

# The c-M relation: observations & simulations

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Reconciling extremely  
different concentration-mass  
relations

*Meneghetti & Rasia (to be sub.)*

X-ray c-M relation:  
understanding the bias

*Rasia, Mazzotta, Ettori,  
Borgani, Meneghetti (to be  
sub.)*

# Apple to Apple is not enough!

Comparing apple to apple is not enough...



We need to pay also attention at the analysis procedure!



Same apple BUT the cooked one has more concentration of sugar



# NFW Navarro, Frenk, White

1996 “The Structure of Cold Dark Matter Halos”

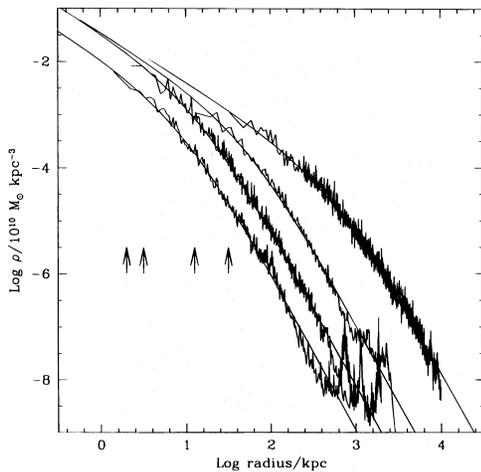


FIG. 3.—Density profiles of four halos spanning 4 orders of magnitude in mass. The arrows indicate the gravitational softening,  $h_s$ , of each simulation. Also shown are fits from eq. (3). The fits are good over two decades in radius, approximately from  $h_s$  out to the virial radius of each system.

$$\rho(x) = \frac{\rho_s}{x(1+x)^2}, x = r/r_s$$

$$\rho_s = \frac{\rho_{cr} \Delta}{3} \frac{c}{\ln(1+c) - c/(1+c)}$$

$$c_\Delta = r_\Delta / r_s$$

$$M(< x) = 4\pi\rho_s r_s^3 [\log(1+x) - x/(1+x)]$$

$$M_* = 3.3e13 M_{sun}$$

$$C_{200} = R_{200} / r_s$$

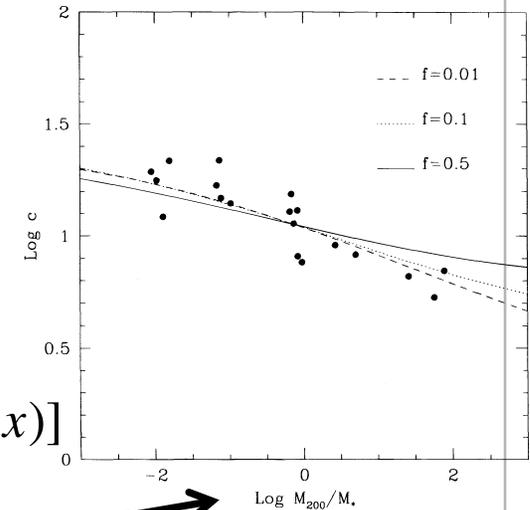
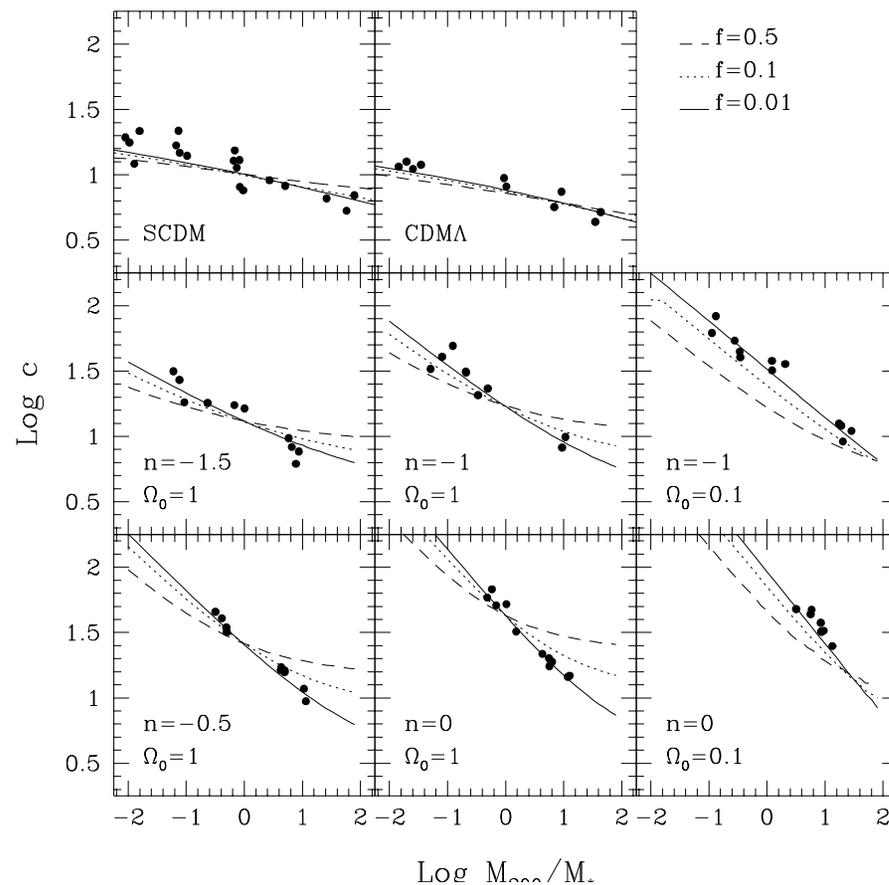


FIG. 8.—Concentration  $c$  as a function of the mass of the halo. The curves show the mass-concentration relation predicted from the formation times of halos. All curves are as in Fig. 7 and have been normalized so that they cross at  $M_{200} = M_*$ .

