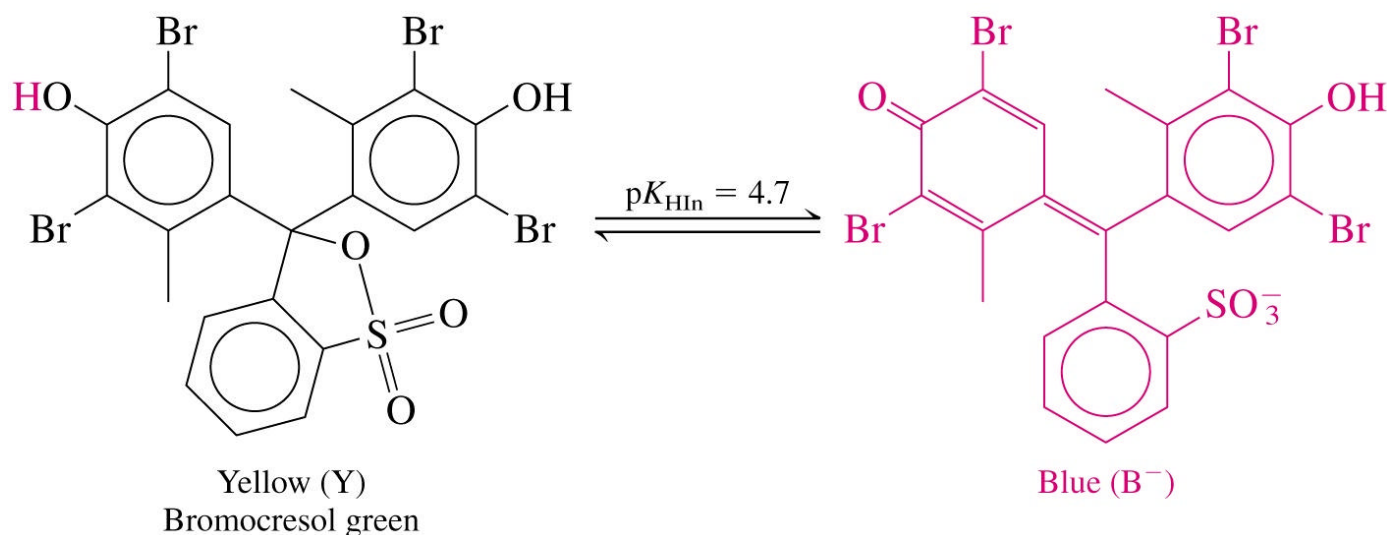


pH indicators---how they work!

pH indicators are either weak acids or weak bases---that are different in color (change in absorbance) in protonated vs. unprotonated form!

They are used at very low concentrations ----to “indicate” the pH of the solution----with the pH generally being controlled by other components!!



Equilibrium for indicator species: $\text{Hin} \rightleftharpoons \text{H}^+ + \text{In}^-$

$$K_{\text{Hin}} = \frac{[\text{H}^+][\text{In}^-]}{[\text{Hin}]}$$

$$\text{pH} = \text{p}K_{\text{Hin}} + \log \frac{[\text{In}^-]}{[\text{Hin}]}$$

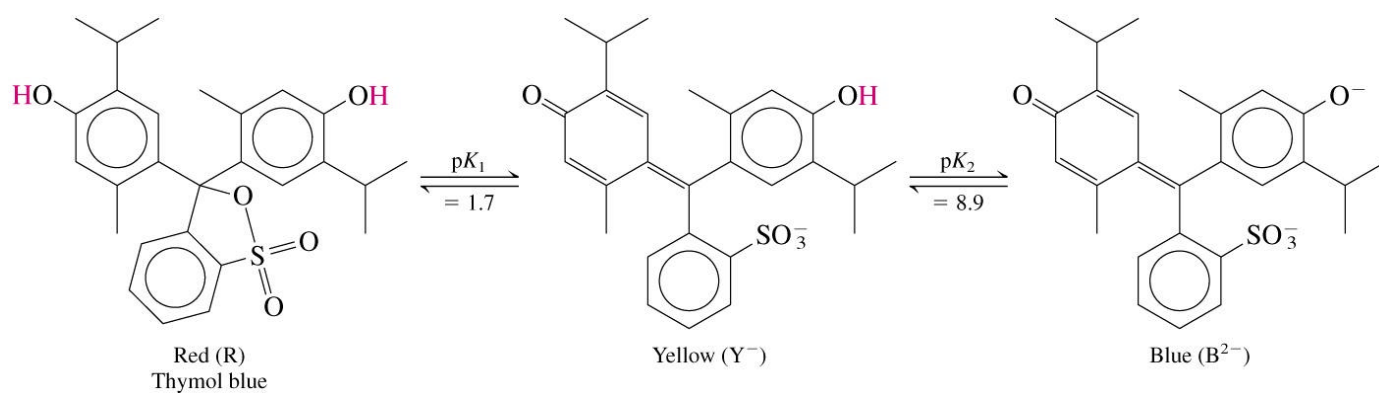
for bromocrescol green----**In⁻** is blue and **HIn** is yellow!

