}=\frac{\ell_{1}}{\ell_{2}} \tag{67}
\end{equation*}
$$

Also, by (43),

$$
\begin{equation*}
\eta_{i}^{\lambda}=\frac{\ell_{i} \phi_{\mu \mu}}{h_{i}(1-\alpha)}=\frac{\ell_{i}}{\theta h_{i}\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]}, \tag{68}
\end{equation*}
$$

and by (44),

$$
\begin{equation*}
\eta^{\lambda}=\frac{\left(\ell_{1}+\ell_{2}\right) \phi_{\mu \mu}}{\left(h_{1}+h_{2}\right)(1-\alpha)}=\frac{\ell_{1}+\ell_{2}}{\theta\left(h_{1}+h_{2}\right)\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]} \tag{69}
\end{equation*}
$$

It is useful to relate $\eta_{i}^{\lambda}$ to $\eta^{\lambda}$ by the following implication of (68) and (69):

$$
\begin{equation*}
\eta_{i}^{\lambda}=\frac{\frac{\ell_{i}}{\ell_{1}+\ell_{2}}}{\frac{h_{i}}{h_{1}+h_{2}}} \eta^{\lambda} . \tag{70}
\end{equation*}
$$

Both $\eta_{i}^{\lambda}$ and $\eta^{\lambda}$ are inversely proportional to $\theta$. Therefore, a modest departure from scale symmetry in consumption leads to only a modest modification in the implied value of $\eta_{i}^{\lambda}$ and $\eta^{\lambda}$ as a function of $\ell_{1}, \ell_{2}$ and $\alpha$. For example, if $\theta=1.1$, so that consumption growing 2 percent per year with no trend in labor would imply $W_{i} / C$ up 20 percent (or 22 percent after compounding) over the course of a century, then the implied value of $\eta_{i}^{\lambda}$ would be $\frac{10}{11}$ as large as if strict scale symmetry in consumption held.

By (42) and (43), in terms of the unknown value of $\phi_{12}$,

$$
\eta_{i i}^{\lambda}=\eta_{i}^{\lambda}-\frac{\phi_{12}}{h_{i}}
$$

while

$$
\begin{aligned}
& \eta_{12}^{\lambda}=\frac{\phi_{12}}{h_{1}} \\
& \eta_{21}^{\lambda}=\frac{\phi_{12}}{h_{2}}
\end{aligned}
$$

These are quite useful formulas if $N_{1}$ and $N_{2}$ are Frisch separable, so that $\phi_{12}=0$, as we assume in our primary functional form. If not, to get further, let's relate $\phi_{12}$ to the Frisch elasticity of substitution between $N_{1}$ and $N_{2}$.

Define the Frisch elasticity of substitution between $N_{1}$ and $N_{2}$ by

$$
\begin{equation*}
\sigma_{12}^{\lambda}=\left.\frac{\partial \ln \left(N_{1} / N_{2}\right)}{\partial \ln \left(W_{1} / W_{2}\right)}\right|_{\lambda=\text { constant }, U=\text { constant }} \tag{71}
\end{equation*}
$$

From (49), (50) and (53),

$$
\begin{equation*}
\frac{\mu}{C} d U=\phi_{\mu \mu}\left[d \ln \mu-\ell_{1} d \ln W_{1}-\ell_{2} d \ln W_{2}\right]=0 \tag{72}
\end{equation*}
$$

If $d \ln m u=-d \ln \lambda=0$, this implies

$$
\begin{equation*}
\ell_{1} d \ln W_{1}+\ell_{2} d \ln W_{2}=0 \tag{73}
\end{equation*}
$$

or

$$
\begin{aligned}
& d \ln W_{1}=\frac{\ell_{2}}{\ell_{1}+\ell_{2}} d \ln \left(W_{1} / W_{2}\right) \\
& d \ln W_{2}=\frac{-\ell_{1}}{\ell_{1}+\ell_{2}} d \ln \left(W_{1} / W_{2}\right)
\end{aligned}
$$

Thus (remembering that $d \ln \mu=0$ ),

$$
\begin{align*}
& d \ln N_{1}=\frac{\ell_{2} \phi_{11}-\ell_{1} \phi_{12}}{h_{1}\left(\ell_{1}+\ell_{2}\right)} d \ln \left(W_{1} / W_{2}\right)  \tag{74}\\
& d \ln N_{2}=\frac{\ell_{2} \phi_{12}-\ell_{1} \phi_{22}}{h_{2}\left(\ell_{1}+\ell_{2}\right)} d \ln \left(W_{1} / W_{2}\right) \tag{75}
\end{align*}
$$