# NFW Navarro, Frenk, White

1997 “Universal density profile from hierarchical clustering”

- Groups formed when the universe was denser  $\rightarrow$  higher concentration



# 1<sup>st</sup> Comparison: between two theoretical papers

## PROBLEM

- Duffy et al.08 ([D08](#)), Prada et al.12 ([P12](#))
- Both use DM-only simulations
- Have a very similar cosmological model

## BUT

- C-M relation differ in NORMALIZATION (Prada et al. 12 is higher)
- And in shape (Prada et al. 12 presents an upturn at high masses)

# D08 vs P12

## Methods and binning

- D08: Method  
STANDARD: density profiles fitting by NFW between  $[0.05-1] R_{\text{vir}}$

- D08: Bin in Mass

- P12 Method through circular velocity

$$V_{\text{max}} = \max[(GM/R)^{1/2}]$$

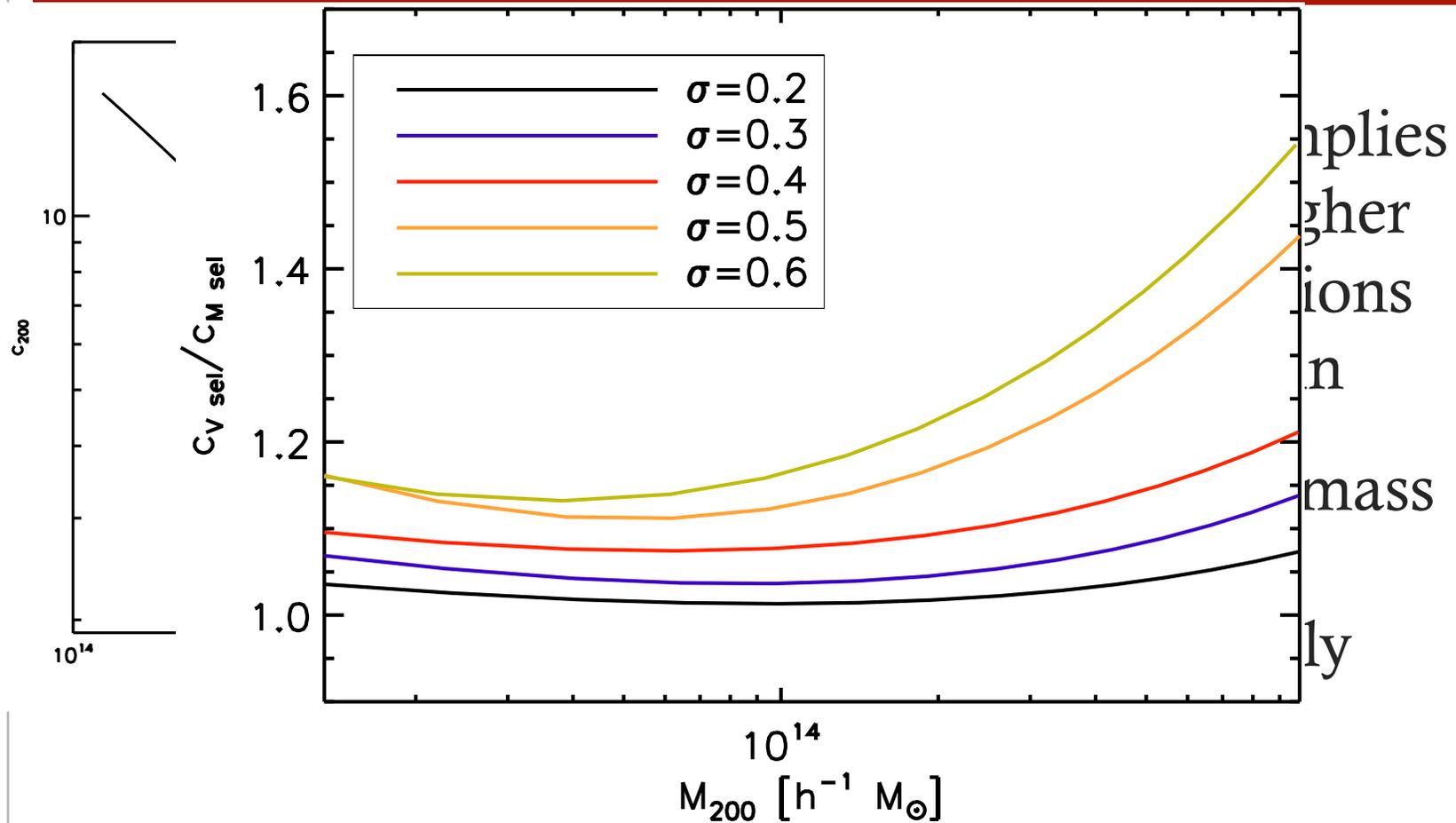
$$V_{200} = (GM_{200}/R_{200})^{1/2}$$

$$\frac{V_{\text{max}}}{V_{200}} = \sqrt{\frac{0.216c}{f(c)}} = F(c)$$

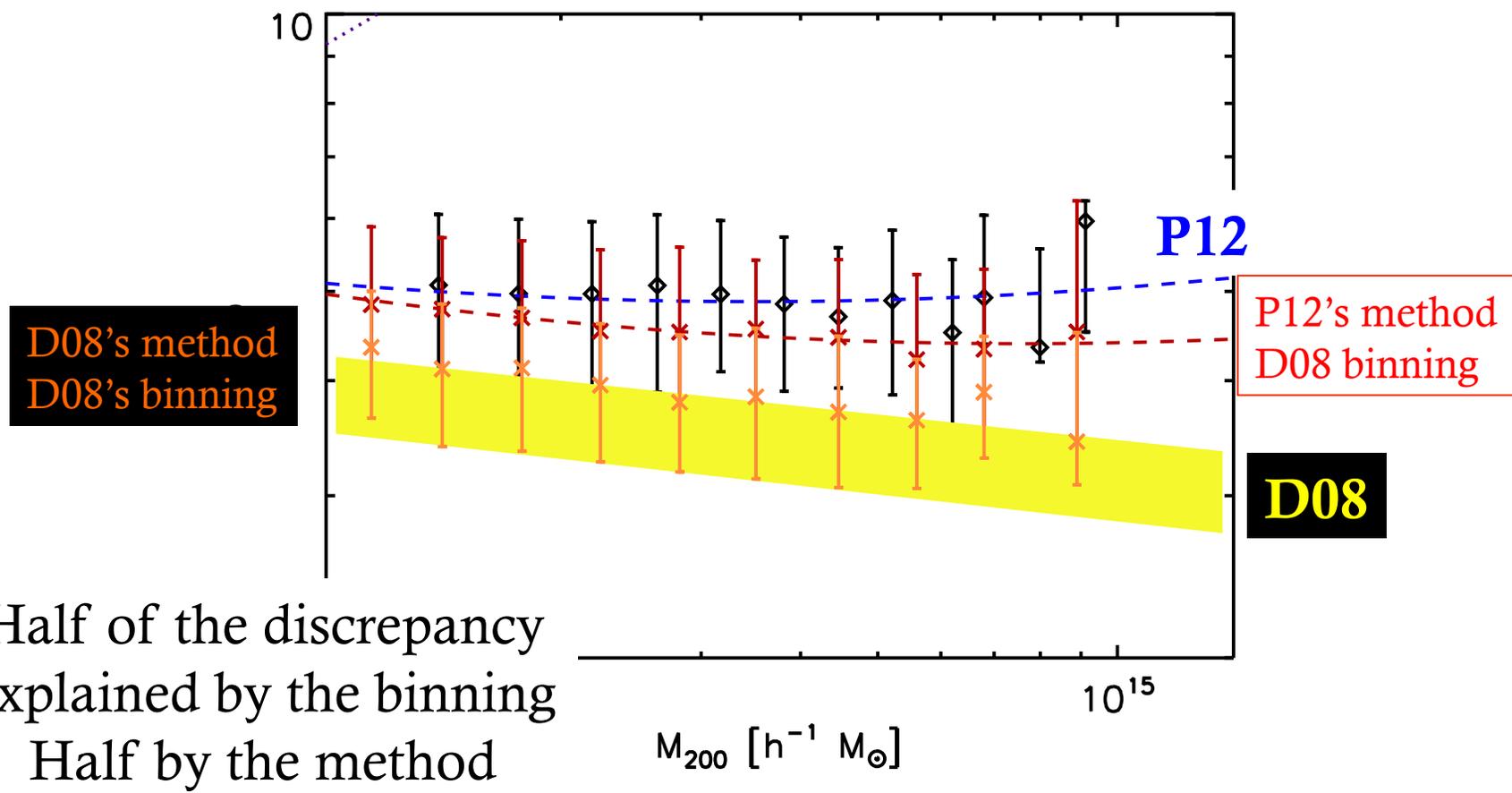
$$f(c) = \ln(1+c) - c/(1+c)$$

- P12: Bin in Velocity

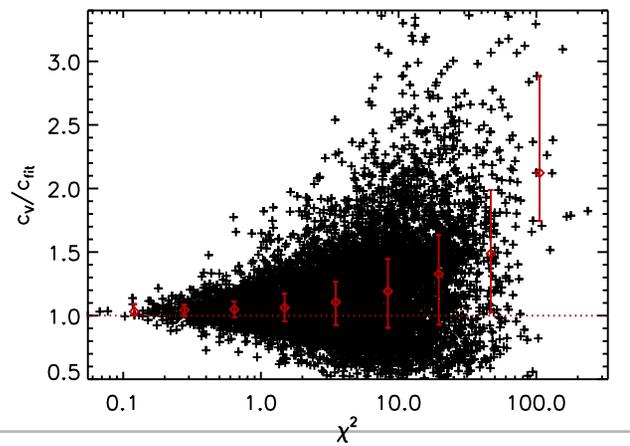
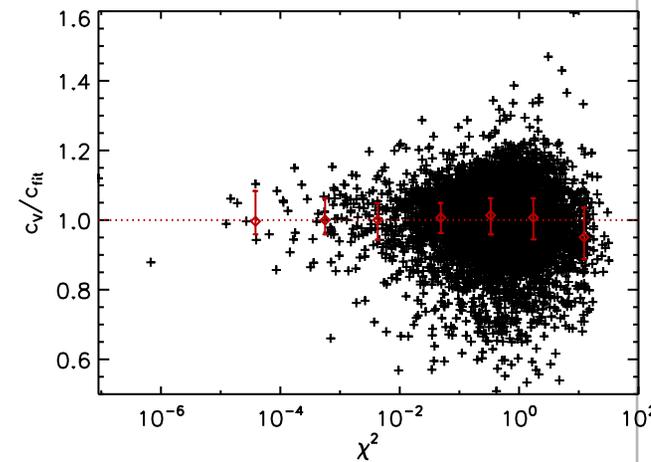
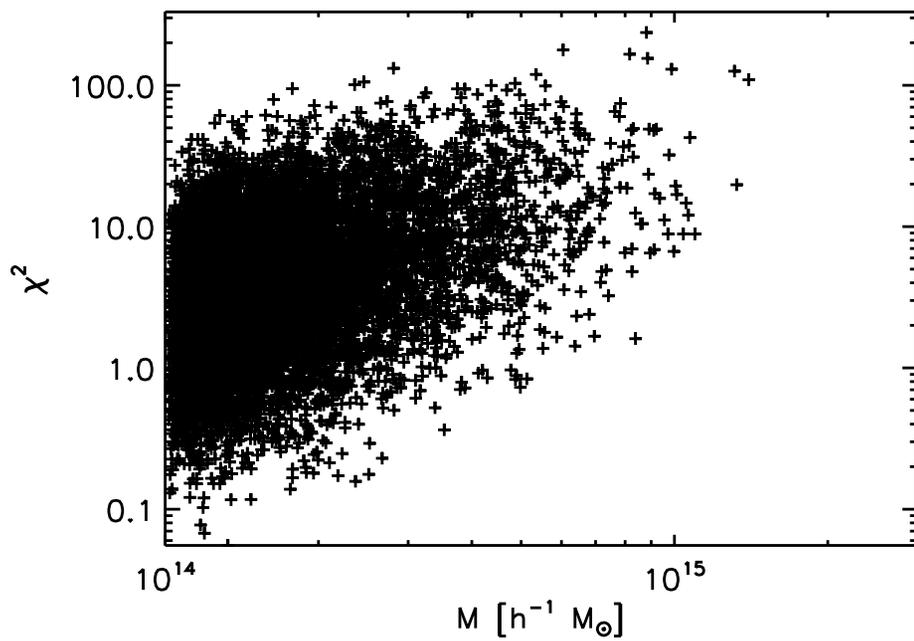
# BINNING



