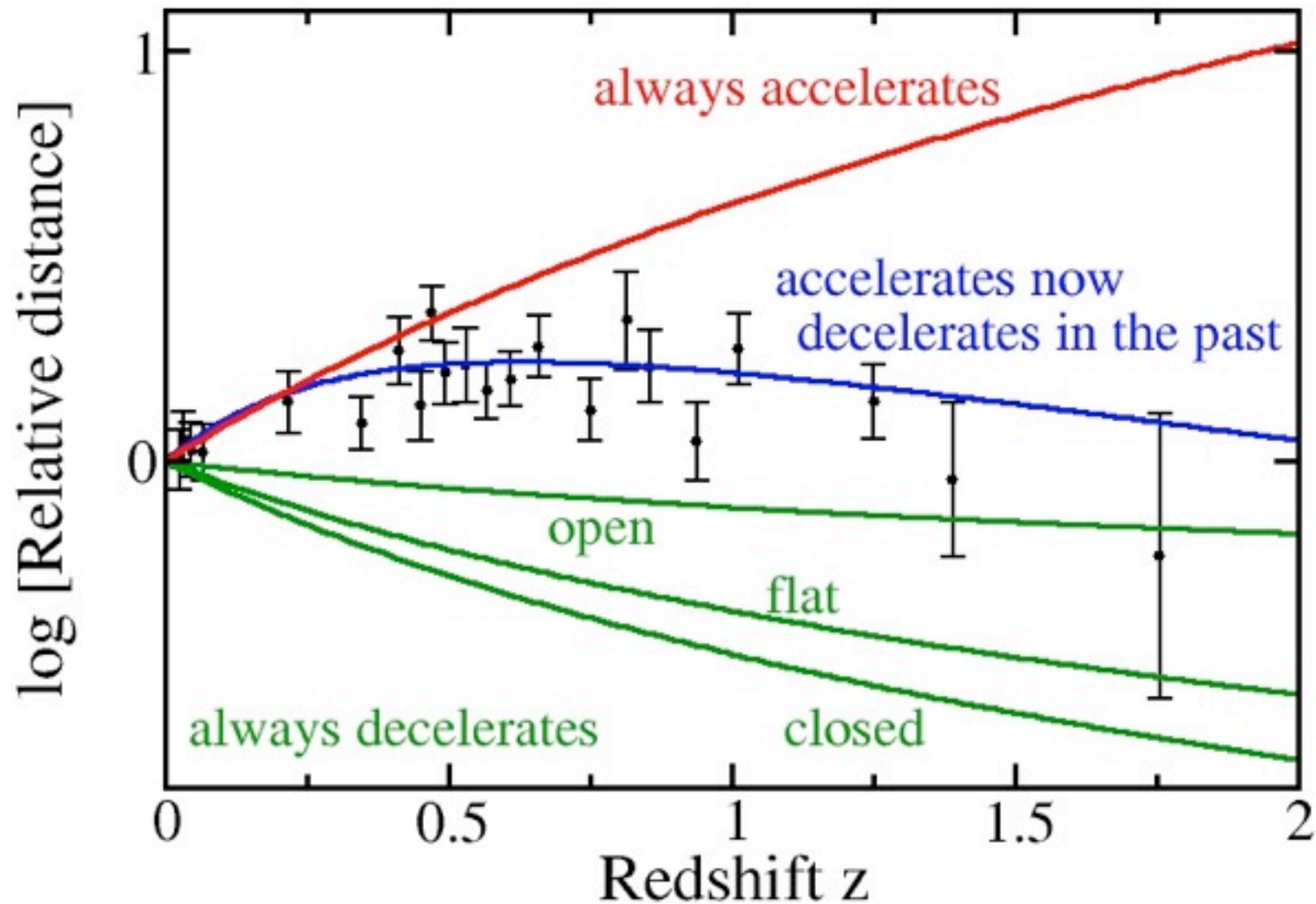


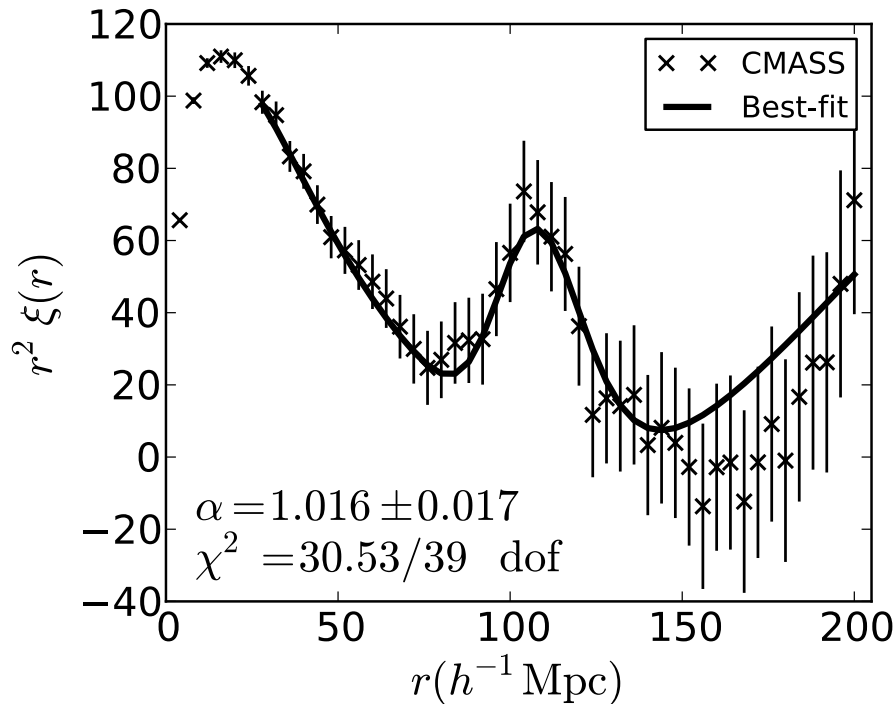
Dark Energy:  
Pedagogical Overview and  
Future Prospects

Dragan Huterer  
University of Michigan

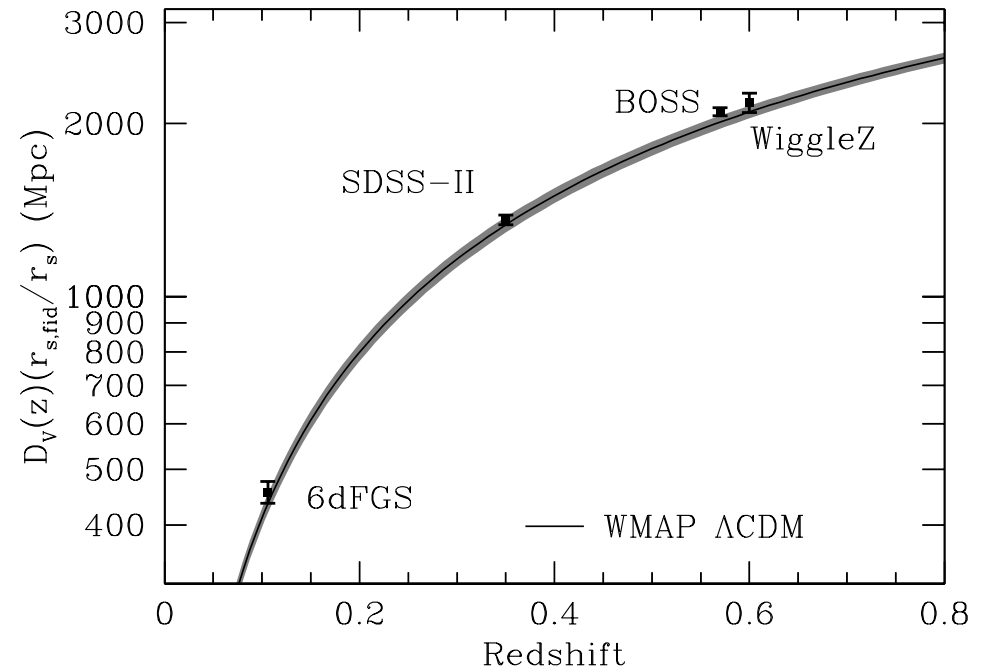
# Supernova Hubble diagram (binned)



# Baryon Acoustic Oscillations



Anderson et al, 1203.6594 (BOSS)



sensitive to  $D_V(z) \equiv \left[ cz (1+z)^2 \frac{D_A^2(z)}{H(z)} \right]^{1/3}$

But, with separation of radial and angular modes,  
 can measure  $D_A(z)$  and  $H(z)$  separately