at pH 4.7 (the $\text{p}K_{\text{a}}$) ---have half in blue form, and half in yellow form-
get a green color!!

Typically---when $[\text{Hin}]/[\text{In}^-] > 10$; color of solution will be color of Hin species; when $[\text{In}^-] / [\text{Hin}] > 10$; color of solution will be color of In⁻ species!

•By using very low concentrations of indicator---we can get very sharp change in color at equivalence points in pH titrations!

Example of indicator that is diprotic---two different pKa values
three different species possible--with three different colors!



at pH $\ll 0.7$ ---solution will be **red**
 from pH approx. 0.;7 -2.7; solution will look **orange**
 from pH 2.7 --7.9; solution will be **yellow**
 from pH 7.9 - 9.9 ; solution will be **green**
 at pHs > 9.9 ; solution will be **blue!**

Acid-Base Titrations---predicting shape and pH at given points along a titration curve!

Different types ---

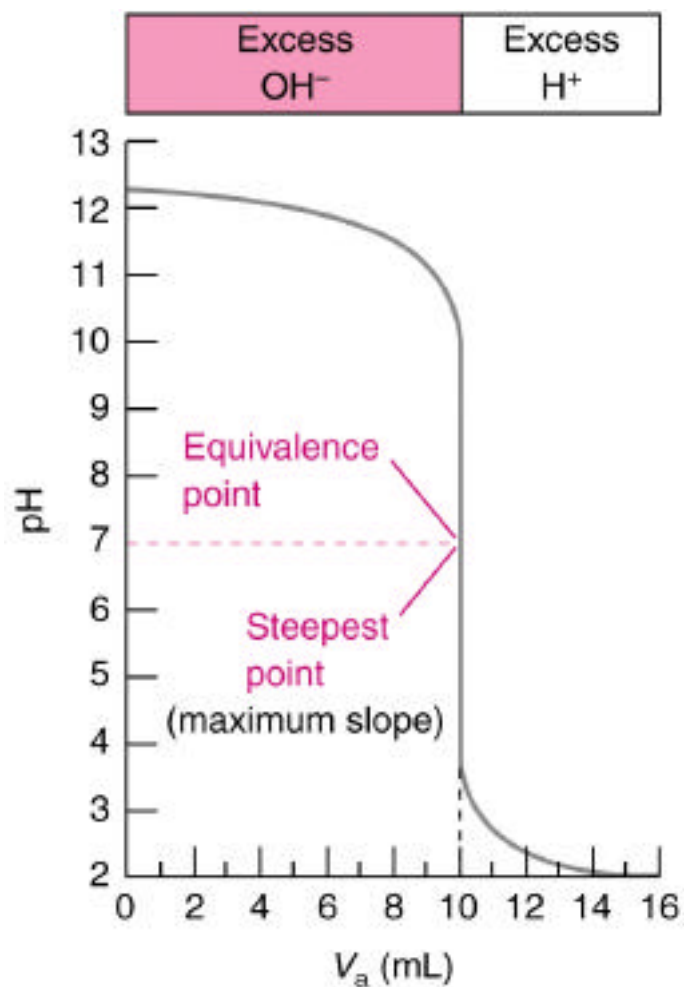
- a) titration of strong acid with strong base or vica versa!
- b) titration of weak acid with strong base
- c) titration of weak base with strong acid

Lets start with strong acid/strong base situation--

we know that $\text{H}^+ + \text{OH}^- \text{-----} \rightarrow \text{H}_2\text{O}$ $K = 1/K_w = 10^{14}$ ---very favorable reaction---rxn goes to completion!