Combining (74) and (75),

$$
h_{1} d \ln N_{1}+h_{2} d \ln N_{2}=\frac{\ell_{2}\left(\phi_{11}+\phi_{12}\right)-\ell_{1}\left(\phi_{12}+\phi_{22}\right)}{\ell_{1}+\ell_{2}}
$$

Weak separability between consumption and a labor aggregate implies that

$$
h_{1} d \ln N_{1}+h_{2} d \ln N_{2}=0
$$

That is, $N_{1}$ and $N_{2}$ change in such a say as to stay on the same indifference curve between $N_{1}$ and $N_{2}$. Because the labor aggregate remains unchanged, consumption $C$ must also remain unchanged to keep $\lambda$ fixed.

Subtracting (75) from (74) and dividing through by $d \ln \left(W_{1} / W_{2}\right)$ yields after simplification using (68),

$$
\begin{equation*}
\sigma_{12}^{\lambda}=\frac{\ell_{2} \eta_{1}^{\lambda}+\ell_{1} \eta_{2}^{\lambda}}{\ell_{1}+\ell_{2}}-\frac{\left(h_{1}+h_{2}\right) \phi_{12}}{h_{1} h_{2}} \tag{76}
\end{equation*}
$$

Thus, $\phi_{12}$ is given by

$$
\begin{equation*}
\phi_{12}=\frac{h_{1} h_{2}}{h_{1}+h_{2}}\left\{\frac{\ell_{2} \eta_{1}^{\lambda}+\ell_{1} \eta_{2}^{\lambda}}{\ell_{1}+\ell_{2}}-\sigma_{12}^{\lambda}\right\} \tag{77}
\end{equation*}
$$

Thus, $\phi_{12}$ differs from zero when the elasticity of substitution between $N_{1}$ and $N_{2}$ differs from a weighted average of the Frisch labor supply elasticities of $N_{1}$ and $N_{2}$. The lower the elasticity of substitution between $N_{1}$ and $N_{2}$, the more Frisch complementarity there is between $N_{1}$ and $N_{2}$.

Let us examine uncompensated labor supply elasticity $\eta^{X}$ next, since the size of $\eta^{X}$ is an alternative way of measuring the degree of departure from strict scale symmetry in consumption. Equations (47) and
(48), together with (53) imply that

$$
\frac{d X}{C}=\phi_{\mu \mu} d \ln \mu-\left[\ell_{1} \phi_{\mu \mu}+h_{1}\right] d \ln W_{1}-\left[\ell_{2} \phi_{\mu \mu}+h_{2}\right] d \ln W_{2}
$$

Therefore, $d X=0$ implies

$$
d \ln \mu=\left(\frac{h_{1}}{\phi_{\mu \mu}}+\ell_{1}\right) d \ln W_{1}+\left(\frac{h_{2}}{\phi_{\mu \mu}}+\ell_{2}\right) d \ln W_{2}
$$

and by (55),

$$
\begin{equation*}
\eta_{i j}^{X}=\frac{1}{h_{i}}\left[\phi_{i j}-\ell_{i} \phi_{\mu \mu}\left(\frac{h_{j}}{\phi_{\mu \mu}}+\ell_{j}\right)\right]=\eta_{i j}^{\lambda}-\frac{\ell_{i} \ell_{j} \phi_{\mu \mu}}{h_{i}}-\frac{\ell_{i} h_{j}}{h_{i}} \tag{78}
\end{equation*}
$$

Adding up,

$$
\begin{equation*}
\eta_{i}^{X}=\eta_{i}^{\lambda}-\frac{\ell_{i}}{h_{i}}\left[\left(\ell_{1}+\ell_{2}\right) \phi_{\mu \mu}+\frac{\ell_{i}\left(h_{1}+h_{2}\right)}{h_{i}}\right] \tag{79}
\end{equation*}
$$

and averaging with labor income weights,

$$
\begin{equation*}
\eta^{X}=\eta^{\lambda}-\frac{\left(\ell_{1}+\ell_{2}\right)^{2}}{h_{1}+h_{2}} \phi_{\mu \mu}-\left(\ell_{1}+\ell_{2}\right) \tag{80}
\end{equation*}
$$

Note that using (70), we obtain a similar relationship:

$$
\begin{equation*}
\eta_{i}^{X}=\frac{\frac{\ell_{i}}{\ell_{1}+\ell_{2}}}{\frac{h_{i}}{h_{1}+h_{2}}} \eta^{X} \tag{81}
\end{equation*}
$$

The similarity to (70) is a consequence of the structure imposed by weak separability between consumption and a labor aggregate.