# METHOD: MultiDark simulations

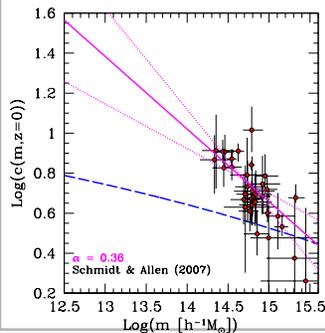
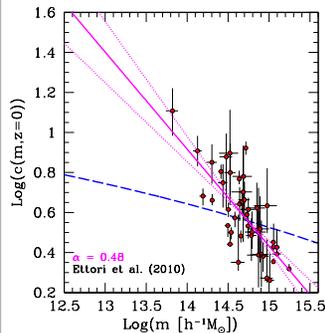
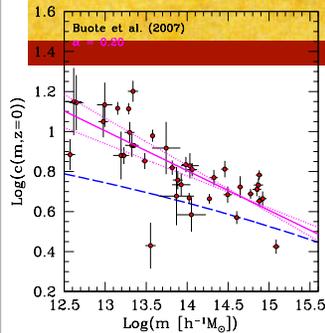


# WHY?



# 2nd Comparison: X-ray and simulation

$$c = c_0 \left[ \frac{M}{M_0} \right]^\alpha$$



- *Pointecouteau et al. 05, Vikhlinin et al. 06* agree with simulations.
- *Buote et al. 2007, Schmidt & Allen 2007, Ettori et al. 2010* claimed agreement within the errors but...

*Fedeli 2012*

## *Problem*

The relation is steeper in observation than in theory.

B07:  $\alpha = -0.20$

E10:  $\alpha = -0.48$

SA07:  $\alpha = -0.36$

Gao et al. 08

$\alpha = -0.10$

# c-M relation: different approaches

## SIMULATIONS

## OBSERVATIONS

- NFW fit to 3D profile
- Fit done from the central regions to the virial radius or beyond
- Most work based on DM-only simulations
- In cosmological boxes selection based on M

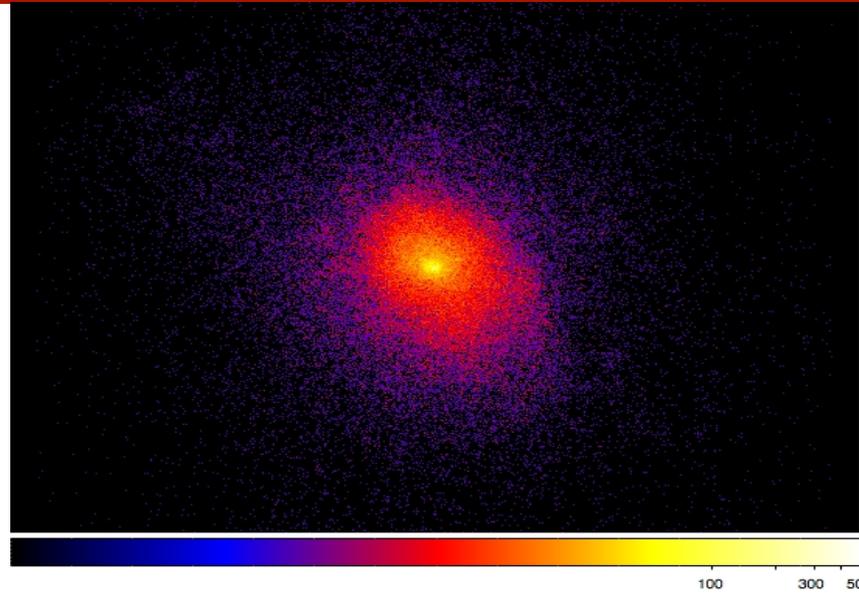
- Information is projected
- Radial range is determined by the S/N or field of view
- The real Universe has baryons!
- Observational selection function: cut in  $L_X$  (in the best scenario)

RADIAL RANGE  
BARYONS  
SELECTION FUNCTION

# SAMPLE

52 simulated clusters  
with 4 different physics  
(*Fabjan, Borgani, ER, et al. 2011, ER et al. 2012*):

- DM-only
- NR (no-radiative)
- CSF (cooling-star formation-feedback)
- AGN



Synthetic X-ray catalogue (*ER et al. 2012, NJP, 14, 501\**):

20 CSF clusters processed through X-MAS (*Gardini, ER et al. 2004, ER et al. 2008*) to create Chandra-like observations

\*(Video Abstract: [iopscience.iop.org/1367-2630/14/5/055018](http://iopscience.iop.org/1367-2630/14/5/055018))

# STANDARD

## FITTING

## PROCEDURE

Typical SIM radial range: from [0.07-1.4] of  $R_{200}$  ( $=[0.05-1] R_{\text{vir}}$ )

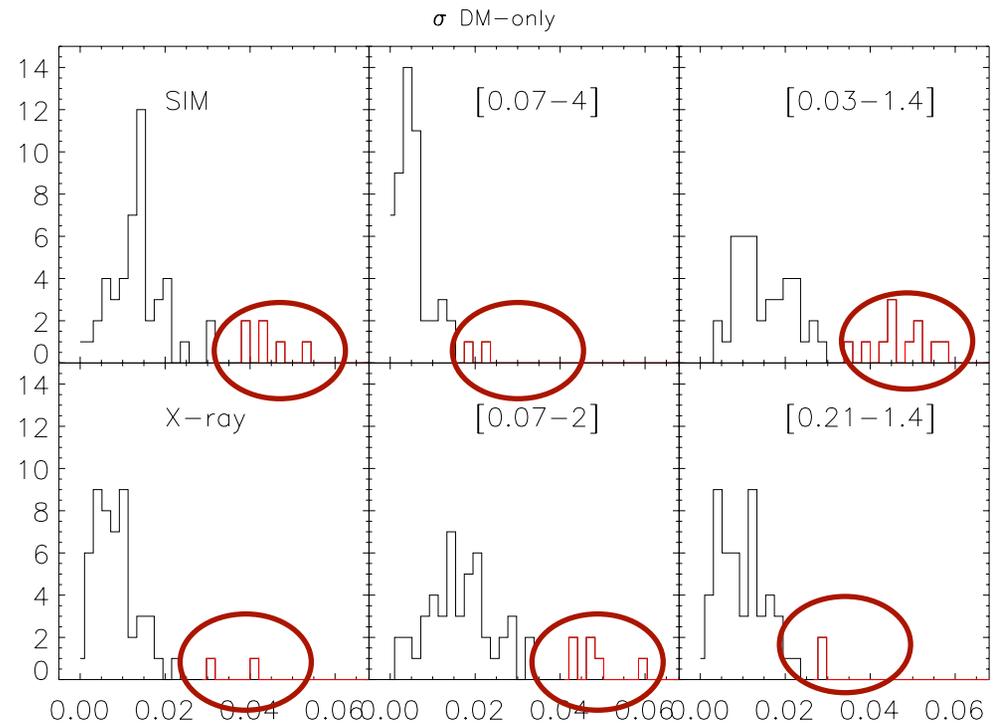
Halos presenting large residuals have been eliminated