# Weak Gravitational Lensing



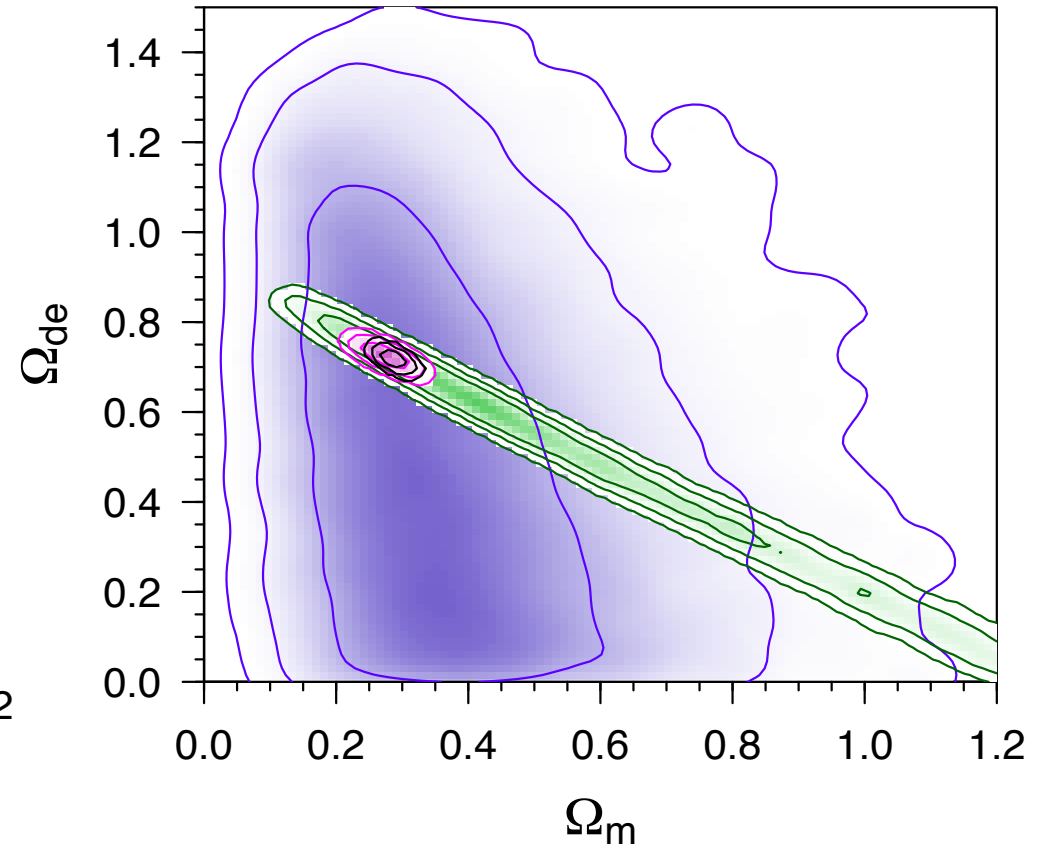
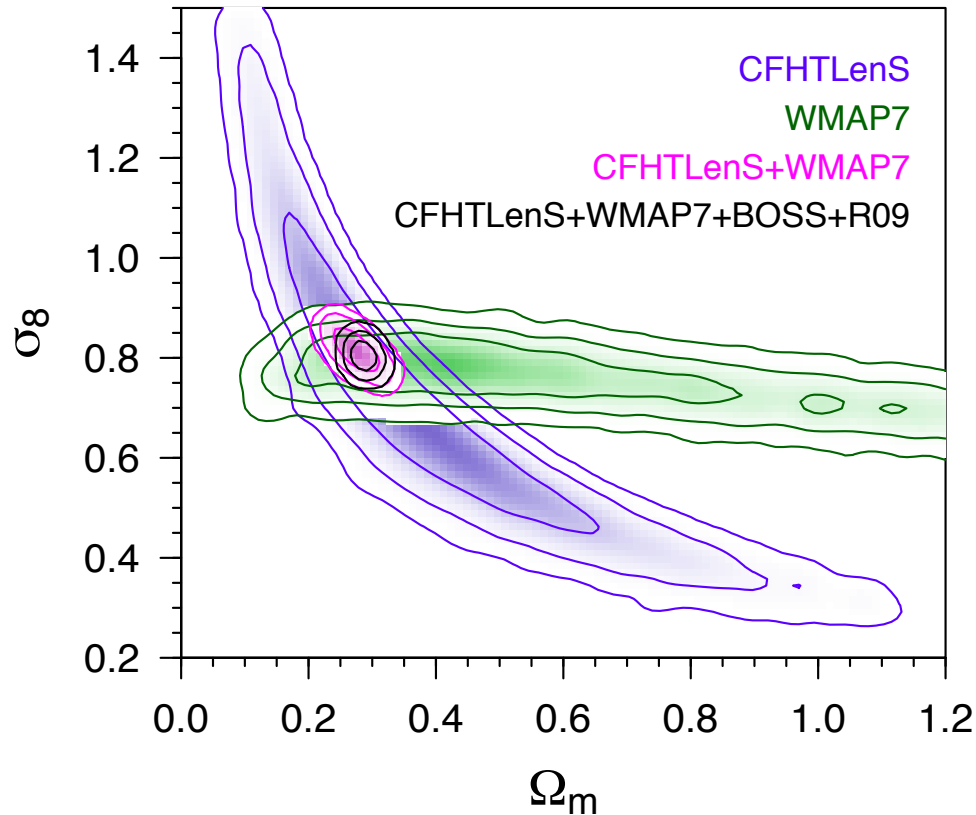
Credit: NASA, ESA and  
R. Massey (Caltech)

**Key advantage: measures distribution of matter, not light**

# Weak Gravitational Lensing

current constraints on DE are weak

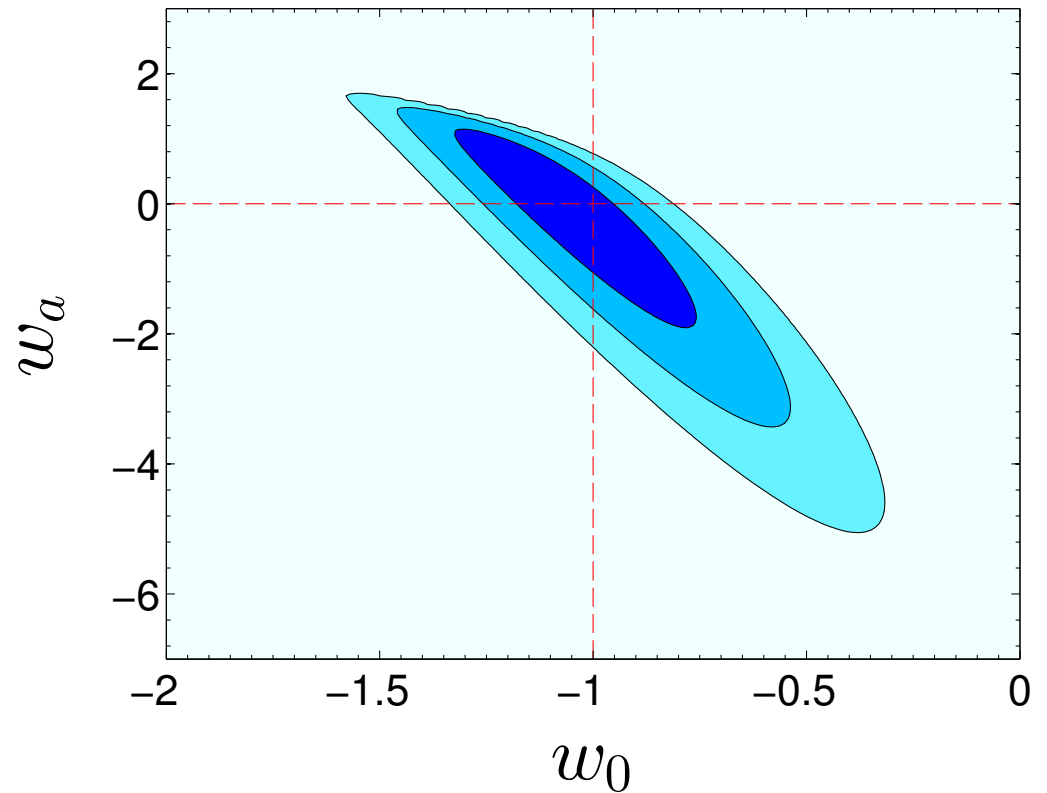
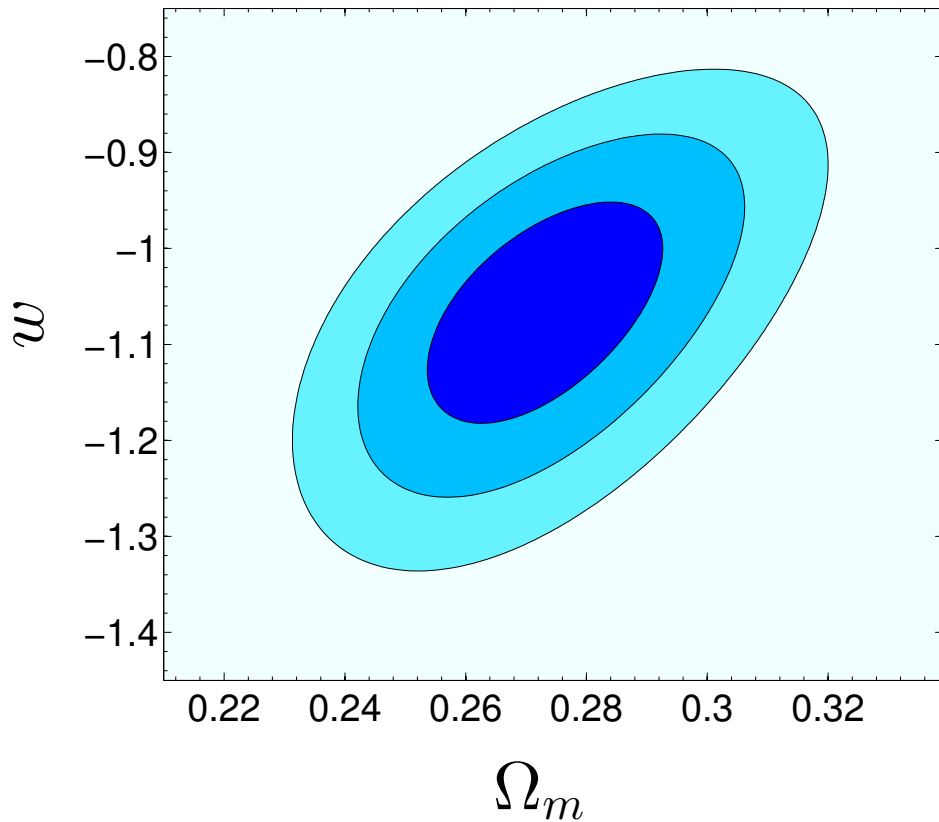
Kilbinger et al (CFHTLenS), arXiv:1212.3338



... but WL still has a lot of promise! (no bias)

Since the discovery of acceleration, constraints have converged to  $w \approx -1$

SN + BAO + CMB(WMAP) data:



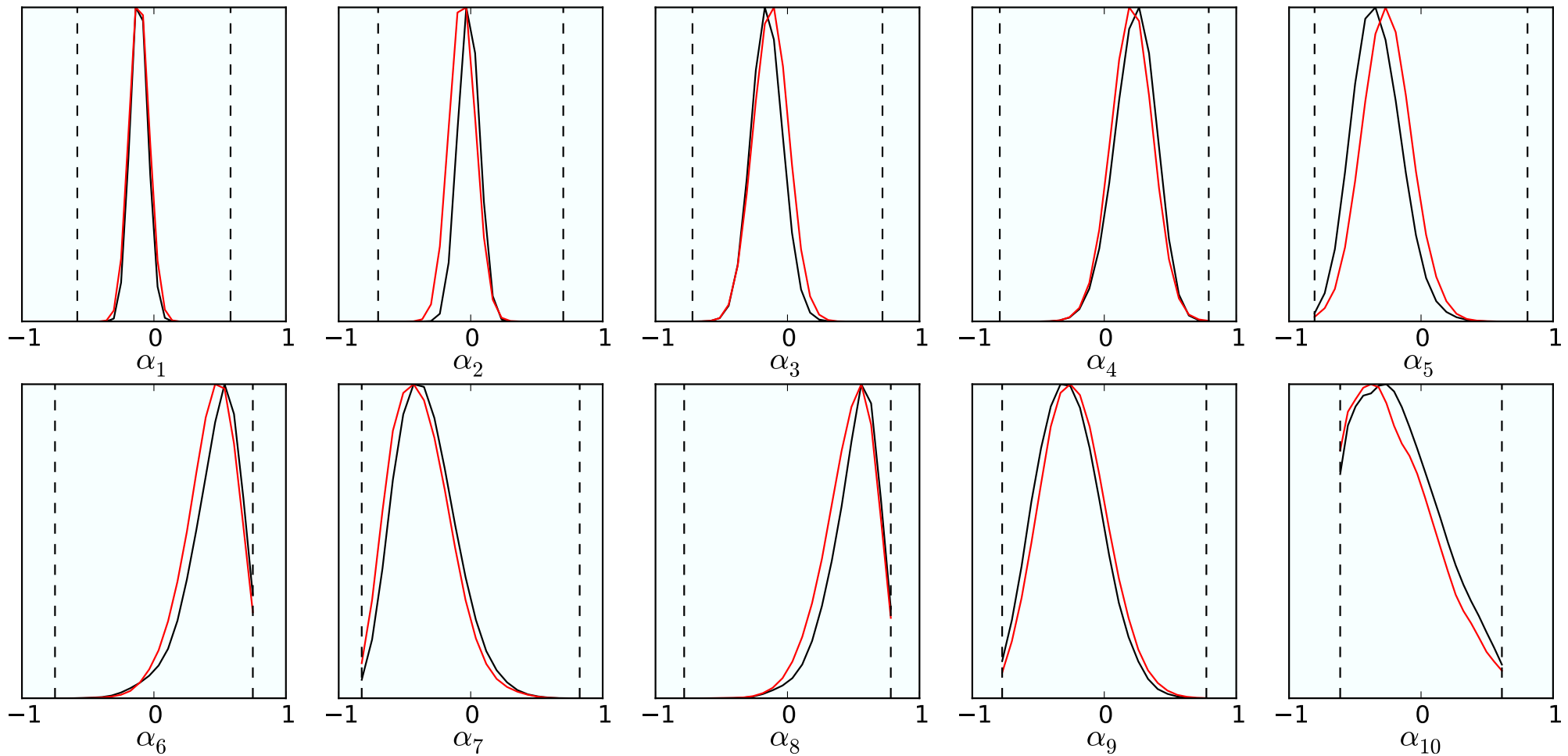
# In *principal*, constraints are good...

(components)

$$w(z_j) = -1 + \sum_{i=1}^N \alpha_i e_i(z_j)$$

$\alpha_i$  = PC amplitude

$e_i(z)$  = PC shape



# Systematic errors

- ▶ Already limiting factor in measurements
- ▶ Will definitely be limiting factor with future data
- ▶ Quantity of interest: (true sys. – estimated sys.) difference
- ▶ **Self-calibration**: measuring systematics internally from the survey -
  - ▶ e.g., parametrize systematics, solve internally for those parameters



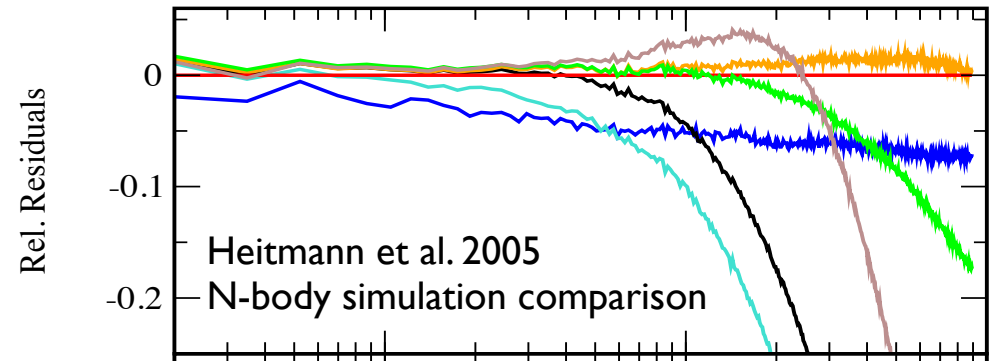
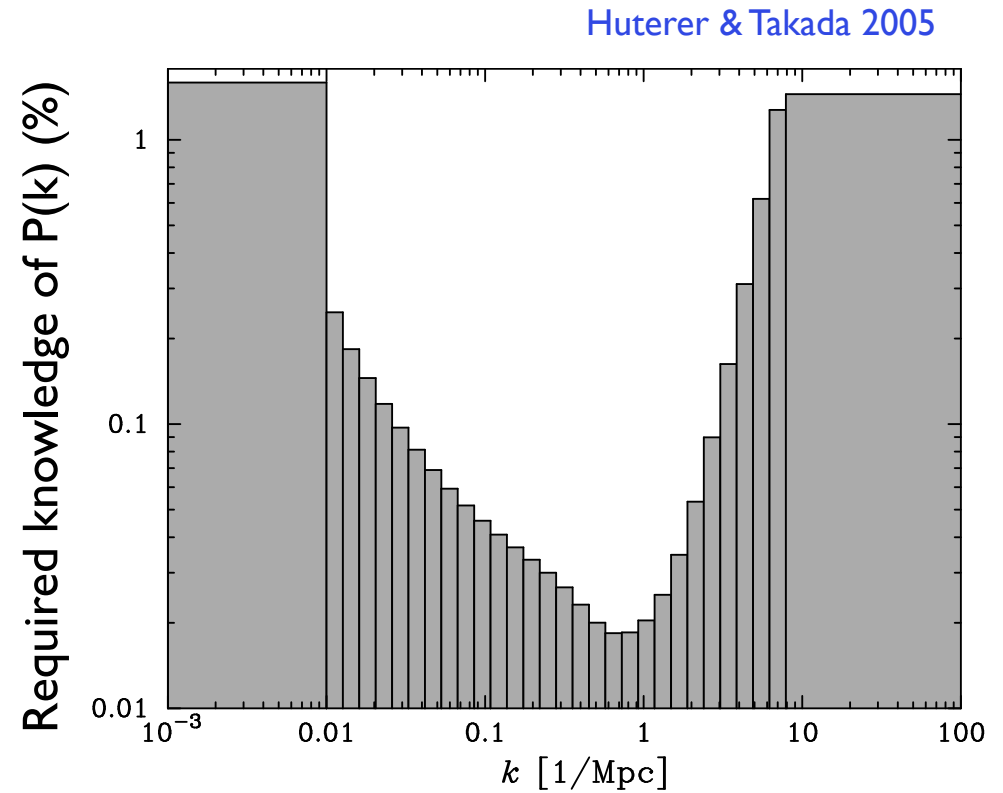
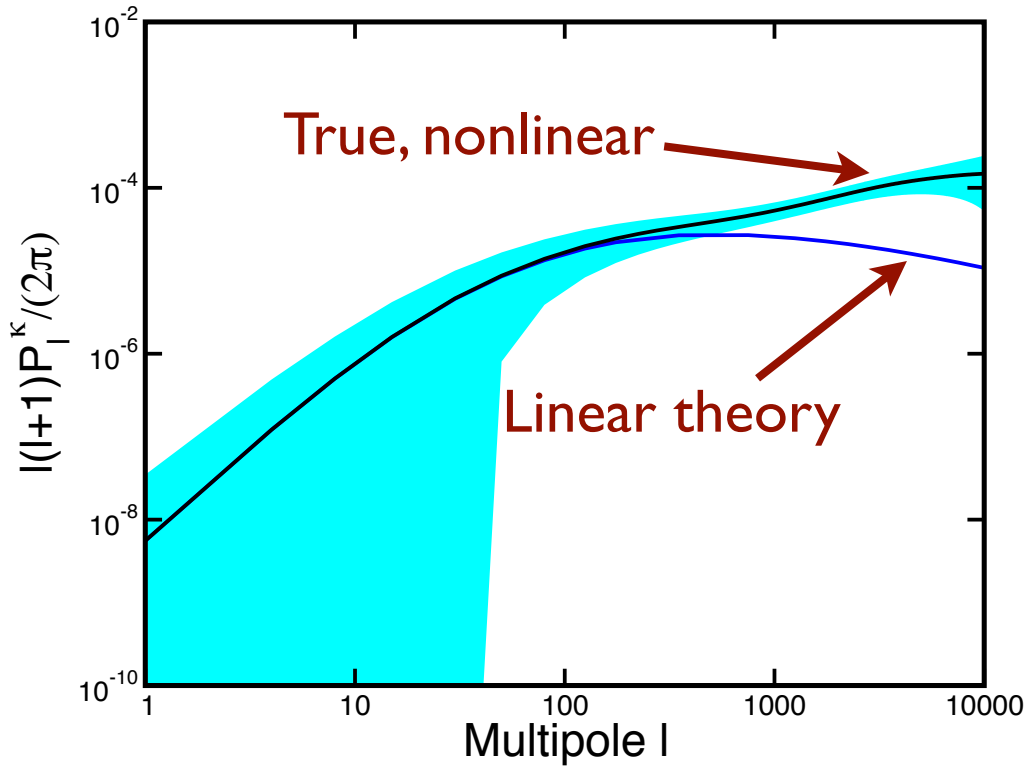
# Systematics summary for the “big four”

Table 2: Comparison of dark energy probes.