Adding $\ell_{1}+\ell_{2}$ to both sides of (80) and substituting in the expression for $\eta^{\lambda}$ in (69),

$$
\begin{equation*}
\eta^{X}+\ell_{1}+\ell_{2}=\phi_{\mu \mu}\left(\frac{\left(\ell_{1}+\ell_{2}\right)\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]}{\left(h_{1}+h_{2}\right)(1-\alpha)}\right) \tag{82}
\end{equation*}
$$

Equations (82) and (65) imply

$$
\begin{align*}
\phi_{\mu \mu} & =\left(\eta^{X}+\ell_{1}+\ell_{2}\right) \frac{\left(h_{1}+h_{2}\right)(1-\alpha)}{\left(\ell_{1}+\ell_{2}\right)\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]} \\
& =\frac{1-\alpha}{\theta\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]} \tag{83}
\end{align*}
$$

Thus,

$$
\begin{equation*}
\theta=\frac{\ell_{1}+\ell_{2}}{\left(h_{1}+h_{2}\right)\left(\eta^{X}+\ell_{1}+\ell_{2}\right)} \tag{84}
\end{equation*}
$$

and

$$
\begin{equation*}
\eta^{X}=\left(\ell_{1}+\ell_{2}\right)\left[\frac{1}{\theta\left(h_{1}+h_{2}\right)}-1\right] \tag{85}
\end{equation*}
$$

Since $\eta^{X}$ is more easily observed than $\theta$, it is good to have an expressions for $\eta^{\lambda}$ in terms of $\eta^{X}$ instead of $\theta$. Substituting in from (84), (68) and (69) become

$$
\begin{gather*}
\eta_{i}^{\lambda}=\frac{\ell_{i}\left(h_{1}+h_{2}\right)\left(\eta^{X}+\ell_{1}+\ell_{2}\right.}{\left(\ell_{1}+\ell_{2}\right) h_{i}\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]},  \tag{86}\\
\eta^{\lambda}=\frac{\eta^{X}+\ell_{1}+\ell_{2}}{\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]} . \tag{87}
\end{gather*}
$$

This implies that as long as $\ell_{1}+\ell_{2}$ is substantial compared to the size of $\eta^{X}$, the difference between $\eta^{X}$ and zero does not change the overall picture of the size of the elasticity $\eta^{\lambda}$.

In addition to using $\eta^{X}$ to gauge the size of $\theta$, it is possible to use either cross-elasticity $\eta_{12}^{X}$ or $\eta_{21}^{X}$ to gauge $\phi_{12}$. Substitute in from (83) for $\phi_{\mu \mu}$ into (78) and rearrange to get

$$
\begin{align*}
\phi_{12} & =h_{1} \eta_{12}^{X}+h_{2} \ell_{1}+\ell_{1} \ell_{2}\left(\eta^{X}+\ell_{1}+\ell_{2}\right) \frac{\left(h_{1}+h_{2}\right)(1-\alpha)}{\left(\ell_{1}+\ell_{2}\right)\left[1-\alpha\left(\ell_{1}+\ell_{2}\right)\right]} \\
& =h_{2} \eta_{21}^{X}+h_{1} \ell_{2}+\ell_{1} \ell_{2}\left(\eta^{X}+\ell_{1}+\ell_{2}\right) \frac{\left(h_{1}+h_{2}\right)(1-\alpha)}{\left(\ell_{1}+\ell_{2}\right)\left[1-\alpha\left(\ell_{1}+\ell_{2}\right)\right]} \tag{88}
\end{align*}
$$

The two versions of the formula reflect the Slutsky symmetry condition.
To complete the set of elasticities, formulas for $\eta^{C}$ and $\eta^{U}$ are in order. By (45), (46) and (53),

$$
\begin{equation*}
d \ln C=\left(1-\ell_{1}-\ell_{2}\right) \phi_{\mu \mu} d \ln \mu+\left[\phi_{11}+\phi_{12}-\ell_{1} \phi_{\mu \mu}\right] d \ln W_{1}+\left[\phi_{12}+\phi_{22}-\ell_{2} \phi_{\mu \mu}\right] d \ln W_{2} . \tag{89}
\end{equation*}
$$