So if we start with base in solution---and add acid---for every proton we add---it will react with hydroxide ion to form water---until there are no more excess hydroxide ions available-**equiv. point = pH 7.0**

3-regions in titration curve-- 1) before equiv. point; 2) at equiv. point; 3) after equiv. point!



titration of 50 mL of 0.02 M KOH with 0.1 M HBr---

need 1 mmole of HBr to neutralize all the base
(50 mL x 0.02 = 1 mmole)

therefore at equiv. point--

$$M_{\text{HBr}} \times V_{\text{HBr}} = 1 \text{ mmole}$$

$$0.1 \times V_{\text{HBr}} = 1 \text{ mmole}$$

$$V_{\text{HBr}} = V_e = 10 \text{ mL}$$

Lets see what pH is at various points---via calculations---

when no acid added:

0.02 M KOH only present; $[\text{OH}^-] = 0.02 \text{ M}$;

$$[\text{H}^+] = 10^{-14} / 0.02 = 5 \times 10^{-13} \text{ M}$$

$$\text{pH} = -\log [\text{H}^+] = \mathbf{12.30}$$

when 3 mL of titrant added:

3 ml x 0.1 M = 0.3 mmols of acid---means that you decrease
total amount of OH^- by 0.3 mmols---

therefore: (1.0 mmole - 0.3 mmols) = 0.7 mmols OH^- still

present in solution---but now the **total volume = 50 + 3 = 53 mL**

$$[\text{OH}^-] = 0.7 / 53 = 0.013 \text{ M} ; [\text{H}^+] = 10^{-14} / 0.013 = 7.69 \times 10^{-13}$$

$$\text{pH} = -\log 7.69 \times 10^{-13} = 12.11$$

when 9.90 mL of acid added:

9.90 x 0.1 M = 0.99 mmols of acid;

thus OH^- left = 1.0 - 0.99 = 0.01 mmols

$$[\text{OH}^-] = 0.01 / 59.9 \text{ mL} = 1.67 \times 10^{-4}$$

$$[\text{H}^+] = 10^{-14} / 1.67 \times 10^{-4} = 5.99 \times 10^{-11} ; \text{ therefore } \mathbf{pH = 10.22}$$

when 10.0 mL of acid added (equivalence point):

10 mL x 0.1 M = 1.0 mmol; no more OH^- from the base is present at this point---only OH^- is from autoprotolysis of water!--

$$[\text{OH}^-] = 10^{-7} ; [\text{H}^+] = 10^{-7} ; \mathbf{pH = 7.00}$$

when 10.1 mL of acid added---just beyond equiv. point:

10.1 mL x 0.1 M = 1.01 mmol; excess H^+ by 0.01 mmol

$$[\text{H}^+] = 0.01 \text{ mmol} / 60.1 \text{ mL} = 1.66 \times 10^{-4} \text{ M}$$

$$\text{therefore: } \mathbf{pH = -\log(1.66 \times 10^{-4}) = 3.78}$$

when 11 mL of acid added---far beyond equiv. point:

11 mL x 0.1 M = 1.1 mmol; excess H^+ by 0.1 mmol

$$[\text{H}^+] = 0.1 \text{ mmol} / 61.0 \text{ mL} = 1.64 \times 10^{-3} \text{ M}$$

$$\mathbf{pH = -\log(1.64 \times 10^{-3}) = 2.79}$$

For titration of strong acid with base--the same exact approach is taken to find the pH at various points along the titration curve!

Sample problem: Find the pH when 12.75 mL of 0.0501 M NaOH have been added to 25.00 mL of 0.0506 M HClO_4 !

- how many moles of HClO_4 originally present?

$$25 \text{ mL} \times 0.0506 \text{ M} = \mathbf{1.265 \text{ mmoles}}$$

- after 12.75 mL base--how many moles of base?

$$12.75 \text{ mL} \times 0.0501 \text{ M} = \mathbf{0.639 \text{ mmoles}}$$
 of base---so there must be excess acid still left!

How much acid left? $1.265 - 0.639 = \mathbf{0.626 \text{ mmoles}}$

What pH? ; $[\text{H}^+] = 0.626 \text{ mmoles} / 37.75 \text{ mL} = 0.0166 \text{ M}$

$$\mathbf{pH = -\log (0.0166) = 1.78}$$

↙ total volume

Find pH after 50 mL of base added?--50 mL x 0.0501 M = 2.505 mmole

now have excess base- : $2.505 - 1.265 = 1.24 \text{ mmoles NaOH excess}$

$$[\text{OH}^-] = 1.24 \text{ mmoles} / 75 \text{ mL} = 0.0165 \text{ M} ; [\text{H}^+] = 10^{-14} / 0.0165 =$$