Method	Strengths	Weaknesses	Systematics
WL	growth+geometric, statistical power	CDM assumption	image quality, photo-z
SN	purely geometric, mature	standard candle assumption	evolution, dust
BAO	largely geometric, low systematics	large samples required	bias, non-linearity
CL	growth+geometric, X-ray+SZ+optical	CDM assumption	determining mass, selection function

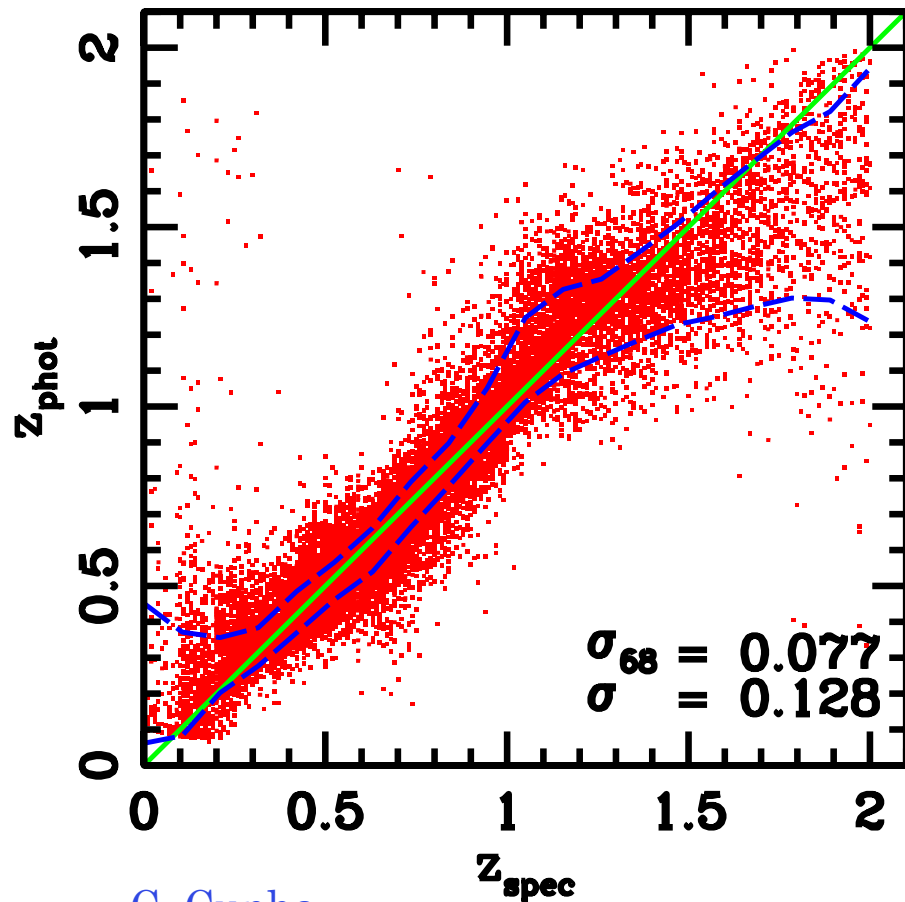
Example 1

# Theory Systematics: calibrating the matter (and, later, gal) $P(k)$ at large $k$



## Example 2

# Poster child of systematics: photometric redshift errors



C. Cunha

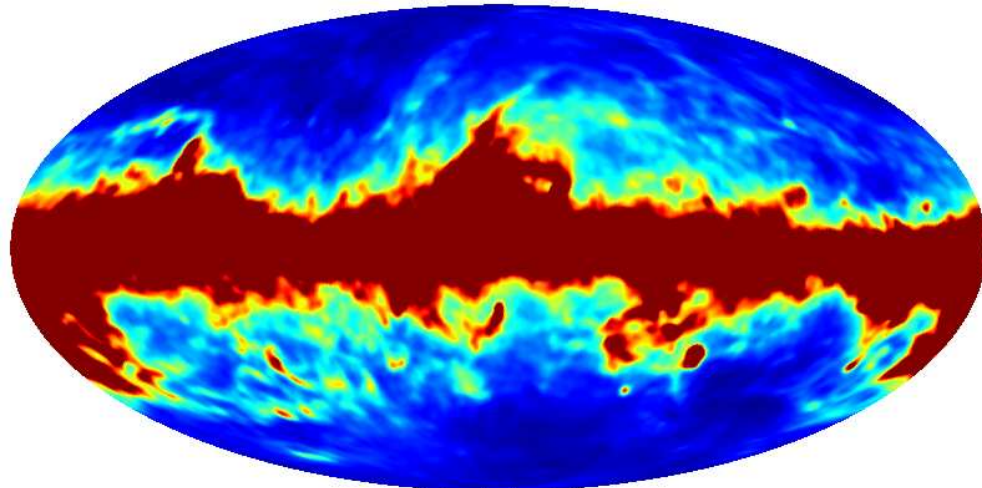
- Measure  $z_{\text{phot}}$  from colors
- Calibrate  $P(z_{\text{phot}} | z_{\text{spec}})$  relation from spectroscopic follow-up
- Need accurate characterization of “islands”, not just `sigma_error` of the “core” of distribution

• Major challenge: spectroscopic surveys typically much shallower than photometric

Example 3

# Photometric calibration errors

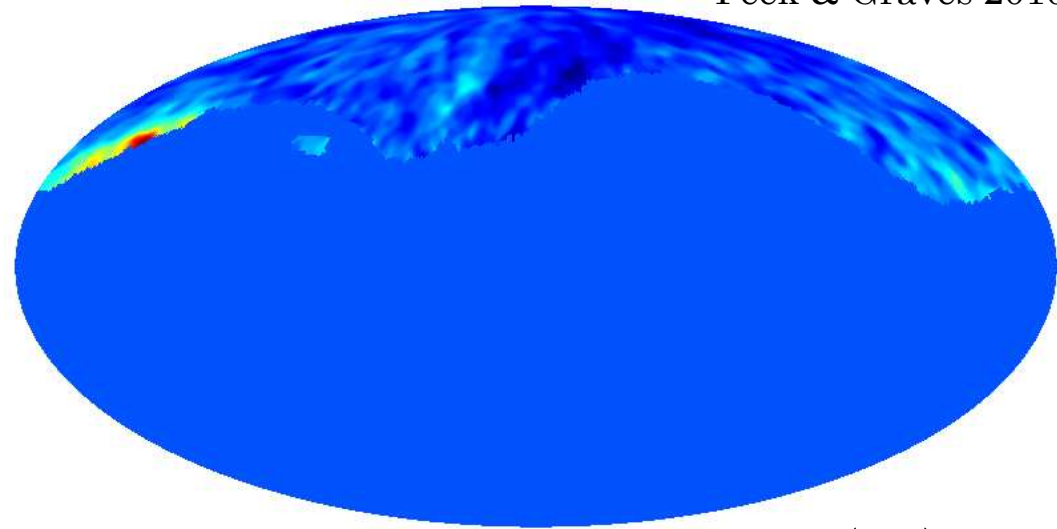
SFD Galactic dust  
extinction map



0.0051 ————— 0.20 E(B-V)

Correction to the extinction map

Peek & Graves 2010



-0.011 ————— 0.043 E(B-V)

Photometric calibration also can be due to:

- “seeing” and weather
- thickness of atmosphere
- instrumental effects
- need to avoid bright stars
- ....

Very generic!

# How do calibration errors affect the measured galaxy angular power spectrum?

$t_{\ell m}$  – observed galaxy field  
 $c_{\ell m}$  – calibration (systematics) field  
 $C_\ell$  – true galaxy clustering power

Final result for the **observed** power spectrum is:

$$\langle t_{\ell m} t_{\ell' m'}^* \rangle = \frac{1}{(1 + \epsilon)^2} \left\{ \underbrace{\delta_{mm'} \delta_{\ell\ell'} C_\ell}_{\text{isotropic}} + \underbrace{\left[ U_{mm'}^{\ell\ell'} C_{\ell'} + (U_{mm'}^{\ell\ell'})^* C_\ell \right] + \sum_{\ell_2 m_2} U_{m_2 m}^{\ell_2 \ell} (U_{m_2 m'}^{\ell_2 \ell'})^* C_{\ell_2}}_{\text{breaks statistical isotropy}} + c_{\ell m} c_{\ell' m'}^* \right\}$$

Cancels effects of  
 calibration  
 monopole

True power

Calibration (biases)

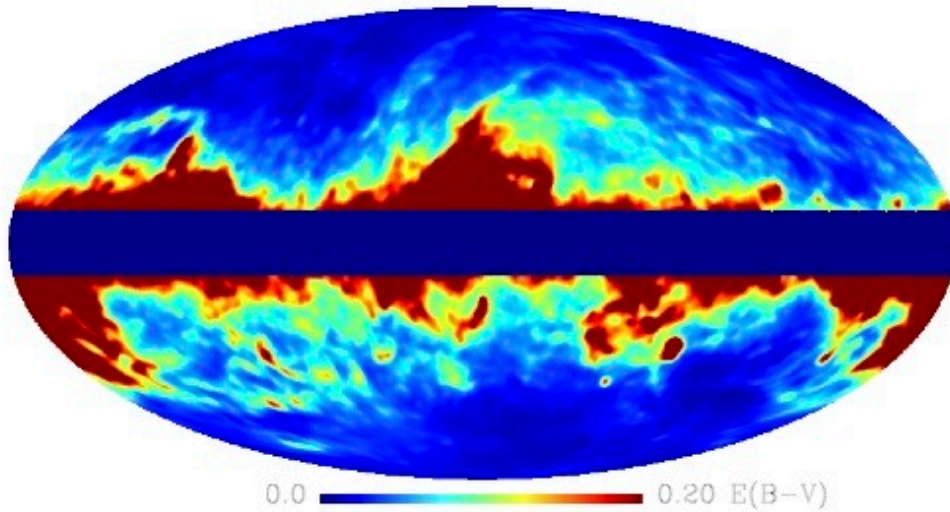
where

$$U_{m_2 m}^{\ell_2 \ell} \equiv \sum_{\ell_1 m_1} c_{\ell_1 m_1} R_{m_1 m_2 m}^{\ell_1 \ell_2 \ell}$$