Thus, $d \ln C=0$ implies

$$
d \ln \mu=\frac{1}{\left[1-\ell_{1}-\ell_{2}\right] \phi_{\mu \mu}}\left[\left(\ell_{1} \phi_{\mu \mu}-\phi_{11}-\phi_{12}\right) d \ln W_{1}+\left(\ell_{2} \phi_{\mu \mu}-\phi_{12}-\phi_{22}\right) d \ln W_{1}\right]
$$

Then

$$
\begin{align*}
\eta_{i j}^{C} & =\frac{1}{h_{i}}\left\{\phi_{i j}-\frac{\ell_{i} \phi_{\mu \mu}}{\left(1-\ell_{1}-\ell_{2}\right) \phi_{\mu \mu}}\left[\ell_{j} \phi_{\mu \mu}-\phi_{j 1}-\phi_{j 2}\right]\right\} \\
& =\eta_{i j}^{\lambda}+\frac{\ell_{i}}{h_{i}\left(1-\ell_{1}-\ell_{2}\right)}\left\{h_{j} \eta_{j}^{\lambda}-\ell_{j} \phi_{\mu \mu}\right\} \tag{90}
\end{align*}
$$

Adding over $j$, and using (69), (70) and (83),

$$
\begin{align*}
\eta_{i}^{C} & =\frac{\ell_{i} \phi_{\mu \mu}\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right]}{h_{i}\left(1-\ell_{1}-\ell_{2}\right)(1-\alpha)} \\
& =\frac{\ell_{i}}{\theta h_{i}\left(1-\ell_{1}-\ell_{2}\right)} \\
& =\frac{\ell_{i}\left(h_{1}+h_{2}\right)\left(\eta^{X}+\ell_{1}+\ell_{2}\right)}{h_{i}\left(\ell_{1}+\ell_{2}\right)\left(1-\ell_{1}-\ell_{2}\right)} \tag{91}
\end{align*}
$$

Averaging with labor income weights,

$$
\begin{equation*}
\eta^{C}=\frac{\ell_{1}+\ell_{2}}{\theta\left(h_{1}+h_{2}\right)\left(1-\ell_{1}-\ell_{2}\right)}=\frac{\eta^{X}+\ell_{1}+\ell_{2}}{1-\ell_{1}-\ell_{2}} \tag{92}
\end{equation*}
$$

Note that

$$
\begin{equation*}
\eta_{i}^{C}=\frac{\frac{\ell_{i}}{\ell_{1}+\ell_{2}}}{\frac{h_{i}}{h_{1}+h_{2}}} \eta^{C} \tag{93}
\end{equation*}
$$

Again, this is a reflection of the assumption of weak separability between consumption and a labor aggregate.
To find $\eta^{U}$, use (72) in the form

$$
\begin{equation*}
d \ln \mu=\ell_{1} d \ln W_{1}-\ell_{2} d \ln W_{2} \tag{94}
\end{equation*}
$$

Then

$$
\begin{equation*}
\eta_{i j}^{U}=\frac{\phi_{i j}-\ell_{i} \phi_{\mu \mu}}{h_{i}}=\eta_{i j}^{\lambda}-\frac{\ell_{i} \ell_{j} \phi_{\mu \mu}}{h_{i}} \tag{95}
\end{equation*}
$$

Adding up over $j$ and using (83), (69) and (70)

$$
\begin{align*}
\eta_{i}^{U} & =\frac{\ell_{i}\left[1-(1-\alpha)\left(\ell_{1}+\ell_{2}\right)\right] \phi_{\mu \mu}}{h_{i}(1-\alpha)} \\
& =\frac{\ell_{i}}{\theta h_{i}} \\
& =\frac{\ell_{i}\left(h_{1}+h_{2}\right)\left(\eta^{X}+\ell_{1}+\ell_{2}\right)}{h_{i}\left(\ell_{1}+\ell_{2}\right)} \tag{96}
\end{align*}
$$

Finally, averaging over $i$ with labor income weights,

$$
\begin{equation*}
\eta^{U}=\frac{\ell_{1}+\ell_{2}}{\theta\left(h_{1}+h_{2}\right)}=\eta^{X}+\ell_{1}+\ell_{2} \tag{97}
\end{equation*}
$$

Not surprisingly,

$$
\begin{equation*}
\eta_{i}^{U}=\frac{\frac{\ell_{i}}{\ell_{1}+\ell_{2}}}{\frac{h_{i}}{h_{1}+h_{2}}} \eta^{U} \tag{98}
\end{equation*}
$$