$$[\text{H}^+] = 6.06 \times 10^{-13} ; \mathbf{pH = 12.22}$$

Titration of weak acid with strong base:



let's say pK_a of HA = 6.15; $K_a = 7.08 \times 10^{-7}$

What is K_b for A^- ? recall--- $K_b = 10^{-14} / K_{a(\text{HA})}$

then $K_b = 1.41 \times 10^{-8}$ ----for rxn in opposite in direction of above-
therefore $K' = 1/(1.41 \times 10^{-8}) = \mathbf{7.1 \times 10^7}$

since K' is large---neutralization reaction goes completely to right

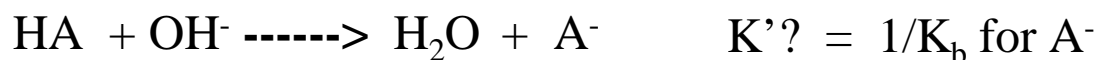
Let's say we have 50.00 mL of 0.0200 M of HA to start in solution!

how much volume of 0.1000 M NaOH is needed to reach equiv. point?

$50.00 \text{ mL} \times 0.0200 \text{ M} = \mathbf{1 \text{ mmole}}$ of acid present---need **1 mmole** of base to reach equivalence point---

Therefore--- $0.1000 \text{ M} \times V_{\text{base}} = 1 \text{ mmole}$; $V_{\text{base}} = \mathbf{10 \text{ mL}}$

Titration of weak acid with strong base:



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What is K_b for A^- ? recall--- $K_b = 10^{-14} / K_{a(\text{HA})}$

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Therefore--- $0.1000 \text{ M} \times V_{\text{base}} = 1 \text{ mmole}$; $V_{\text{base}} = \mathbf{10 \text{ mL}}$

four regions of the titration curve----

1) no base added; what is starting pH?

Calculate like weak acid problem- for F= 0.0200 M with

$$K_a = 7.08 \times 10^{-7}$$

$$x^2 / (0.0200 - x) = 7.08 \times 10^{-7} ; x = 1.19 \times 10^{-4} = [H^+] ; \text{pH} = 3.93$$

2) initial addition of base to titrate weak acid---becomes buffer system

calculation problem-----some of $HA + OH^- \rightarrow A^- + H_2O$

For example---say 2 mL of 0.1000 M NaOH---

produce $2 \text{ mL} \times 0.1000 \text{ M} = 0.2 \text{ mmoles of } A^-$

starting $HA = 1 \text{ mmole}$; therefore after 2 mL of NaOH solution possesses $1.000 - 0.200 = 0.800 \text{ mmoles } HA$ and $0.2 \text{ mmoles } A^-$

Can use HH eqn to calculate pH in this region of titration curve--

$$\text{pH} = \text{p}K_a + \log ([A^-] / [HA]) = 6.15 + \log (0.2 / 0.8) = 5.55$$

note: don't need to calculate conc. of A^- and HA --only need mmoles for numerator and demoninator!

when you have added 5 mL of titrant ---then $V_{\text{base}} = 1/2 V_{\text{eq}}$

Exactly 1/2 of the HA has been titrated----

This means that $[\text{HA}] = [\text{A}^-] \approx 1/2 F$ --the initial conc. of HA

Special situation---since $\text{pH} = \text{pK}_a + \log ([\text{A}^-] / [\text{HA}])$ ---but
log term -----> 0 since $[\text{HA}] = [\text{A}^-]$; **pH = pK_a = 6.15**

3. At equivalence point (10 mL of NaOH added):

All the HA -----> A^- and water----Hence the pH at equiv. point
is a weak base problem----- $\text{A}^- + \text{H}_2\text{O} <-----> \text{HA} + \text{OH}^-$
must calculate $[\text{OH}^-]$ using K_b value---

But-- initial F concentration of A^- is less than initial $[\text{HA}]$ due to dilution by titrant volume!