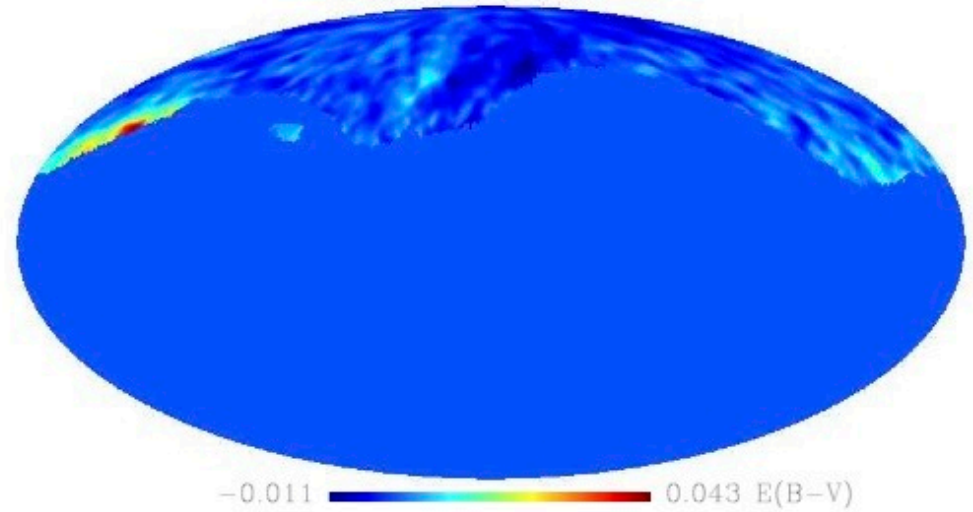
$$R_{m_1 m_2 m}^{\ell_1 \ell_2 \ell} \equiv (-1)^m \sqrt{\frac{(2\ell_1 + 1)(2\ell_2 + 1)(2\ell + 1)}{4\pi}} \begin{pmatrix} \ell_1 & \ell_2 & \ell \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} \ell_1 & \ell_2 & \ell \\ m_1 & m_2 & -m \end{pmatrix}$$

# Calibration bias: Worked Example 1

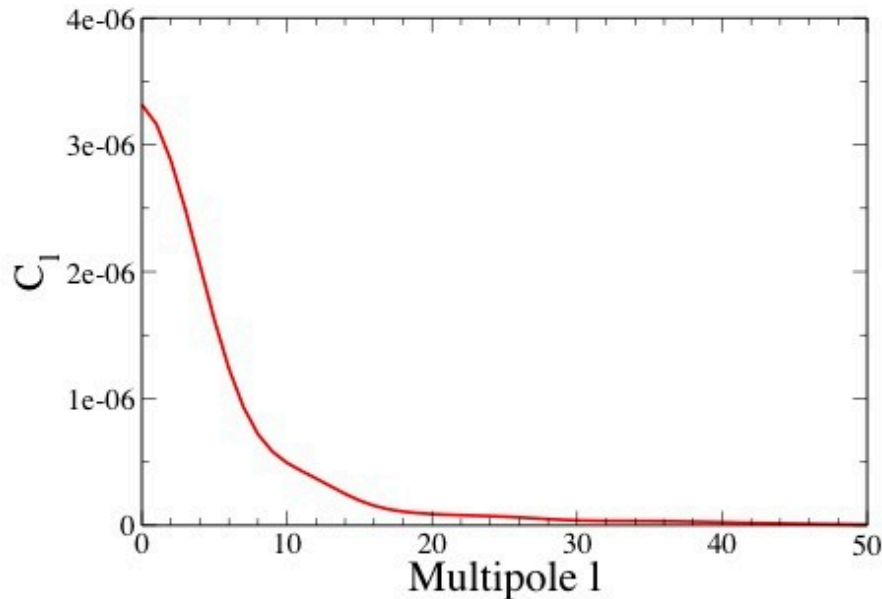
SFD dust map



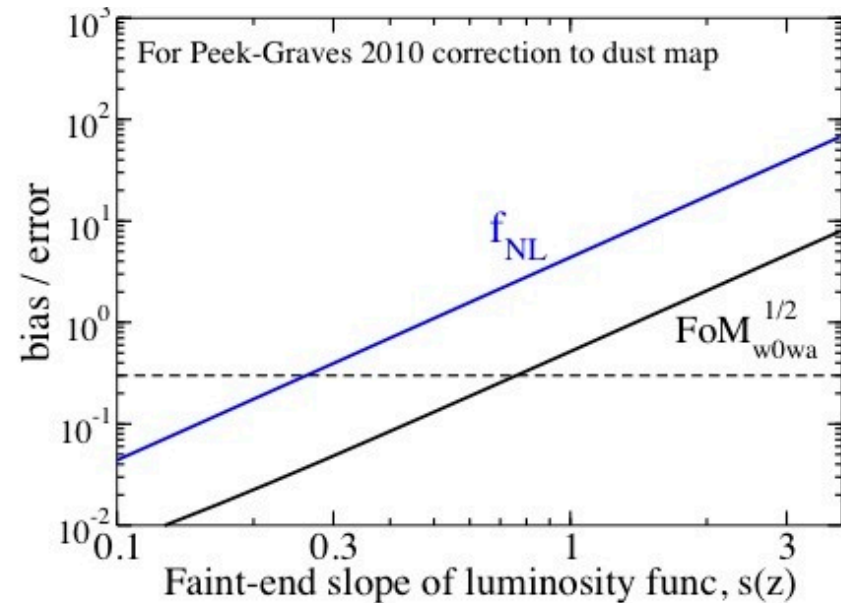
PG10 corrections to map



angular power of corrections

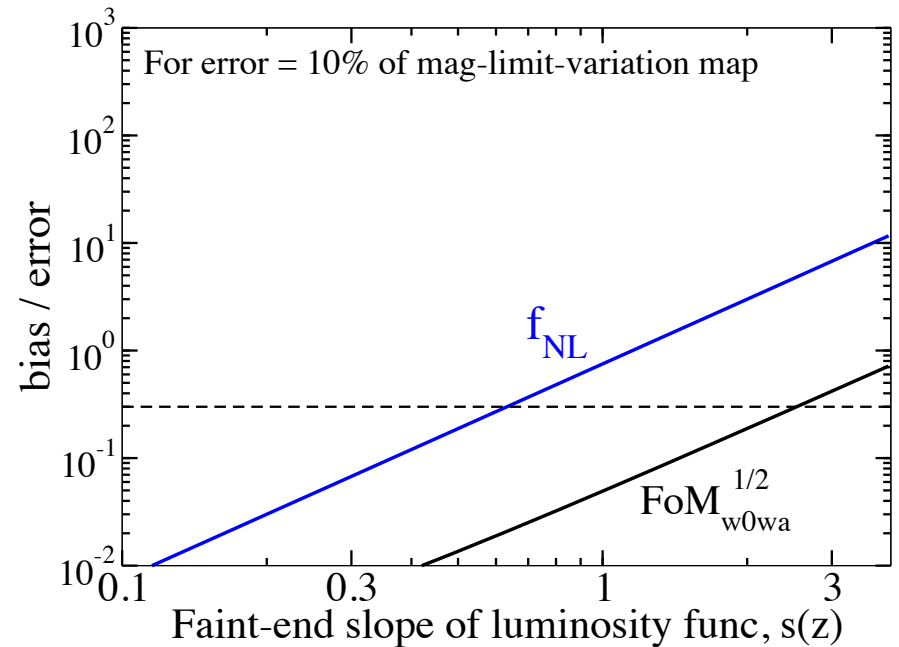
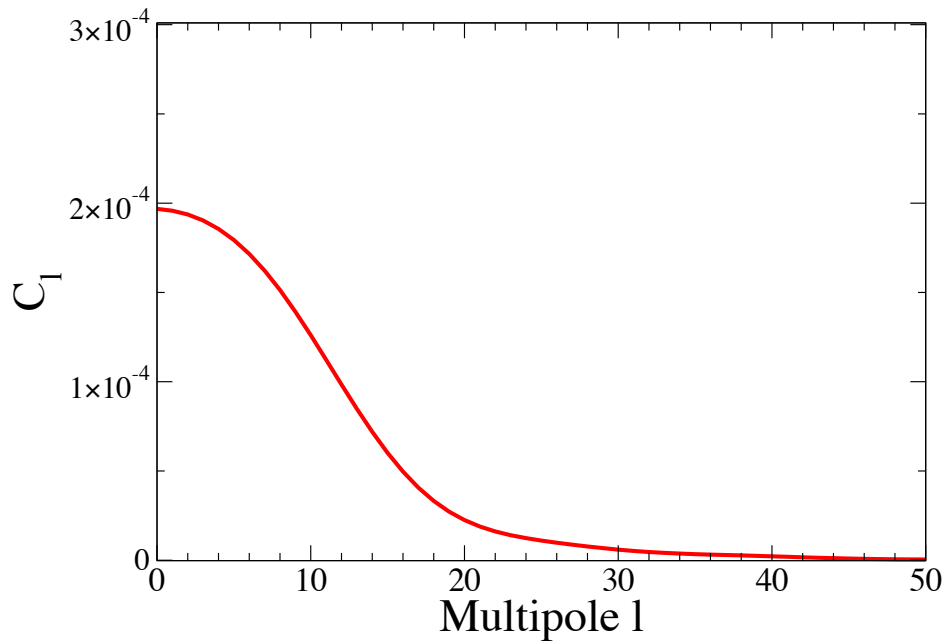
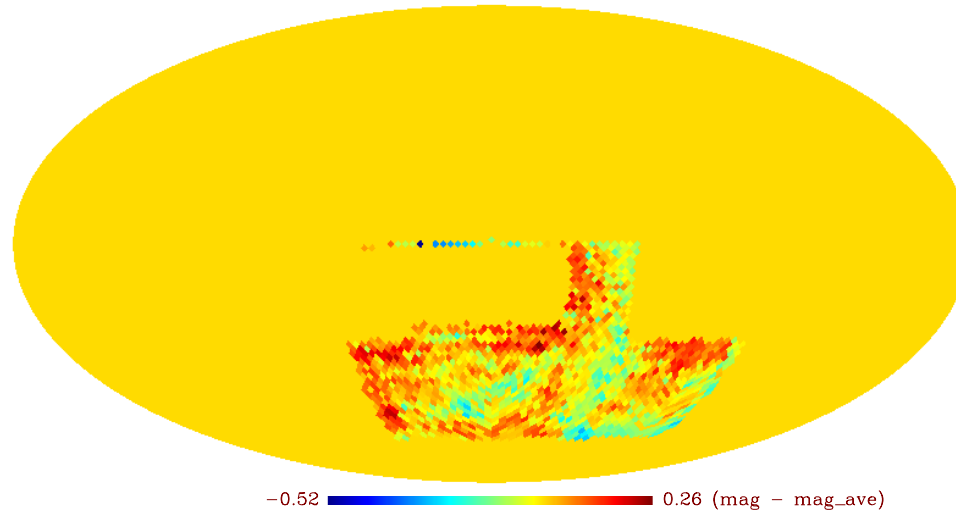