The foregoing equations show the most important relationships. The one remaining task is show how to find the other elasticities from $\eta^{\lambda}$, which is what we literally do after finding $\eta^{\lambda}$ from the parameteric model. Inverting equation (69) yields

$$
\begin{equation*}
\ell_{1}+\ell_{2}=\frac{\theta\left(h_{1}+h_{2}\right) \eta^{\lambda}}{1+\theta(1-\alpha)\left(h_{1}+h_{2}\right) \eta^{\lambda}} \tag{99}
\end{equation*}
$$

Substituting from (99) into (92) and (97) yields

$$
\begin{gather*}
\eta^{C}=\frac{\eta^{\lambda}}{1-\theta \alpha\left(h_{1}+h_{2}\right) \eta^{\lambda}}  \tag{100}\\
\eta^{U}=\frac{\eta^{\lambda}}{1+\theta(1-\alpha)\left(h_{1}+h_{2}\right) \eta^{\lambda}} \tag{101}
\end{gather*}
$$

Using (97) again to find $\eta^{X}$ from $\eta^{X}=\eta^{U}-\ell_{1}-\ell_{2}$, one finds that

$$
\begin{equation*}
\eta^{X}=\frac{\left[1-\theta\left(h_{1}+h_{2}\right)\right] \eta^{\lambda}}{1+\theta(1-\alpha)\left(h_{1}+h_{2}\right) \eta^{\lambda}} \tag{102}
\end{equation*}
$$

Equation (70) implies

$$
\begin{equation*}
\frac{\frac{\ell_{i}}{\ell_{1}+\ell_{2}}}{\frac{h_{i}}{h_{1}+h_{2}}}=\frac{\eta_{i}^{\lambda}}{\eta^{\lambda}} \tag{103}
\end{equation*}
$$

Together with (93), (98) and (81), (103) implies that one can find the individual elasticities $\eta_{i}^{C}, \eta_{i}^{U}$ and $\eta_{i}^{X}$ by multiplying the corresponding household average elasticities by $\frac{\eta_{i}^{\lambda}}{\eta^{\lambda}}$. The individual local MPE $\ell_{i}$ can be found as

$$
\begin{equation*}
\ell_{i}=\frac{h_{i} \eta_{i}^{\lambda}}{\left(h_{1}+h_{2}\right) \eta^{\lambda}}\left(\ell_{1}+\ell_{2}\right)=\frac{\theta h_{i} \eta_{i}^{\lambda}}{1+\theta(1-\alpha)\left(h_{1}+h_{2}\right) \eta^{\lambda}} \tag{104}
\end{equation*}
$$

Finally, in the main text, we discuss the individual own-wage uncompensated elasticity in a dual earner setting: $\eta_{i i}^{X}$. Equations (78), (83), (99) and (104) imply

$$
\begin{equation*}
\eta_{i i}^{X}=\eta_{i i}^{\lambda}-\frac{\theta h_{i} \eta_{i}^{\lambda}\left[1+\theta(1-\alpha) h_{i} \eta_{i}^{\lambda}\right]}{1+\theta(1-\alpha)\left(h_{1}+h_{2}\right) \eta^{\lambda}} \tag{105}
\end{equation*}
$$

In translating these formulas into those in the main text, set $\theta=1$ to impose scale symmetry in consumption and $\eta_{i i}^{\lambda}=\eta_{i}^{\lambda}$ to impose Frisch independence of $N_{1}$ and $N_{2}$. Also, remember that similarly to the other overall household elasticities designated by $\eta$,

$$
\eta^{\lambda}=\frac{h_{1} \eta_{1}^{\lambda}+h_{2} \eta_{2}^{\lambda}}{h_{1}+h_{2}}
$$

and that

$$
h_{i}=\frac{W_{i} N_{i}}{C}
$$


[^0]:    ${ }^{30}$ Both here and in the corresponding expressions below, when a household member works is paid for less than 52 weeks per year, both the labor income $W_{i, t} N_{i, t}$ and the job-induced consumption $J_{i, t}$ need to be multiplied by the actual number of weeks worked per year divided by 52 .

[^1]:    ${ }^{31}$ We do not make adjustments for children, which are infrequent in the HRS sample.
    ${ }^{32}$ See the Technical Appendix C for a demonstration of how these formulas hold in much greater generality.