$[\text{A}^-]_{\text{eq}} = 1 \text{ mmole} / 60 \text{ mL} = \mathbf{0.01667 \text{ M} = F'}$ (new formal conc.)

initial moles of HA at start of titration!
total vol. at equiv. point!

$$K_b \text{ for } A^- = 1.41 \times 10^{-8} = x^2 / (F' - x) \quad ; \quad F' = 0.01667 \text{ M}$$

$$X = 1.53 \times 10^{-5} = [OH^-] \quad ; \quad [H^+] = 10^{-14} / (1.53 \times 10^{-5}) = 6.54 \times 10^{-10}$$

$$\text{pH} = -\log(6.54 \times 10^{-10}) = 9.18 \quad = \text{pH at equiv. point}$$

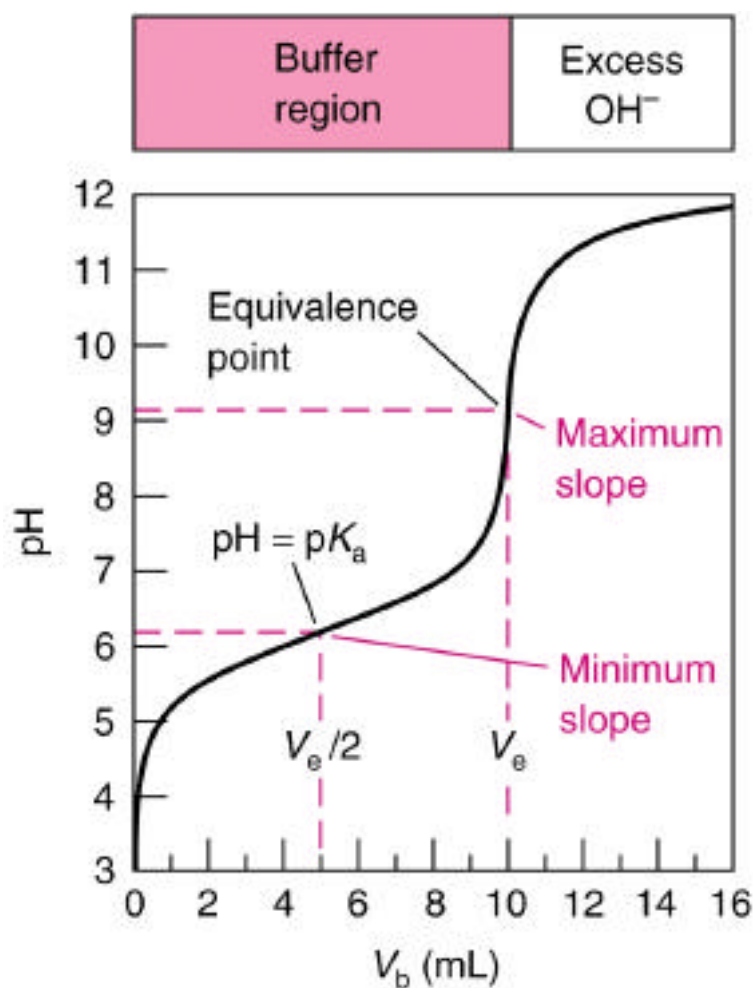
4) pH when there is excess strong base----; can assume contribution from weak base A^- is negligible!

e.g. **11 mL of NaOH added**; total volume now = 61.00 mL

excess base = 1 mL x 0.1000 M = 0.1 mmole;

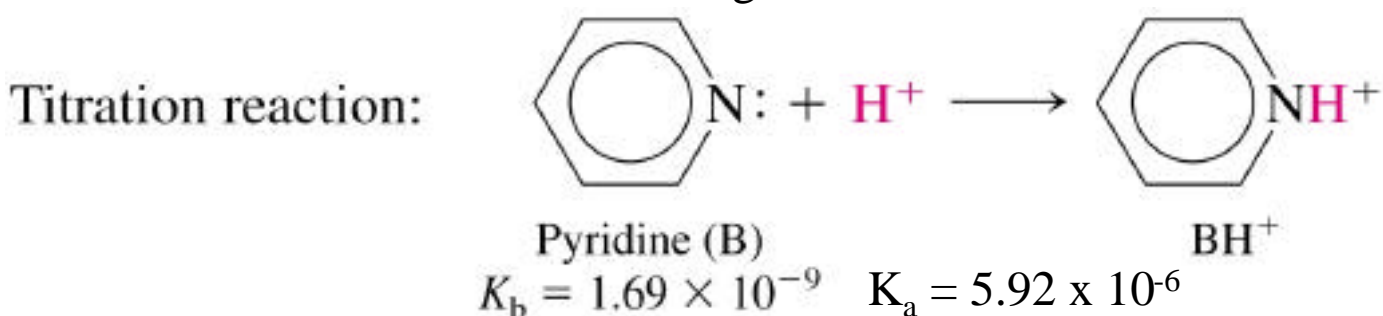
Therefore: $0.1000 / 61.00 = 0.0016 \text{ M} = [OH^-]$

thus-- $[H^+] = 10^{-14} / 0.0016 = 6.25 \times 10^{-12}$; **pH = 11.20**



This is the actual titration curve for 0.02 M HA with $\text{pK}_a = 6.15$ with 0.1000 M NaOH ---we calculated several of the points along the way--on the previous pages!!