bias/error in cosmology



# Calibration bias: Worked Example 2

DES magnitude limit (J. Annis)



# Photometric Calibration systematics

## Summary of findings:

1. Calibration *breaks statistical isotropy* of LSS signal (obvious in retrospect)
2. *Large-angle* errors beyond the monopole - dipole, quadrupole, etc - are most damaging
3. Control at level  $< 0.1\%$  might be required for DES-type survey and beyond



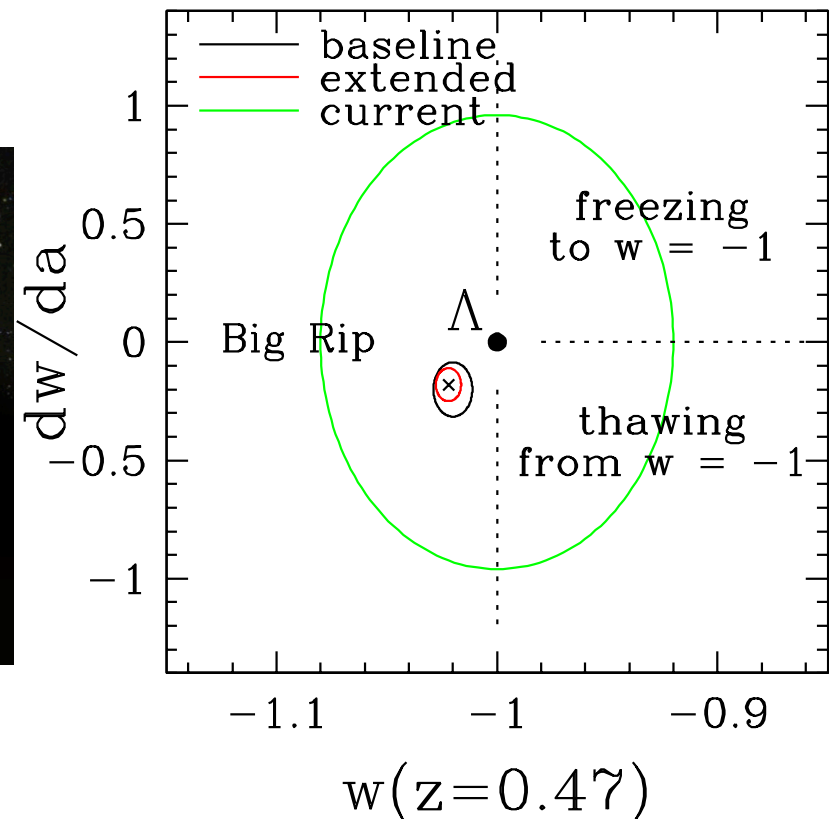
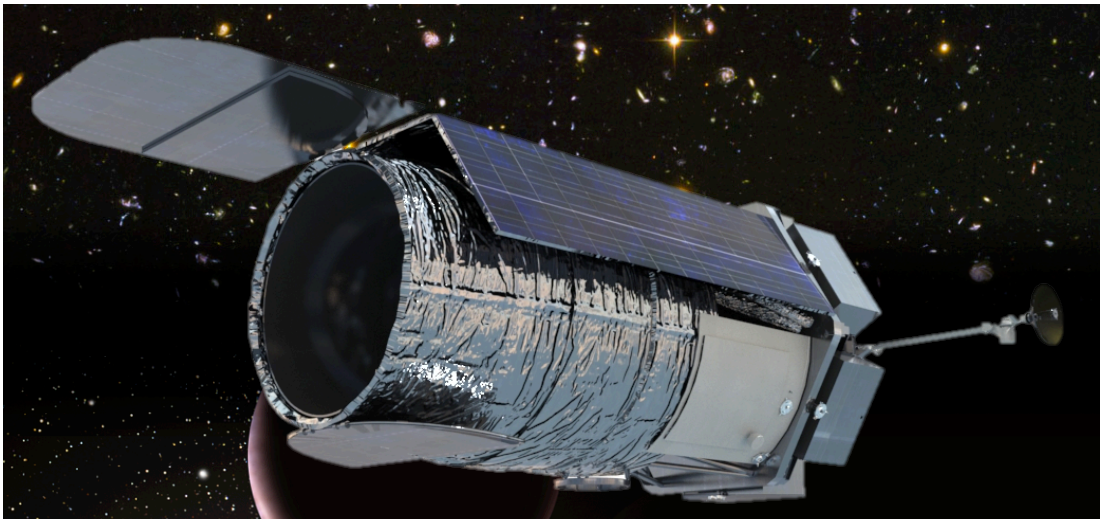
# Recommendations of the “Rocky III” DOE/HEP report (Albrecht et al, 2012)

1. Advanced wide-field spectroscopic survey in time frame roughly between DES and LSST (& Euclid/WFIRST)
  - Stage IV BAO/RSD information
  - Provide calibration data for systematic error mitigation to improve dark-energy constraints from photometric surveys like DES & LSST (in particular, helps WL & CL)
2. Advance SN technique to Stage IV
  - Clearest path: DOE participation in SNe at high-redshift from space (example: DOE-led modest upgrade to WFIRST)
  - Explore vigorously ground-based alternatives (R&D effort for near-IR technology and sky-line suppression)
3. Pilot studies to generate new ideas for the future
  - Deep spectroscopic calibration data needed for LSST. Pilot study to determine exact needs and how to meet them.
  - Pilot studies combining theory and targeted observations to chart an effective modified gravity program to study transition to modified gravity.

In the next 10-15 years, can expect measurements of:

- $w$  (or  $w_{\text{pivot}}$ ) to 0.01 (incl systematics)
- $d(z)$ ,  $\text{growth}(z)$  in bins out to  $z=2-3$
- parametric DE vs MG consistency tests

e.g. WFIRST



# Can we distinguish between DE and MG?

(Usual answer:) Yes; here is how:

- In standard GR,  $H(z)$  determines distances **and** growth of structure

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi\rho_M\delta = 0$$

- So check if this is true by measuring separately

**Distances**

(as known as kinematic probes)  
(a.k.a. 0<sup>th</sup> order cosmology)

Probed by SN Ia, BAO, CMB,  
weak lensing, cluster abundance

**Growth**

(a.k.a. dynamical probes)  
(a.k.a. 1<sup>st</sup> order cosmology)

Probed by galaxy clustering,  
weak lensing, cluster abundance

(Actually...) Not without assuming that DE  
has no e.g. anisotropic stress

$$G_{\mu\nu} + X_{\mu\nu} = 8\pi GT_{\mu\nu} \quad \text{vs.} \quad G_{\mu\nu} = 8\pi GT_{\mu\nu} - X_{\mu\nu}$$

# What if gravity deviates from GR?

For example:

$$H^2 - F(H) = \frac{8\pi G}{3}\rho, \quad \text{or} \quad H^2 = \frac{8\pi G}{3} \left( \rho + \frac{3F(H)}{8\pi G} \right)$$



