

# Problem Set 1

## Physics 520

Fall 2005  
L. Sander  
9/8/05 due 9/15/05

1. Calculate the van der Waals' interaction between two H atoms in their ground state. Use the Hamiltonian for the two the single atoms as a reference:

$$\mathcal{H} = \sum_{i=1,2} p_i^2/2m - e^2/|\mathbf{r}_i - \mathbf{R}_i|$$

and the rest as a perturbation:

$$\delta\mathcal{H} = -e^2/|\mathbf{r}_1 - \mathbf{R}_2| - e^2/|\mathbf{r}_2 - \mathbf{R}_1| + e^2/|\mathbf{r}_1 - \mathbf{r}_2| + e^2/|\mathbf{R}_1 - \mathbf{R}_2|$$

See Ashcroft and Mermin, Schiff, *Quantum Mechanics*. Assume that  $r_i \ll d$ , where  $d$  is the distance between the nuclei. Consider only the first excited state of H in your perturbation theory; do not use the trick in Schiff's book which involves using an approximate summation over all states.

2. a.) He is a liquid sufficiently near  $T=0$ . Explain why. (Hint: estimate the zero point kinetic energy due to the localization of He atoms in a cell of size  $\sigma = 2.56$  Angstrom. The energy parameter is  $\epsilon = 1.4 \times 10^{-15}$  ergs.). b.)  $H_2$  is a solid. However,  $H_2$  is lighter and has bigger zero point fluctuations. Explain.

3. Argon has  $\epsilon = 1.7 \times 10^{-14}$  ergs and  $\sigma = 3.4$  Angstrom. Find the equilibrium distance between atoms and the binding energy per atom for (hypothetical) simple cubic Ar.

4. a.) When spheres are as closely packed as possible they form either a fcc lattice or a hcp crystal. Prove that when spheres are packed they fill the following percentages of the available volume (the packing fraction).

simple cubic	52%
body-centered cubic	68%
fcc	74%

b.) Find the  $c/a$  ratio such that hcp is close-packed. What is the packing fraction?

5. Show that no two dimensional Bravais lattice can have a 5 or 7-fold axis of rotation, i.e., no axis such that a rotation by  $2\pi/5$  or  $2\pi/7$  leaves that lattice invariant. See AM p. 129 for a hint.