Titration of weak base with strong acid---Analogous treatment to titration of weak acid with strong base!!



e.g.---25.00 mL of 0.08364 M pyridine titrated with 0.1067 M HCl
 mmoles pyridine base = $0.08364 \times 25.00 = \mathbf{2.091 \text{ mmoles}}$

at equiv. point:

$$V_{\text{HCl}} \times 0.1067 \text{ M} = 25.00 \text{ mL} \times 0.08364 ; V_{\text{e(HCl)}} = \mathbf{19.60 \text{ mL HCl}}$$

What is pH after 4.63 mL of acid added:

mmoles acid = $4.63 \times 0.1067 = \mathbf{0.4940 \text{ mmole}}$ of Pyridinium cation;

therefore free base left = $2.091 - 0.4940 = \mathbf{1.597 \text{ mmole}}$ Pyridine left

thus $\text{pH} = \text{pK}_a + \log ([\text{pyr}] / [\text{Hpyr}^+]) = 5.23 + \log (1.597 / 0.4940) =$
 $\text{pH} = 5.74$

What would be pH at equivalence point?

This is weak acid problem---all of the pyridine converted to Hpyr⁺;
-started with 2.091 mmoles pyridine---will have 2.091 mmoles of
pyridinium ion at equivalence point!

$$K_a = 5.92 \times 10^{-6} = x^2 / (F' - x)$$

$$F' = 2.091 \text{ mmoles} / (25.0 \text{ mL} + 19.6 \text{ mL}) = 0.0469 \text{ M Hpyr}^+$$

$$x_1 = 1.67 \times 10^{-4}; \quad x_2 \text{ (second. approx.)} = 1.66 \times 10^{-4} = [\text{H}^+]$$

$$\text{pH} = 3.78$$

note: pH at equivalence point is quite low--why? ---because
pyridine is very weak base!---if you calculated pH at start of titration
what would it be? $1.69 \times 10^{-9} = x^2 / (F - x)$; $F = 0.08364$

$$x = [\text{OH}^-] = 1.19 \times 10^{-5}; \quad [\text{H}^+] = 8.40 \times 10^{-10}$$