$$c = c_0 \left[ \frac{M}{M_0} \right]^\alpha$$

$$M_0 = 5 \times 10^{14} M_{\text{sun}}/h$$

## Residuals

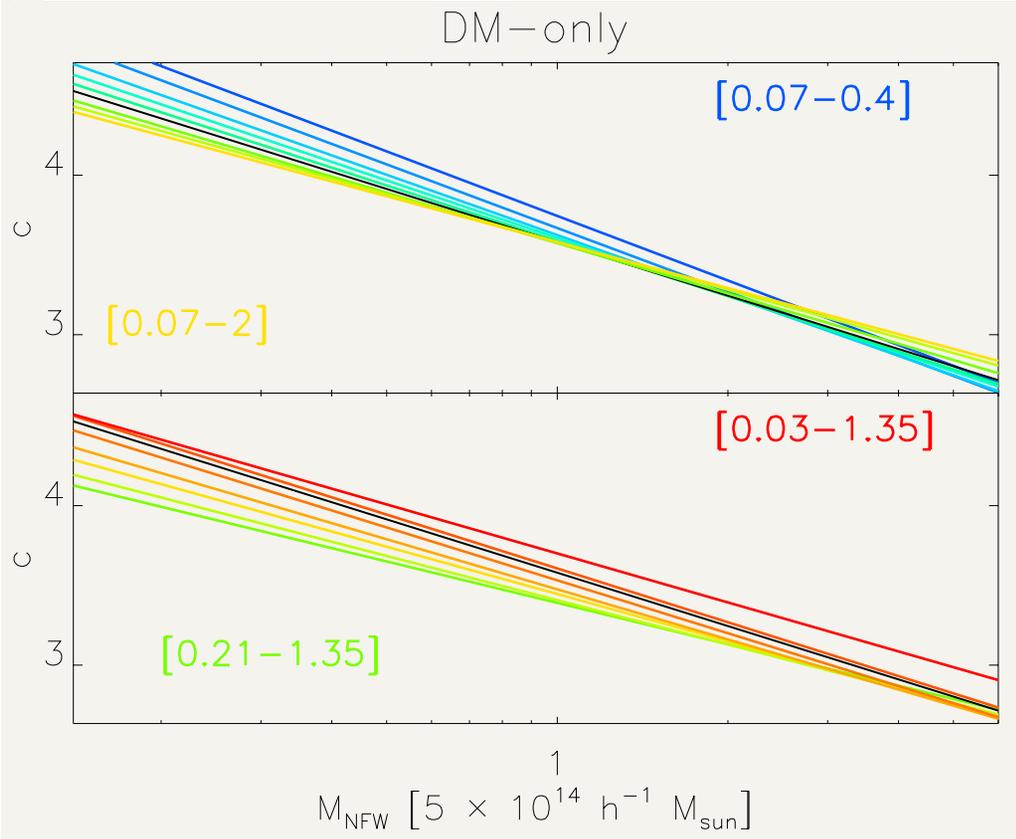
$$\sigma^2 = \frac{\sum_1^{N_{bin}} [\log(\rho_i) - \log(\rho_{NFW})]^2}{N_{bin}}$$



Max slope = -0.2  
+20%  
Min slope = -0.12  
-15%

# RADIAL RANGE (DM ONLY)

$$c = c_0 \left( \frac{M}{M_0} \right)^\alpha$$



~ Black line = SIM  
radial range

[0.07-1.4]  $R_{200}$

EXTERNAL RADIUS:

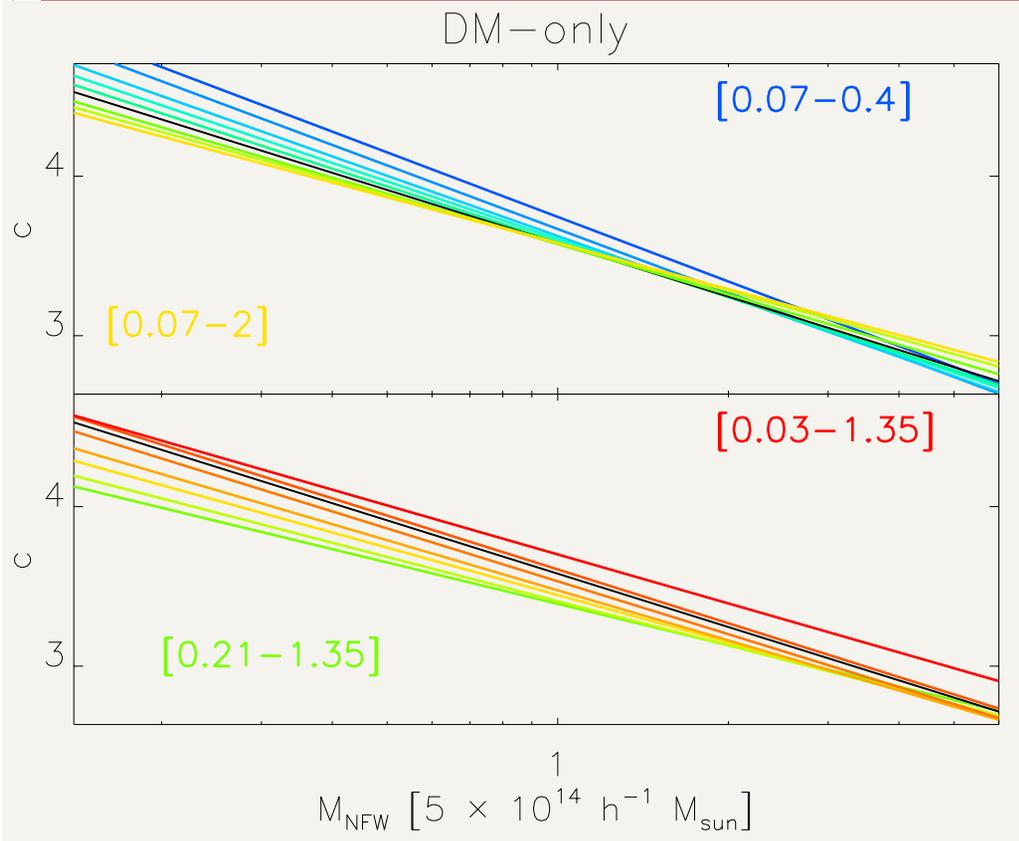
~ X-ray has a steeper  
slope

~ the difference is  
caused by the 17 least  
massive systems

Max slope = -0.2  
 +20%  
 Min slope = -0.12  
 -15%

# RADIAL RANGE (DM ONLY)

$$c = c_0 \left( \frac{M}{M_0} \right)^\alpha$$



~ Black line = SIM  
 radial range [0.07-1.4]  
 $R_{200}$

INTERNAL RADIUS:  
 ~ modifying the inner  
 radius changes the  
 normalization

~ X-ray (to 50 kpc) and  
 strong-lensing results  
 might have an higher  
 normalization