Modified gravity

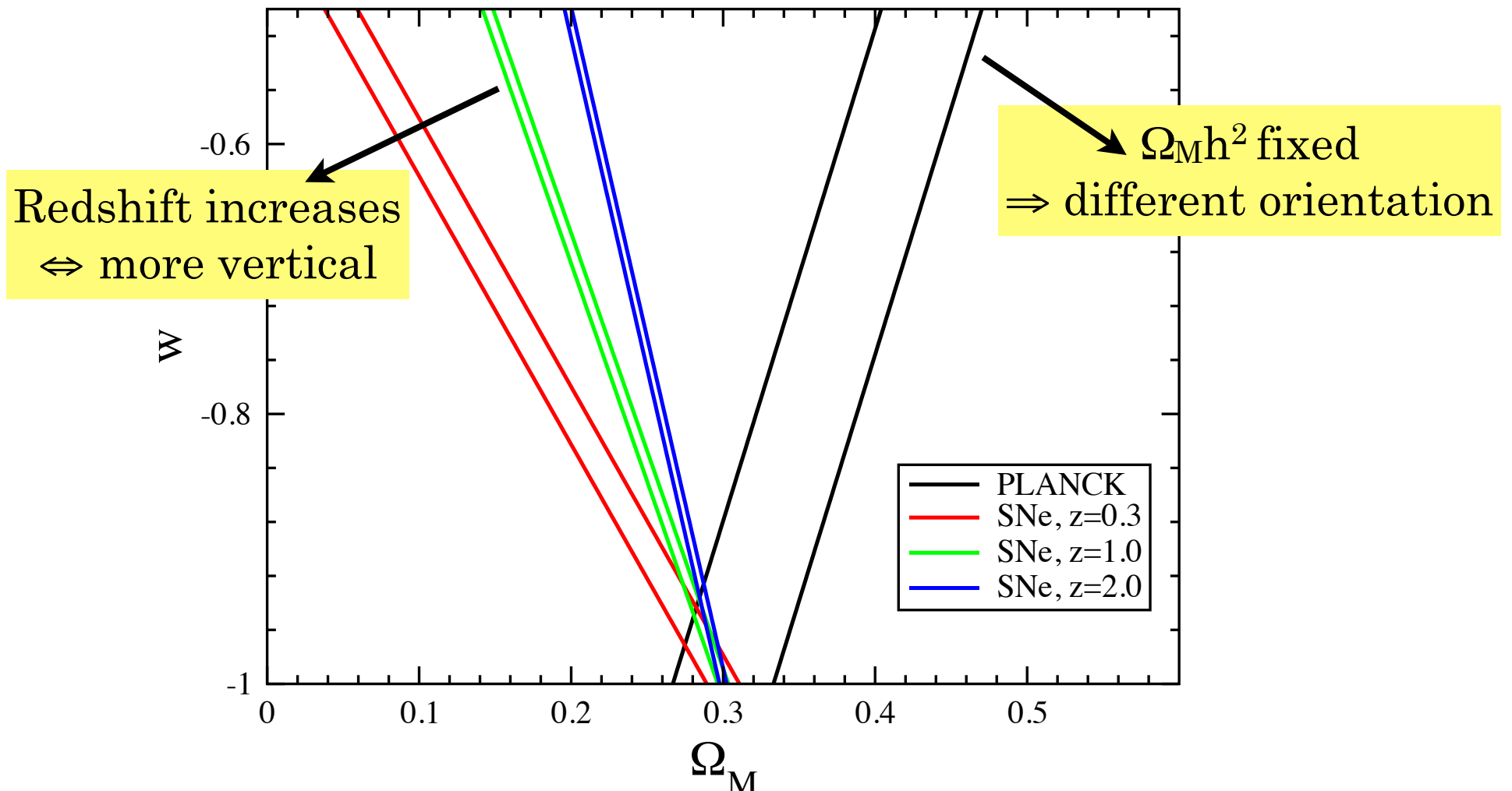


Dark energy

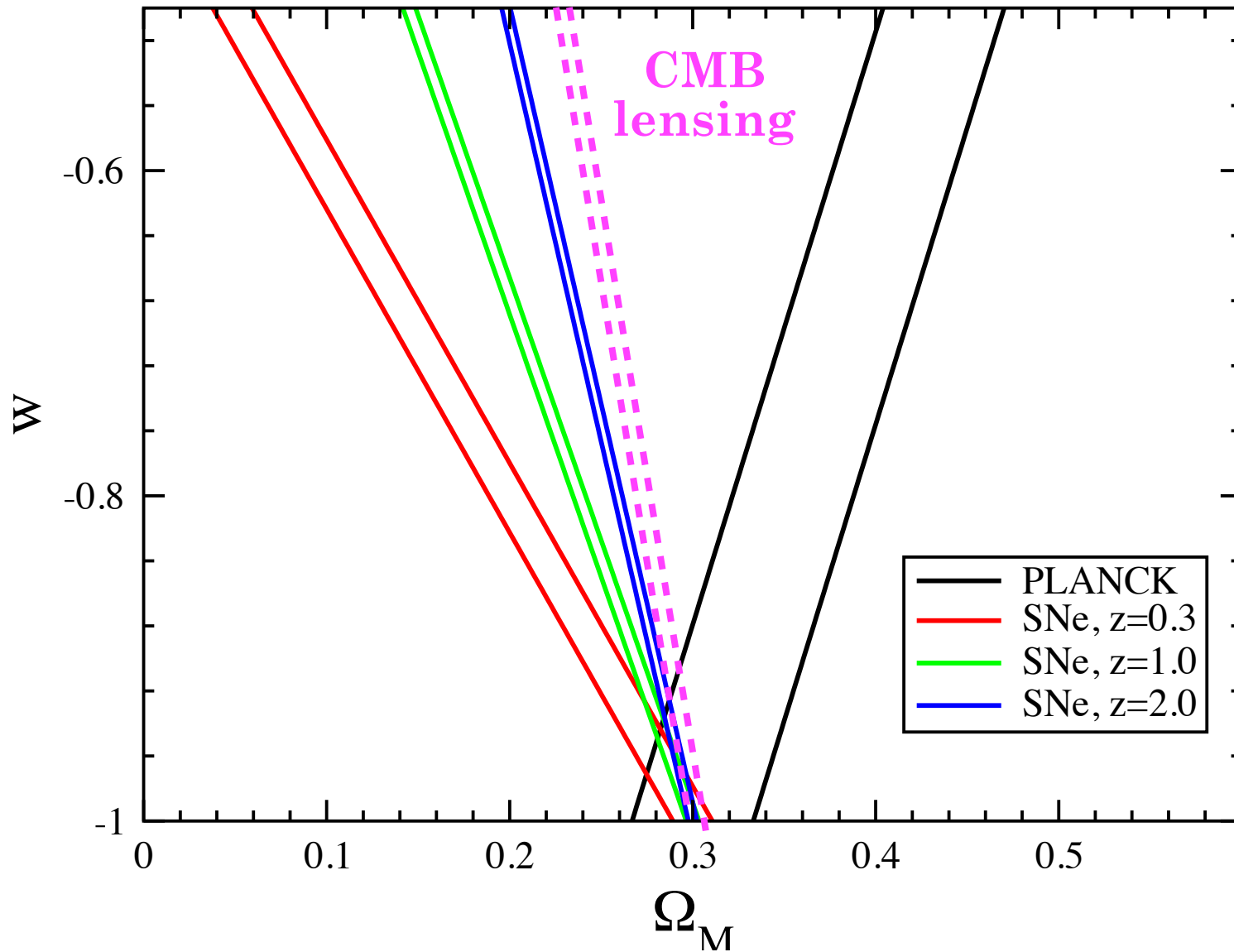
Notice: there is **no way** to distinguish these two possibilities just by measuring expansion rate  $H(z)$ !

$D_A(z)$  with  $\Omega_M h^2$  fixed is basically the “CMB shift parameter”  $R$

$$R = \sqrt{\Omega_M h^2} \int_0^{z_*} \frac{dz'}{H_0 \sqrt{\Omega_M (1+z')^3 + (1-\Omega_M)(1+z')^{3(1+w)}}$$



# CMB Lensing gives $D_A(z \sim \text{few})$

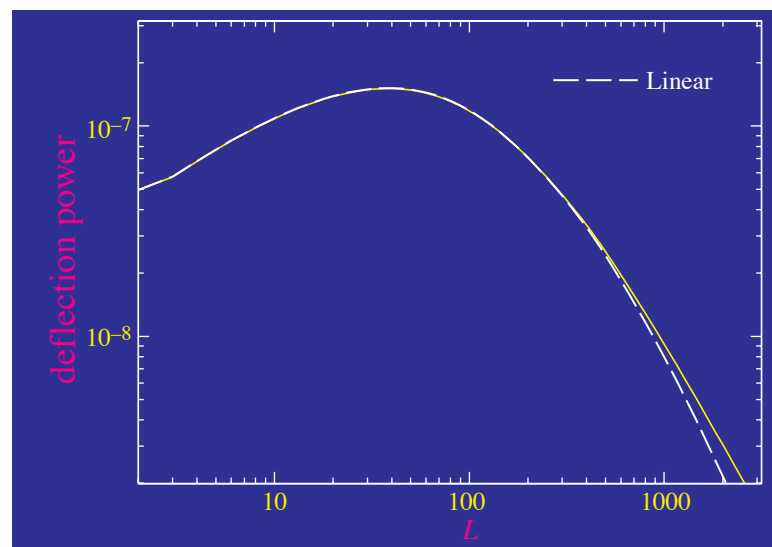


[Recall, CMB lensing additionally carries info about power spectrum  $P(k)$ ]

# Lensing potential:

$$\phi(\hat{\mathbf{n}}) = -2 \int_0^{z_{\text{rec}}} \frac{dz}{H(z)} \Psi(z, D(z)\hat{\mathbf{n}}) \left( \frac{D(z_{\text{rec}}) - D(z)}{D(z_{\text{rec}})D(z)} \right)$$

Angular power  
of potential:



Wayne Hu

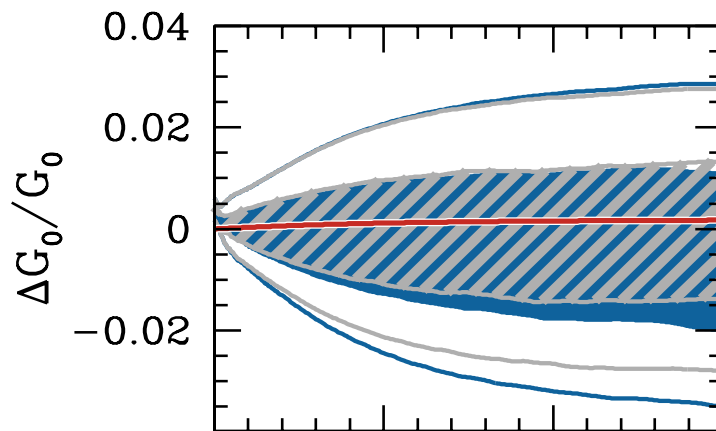
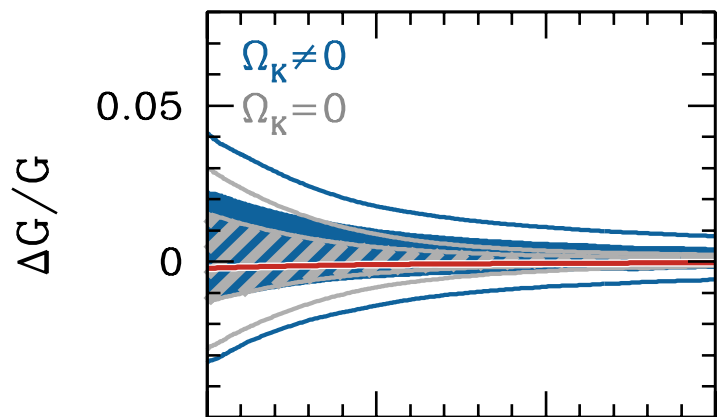
$$C_{\ell}^{\phi\phi} = \frac{8\pi^2}{\ell^3} \int_0^{z_{\text{rec}}} \frac{dz}{H(z)} D(z) \left( \frac{D(z_{\text{rec}}) - D(z)}{D(z_{\text{rec}})D(z)} \right)^2 P_{\Psi}(z, k = \ell/D(z))$$

geometry

DM clustering

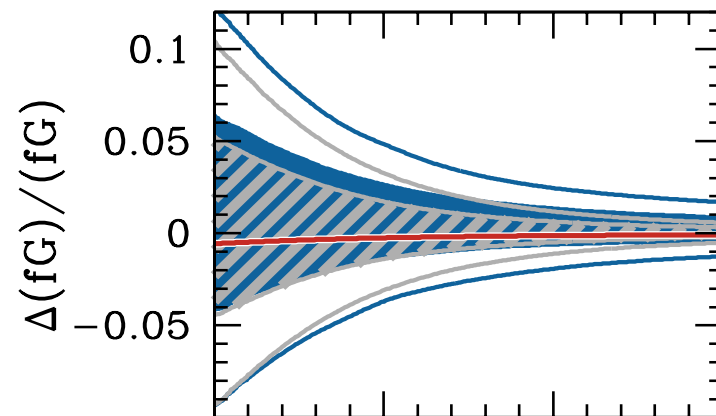
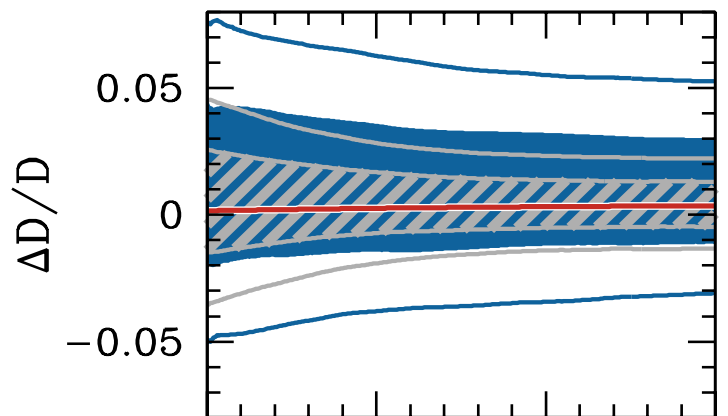
*Current data* **ΛCDM** predictions - flat or curved

Growth  
to  $z=1000$



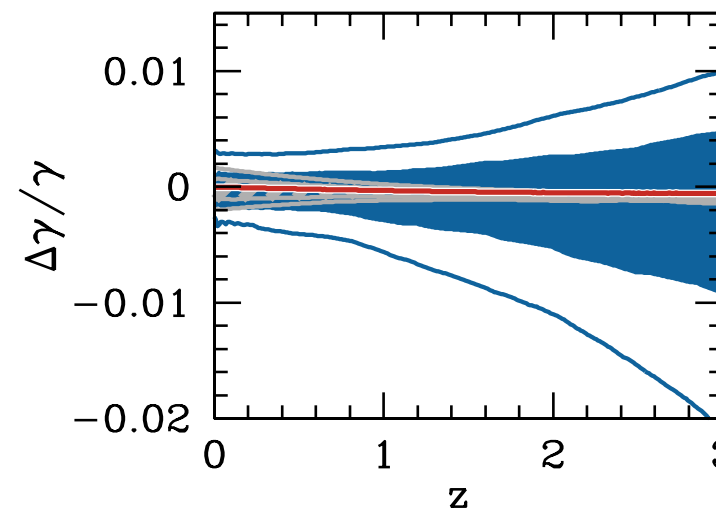
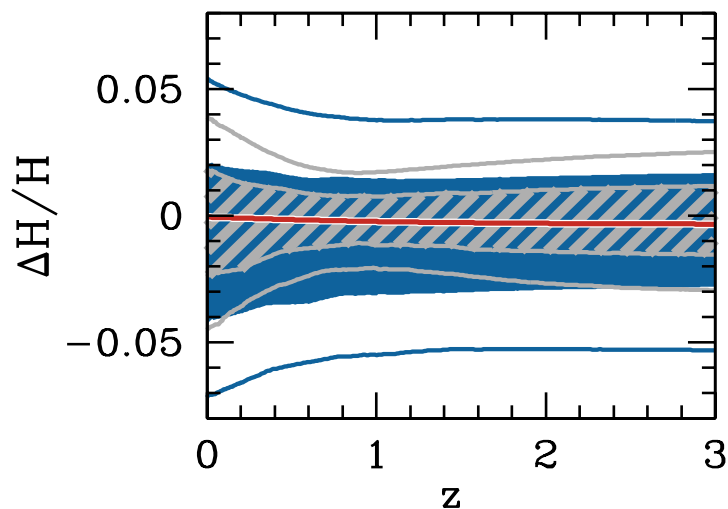
Growth  
to  $z=0$

Distance



$f \times G$

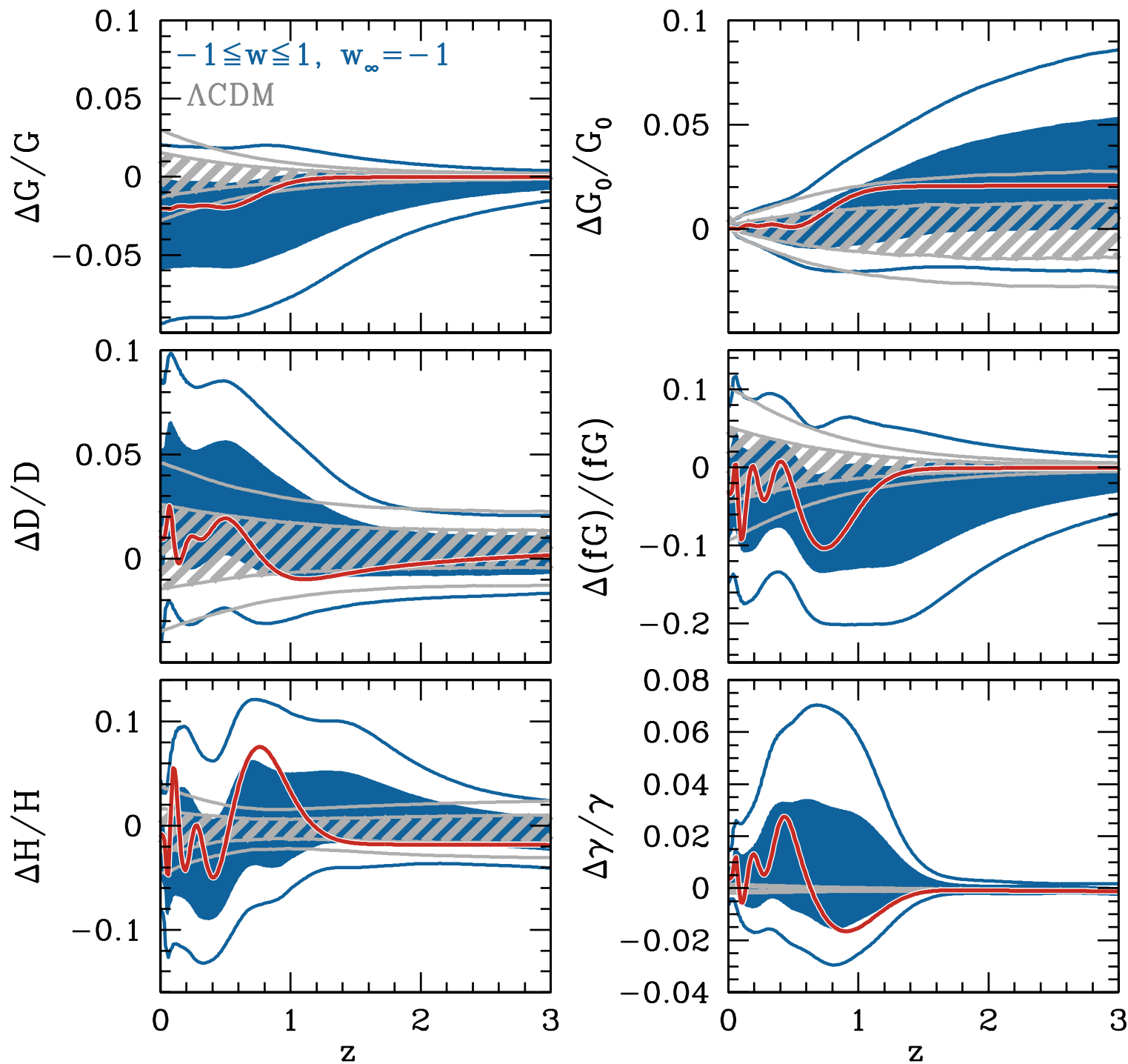
Hubble  
parameter



Growth index



Current data Quintessence predictions (flat, no Early DE)



Future data

# ΛCDM predictions (flat or curved)

Grey: flat

Blue: curved

D, G to <1% everywhere  
H(z=1) to 0.1% for flat ΛCDM