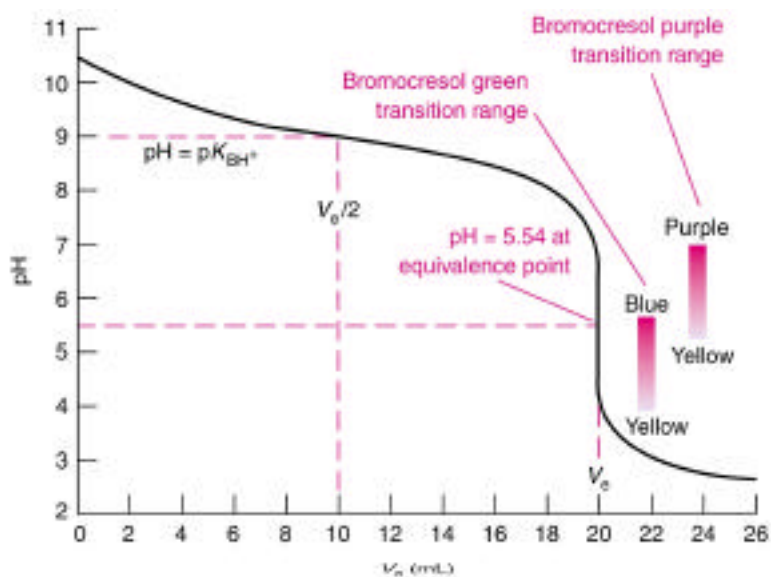
$$\text{pH} = 9.08$$

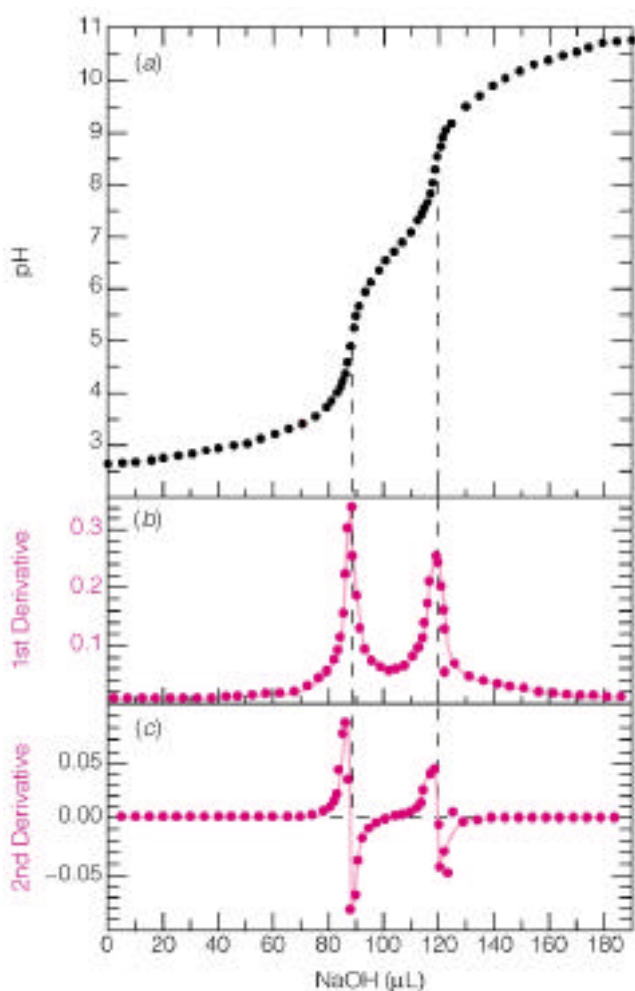
Detecting end points!---use of indicators

-choose indicator that has pK_a near the equivalence point pH of for titration---so that color change occurs in steepest region of titration curve!

- always use small amount of indicator---since they are also acids and bases---hence using high concentrations will consume analyte or titrant!

titration of
weak base with
 $pK_b = 5.00$ with
(100 mL of 0.0100 M)
with 0.0500 M HCl





With indicators--can only see pH change at end point of titration

Use pH electrode to monitor pH of solution throughout titration

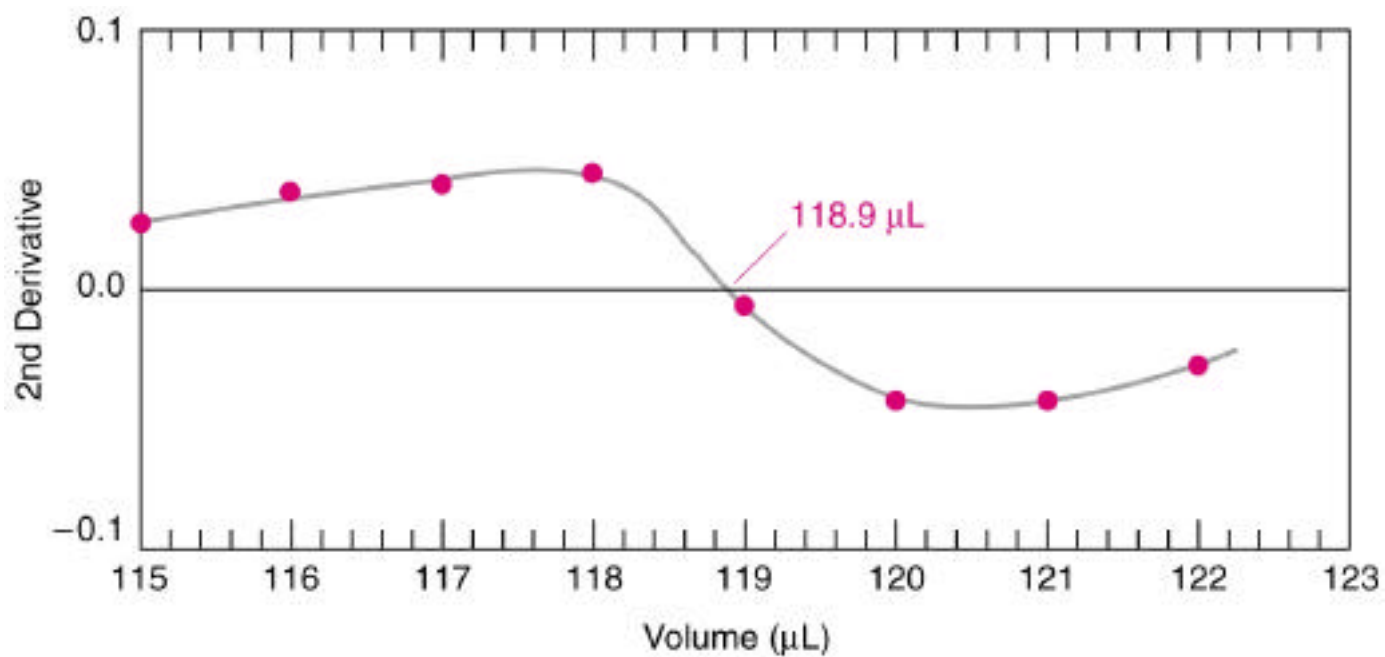
End point/equivalence point can be determined by either first or second derivative method!