$$c = c_0 \left( \frac{M}{M_0} \right)^\alpha$$

# BARYONS

RESULTS  
considering only  
clusters with a  
good NFW fit

ICM PHYSICS:

RED: CSF

GREEN: NR

MAGENTA: AGN

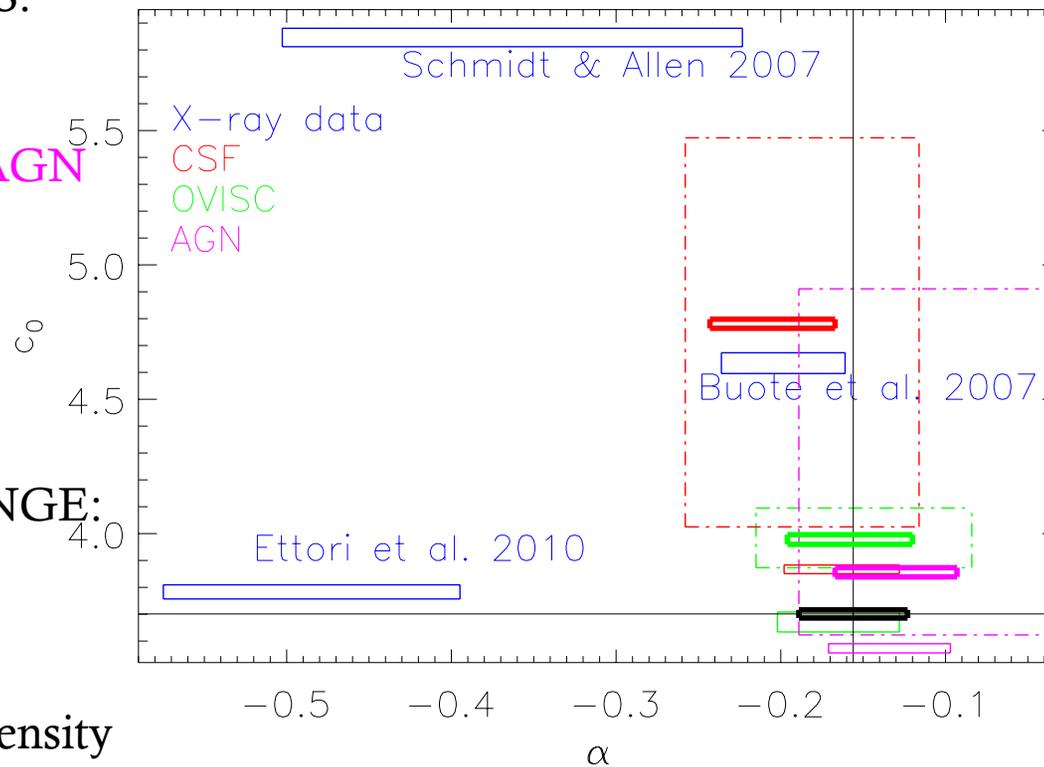
RADIAL RANGE:

SIM

[0.07-1.4]  $R_{200}$

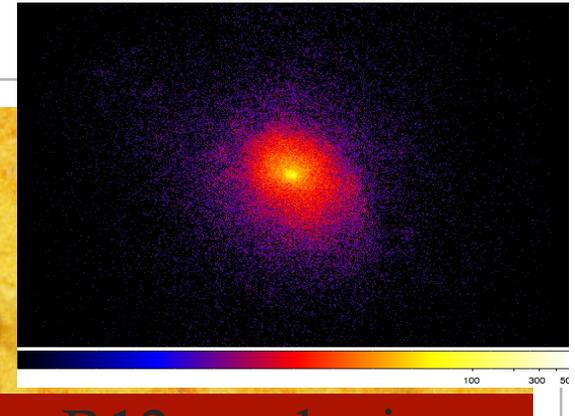
BOLD: total density

THIN: dm density

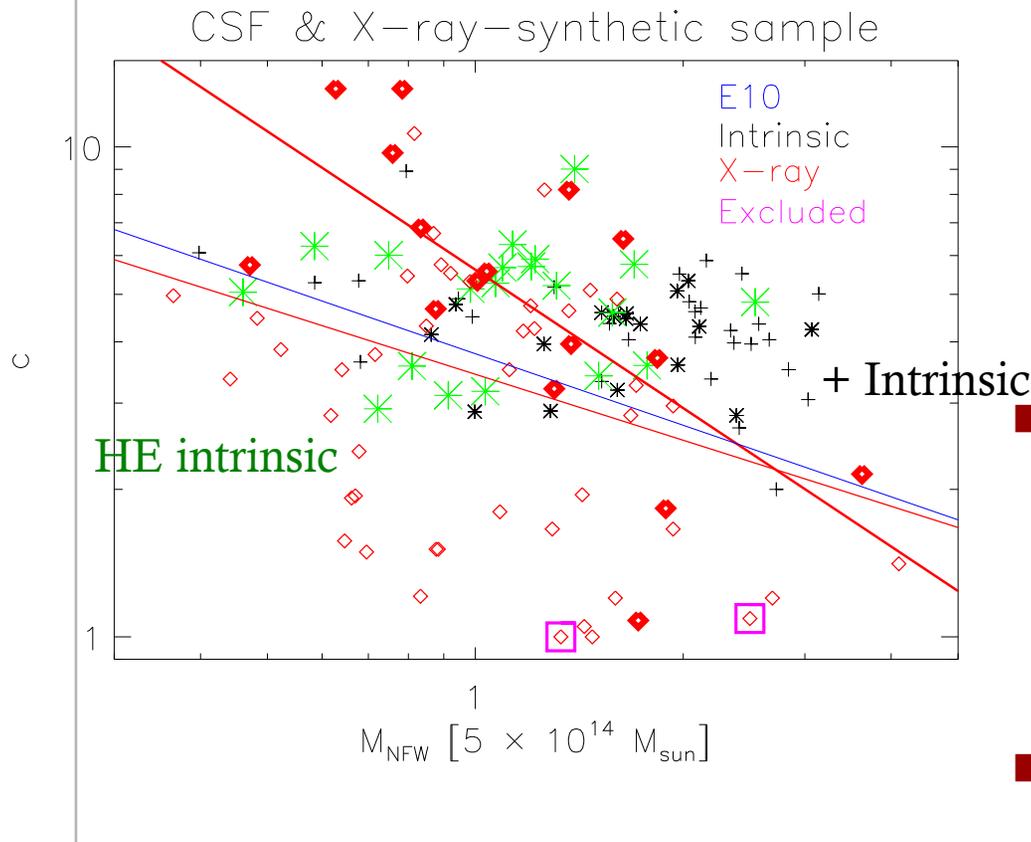


- 1) Normalization is higher with baryons
- 2) Slope is higher for total CSF
- 3) Slopes and normalizations of the only DM component agree better within each other.

# X-RAY



## X-ray + Hydrostatic Equilibrium



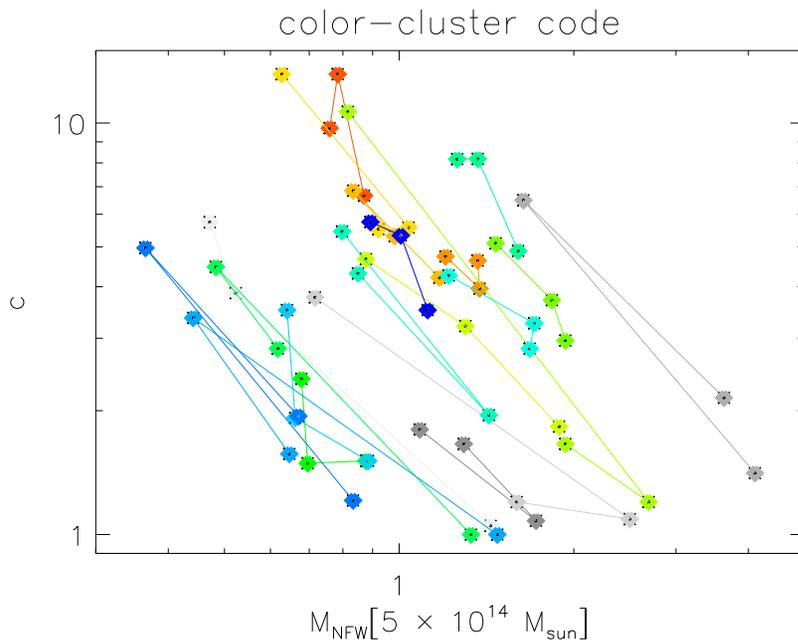
- From the R12 synthetic catalogue (60 X-ray images), we perform the X-ray analysis and computed the mass profiles the we fit with the NFW model

- The HE alone (intrinsic) does not explain the large increase of the scatter and the steepening of the slope

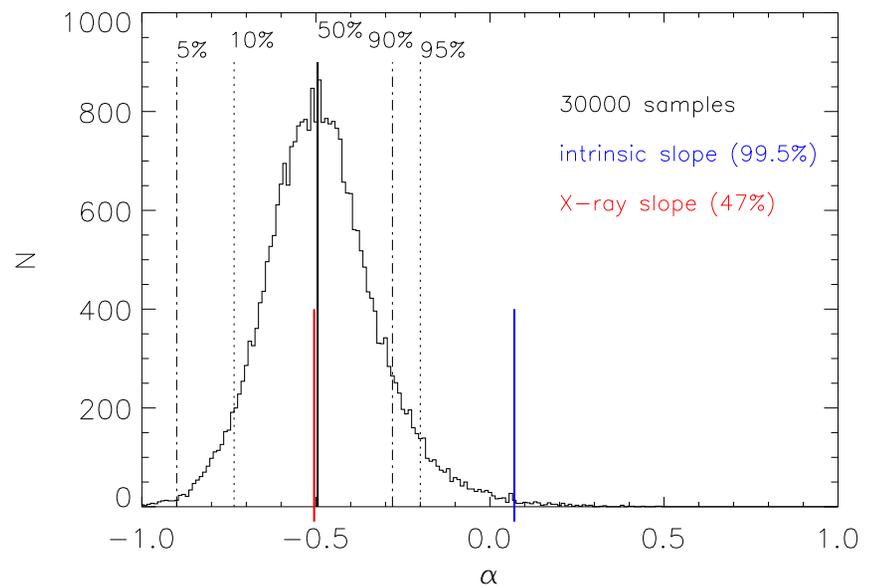
- It is the complete X-ray analysis that steepen the  $c$ - $M$

# TESTING our sample

The 60 X-ray images for the 20 clusters

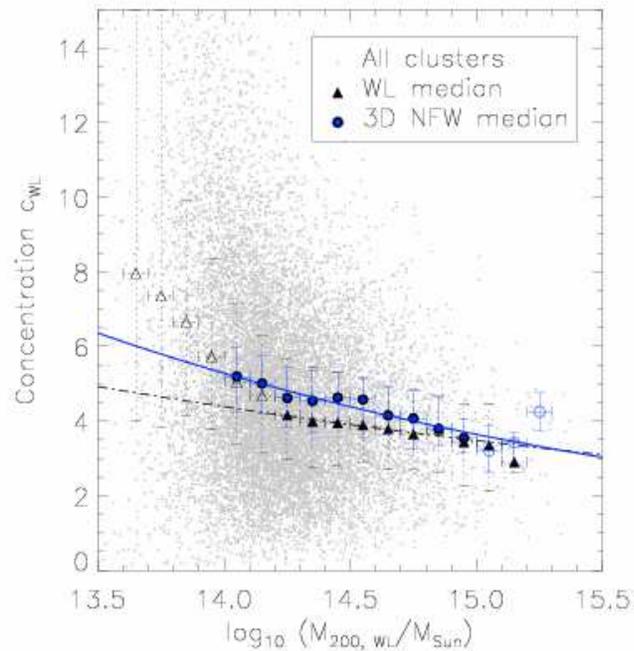


30000 realizations (combinations of the 20 clusters observed from random directions)