slope = $\frac{pH}{vol} = 1st\ derivative$

second deriv = $\frac{(d(pH)/dV)}{dV}$

endpoint = volume at which second deriv. goes to 0 after inflection

blow-up of second derivative plot near equiv. point!



Can model and predict complete titration of weak base with strong acid---or weak acid with strong base! Results in equations that can be put into Excel spread sheet!

for weak acid titrated by strong base:

$$\phi = \frac{C_b V_b}{C_a V_a} = \frac{\alpha_{A^-} - \frac{[H^+] - [OH^-]}{C_a}}{1 + \frac{[H^+] - [OH^-]}{C_b}}$$

– =fraction of HA in A⁻ form!

for weak base titrated by strong acid:

$$\phi = \frac{C_a V_a}{C_b V_b} = \frac{\alpha_{BH^+} - \frac{[H^+] - [OH^-]}{C_b}}{1 + \frac{[H^+] - [OH^-]}{C_a}}$$

$$\text{where: } \alpha_{A^-} = \frac{K_a}{[H^+] + K_a}$$

= fraction of way to equivalence point

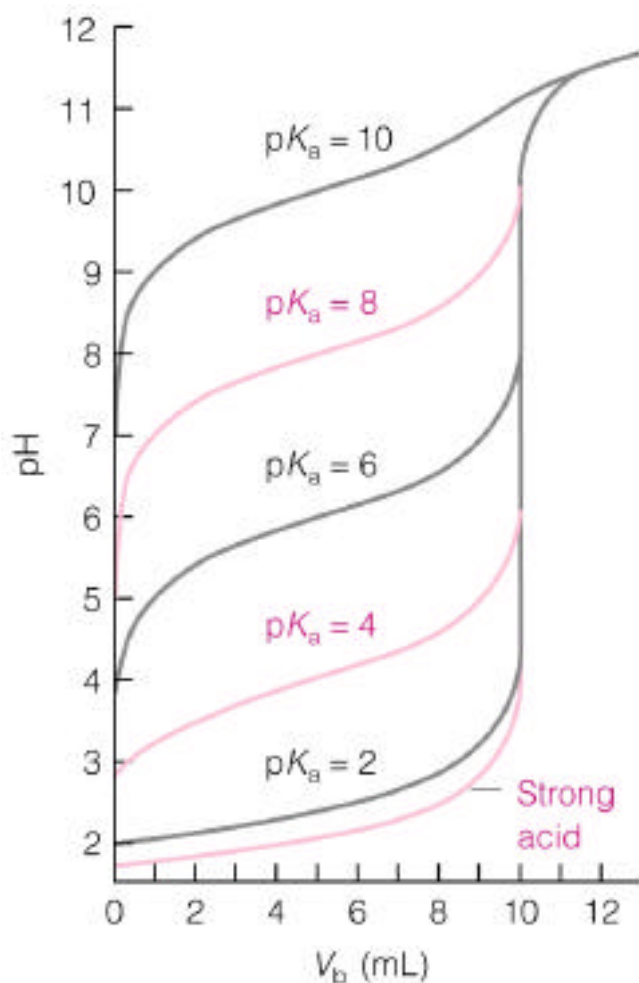
C_b =conc. of base

C_a = conc. of acid

V_a = volume of acid

V_b = volume of base

$$\alpha_{BH^+} = \frac{[H^+]}{[H^+] + K_{a(BH^+)}}$$



example calculated curves
for titration of acids with
strong base--

note: as strength of acid
decreases---end points are
not sharp, and would be
difficult to obtain!

obtain curves by putting in
different pH values in eqn
(then can calc. $[H^+]$, $[A^-]$, etc.)
and finally V_b values for
x-axis!