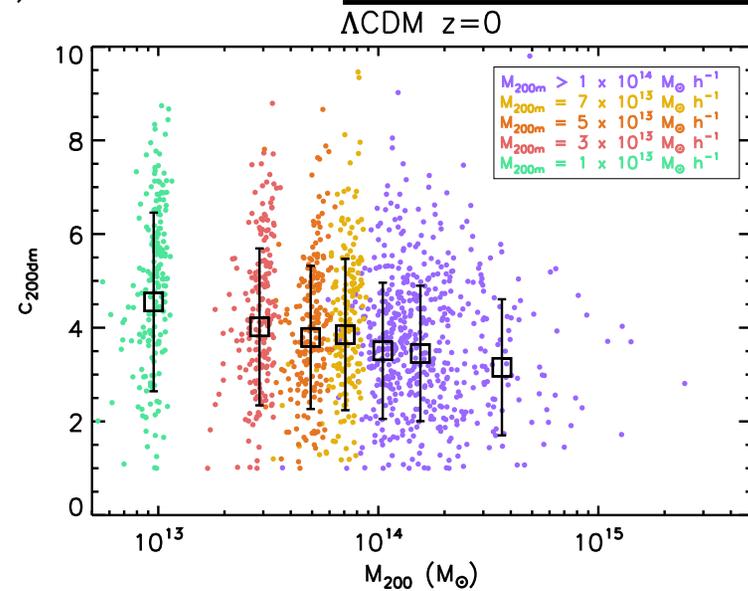


# X-ray SELECTION FUNCTION

Selection Function influences scaling-relation results (*Nord et al. 08, Pratt et al. 2009, Allen et al. 2012*), what about the c-M relation?

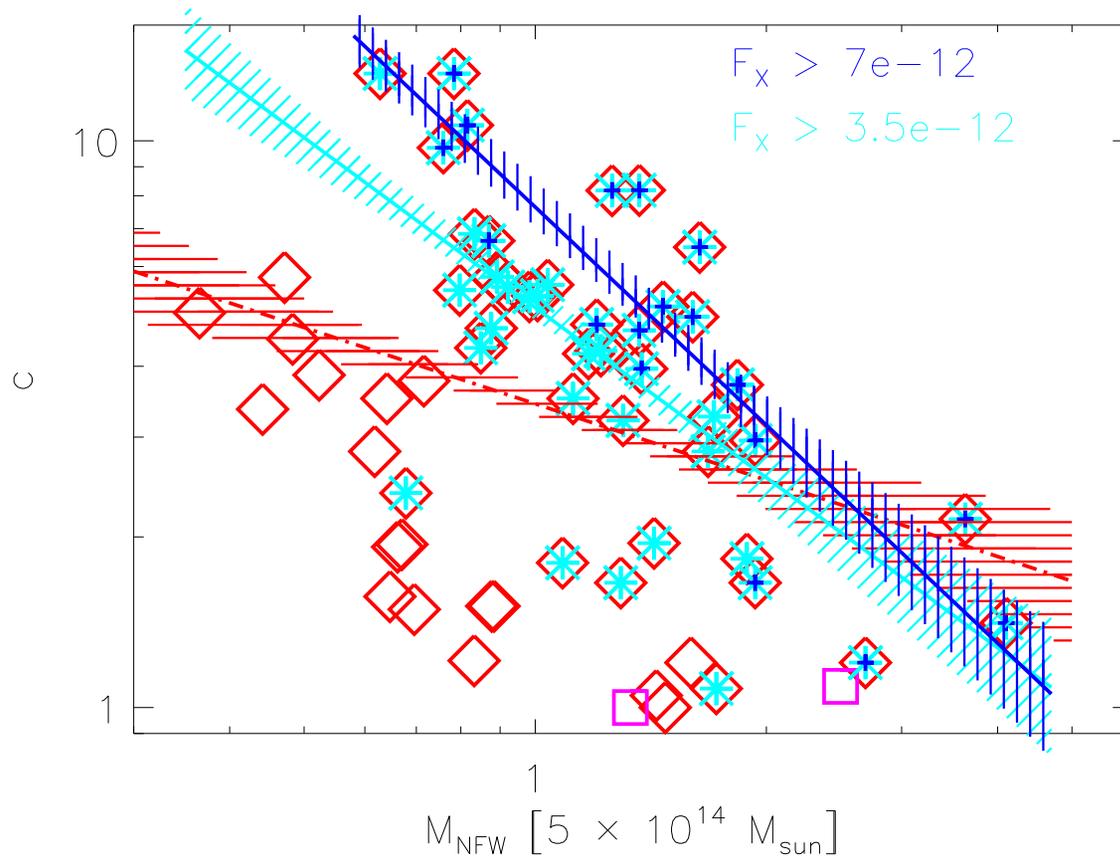
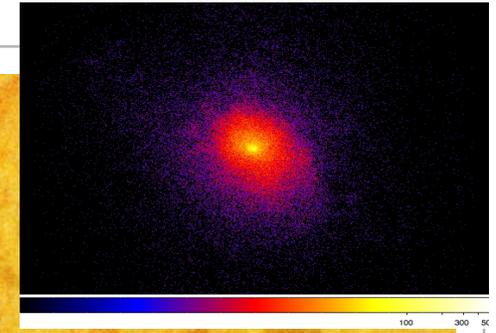


Bahe et al. 2012



De Boni et al. 2012

# X-ray SELECTION FUNCTION



$L_X > 1.4 \cdot 10^{45} \text{ erg/s}$   
 $L_X > 7 \cdot 10^{44} \text{ erg/s}$

If we select our sample on the basis of the X-ray emission we tend to have more concentrated halo at fixed mass

# CONCLUSIONS

- Comparisons NEEDS to be fair!
- If approaches are INTRINSICALLY different a bias in the comparison is very likely. This is the case for the c-M relation.
- D08 and P12 differences in normalization and shape are fully explained by understanding their procedure
- As for the X-ray simulations comparison: small part of the gap is explained by ICM physics and radial range but the majority has to be ascribed to the different methodology and selection functions.
- Radial range: lowering the external fitting radius => slope reduced
- Radial range: decreasing the central excision => normalization increased
- Baryons => all physics: normalization increased
- X-ray approach and Selection function=> slope increased

