



PROPOSITION 6: TIEBREAKER-BREAKER ROUND

Name: _____

Team ID: _____

INSTRUCTIONS

1. Do not begin until instructed to by the proctor.
2. You will have 10 minutes to solve the problem.
3. When you would like to submit your answers, please inform your proctor.
4. **Your score will be the number of correct answers, with ties broken by time of submission.**
5. No calculators or electronic devices are allowed.
6. All submitted work must be your own. You may not collaborate with anyone else during the individual round.
7. When time is called, please put your pencil down and hold your paper in the air. **Do not continue to write.** If you continue writing, your score may be disqualified.
8. Do not discuss the problems until all papers have been collected.
9. If you have a question or need to leave the room for any reason, please raise your hand quietly.
10. Good luck!



ACCEPTABLE ANSWERS

1. All answers must be simplified as much as reasonably possible. For example, acceptable answers include $\sin(1^\circ)$, $\sqrt{43}$, or π^2 . Unacceptable answers include $\sin(30^\circ)$, $\sqrt{64}$, or 3^2 .
2. All answers must be exact. For example, π is acceptable, but 3.14 or $22/7$ is not.
3. All rational, non-integer numbers must be expressed in reduced form $\pm\frac{p}{q}$, where p and q are relatively prime positive integers and $q \neq 0$. For example, $\frac{2}{3}$ is acceptable, but $\frac{4}{6}$ is not.
4. All radicals must be fully reduced. For example, $\sqrt{24}$ is not acceptable, and should be written as $2\sqrt{6}$. Additionally, rational expressions cannot contain radicals in the denominator. For example, $\frac{1}{\sqrt{2}}$ is not acceptable, and should be written as $\frac{\sqrt{2}}{2}$.
5. Answers should be expressed in base 10 unless otherwise specified.
6. Complex numbers should be expressed in the form $a + bi$, where both a and b are written in a form compliant with the rules above. In particular, no complex denominators are allowed. For example, $\frac{1+2i}{1-2i}$ should be written as $-\frac{3}{5} + \frac{4}{5}i$ or $\frac{-3+4i}{5}$.
7. If a problem asks for all solutions, you may give the answers in any order. However, no credit will be given if any solution is missing or any solution is given but not correct.
8. Angle measurements should be given in radians unless otherwise specified.
9. Answers must be written legibly to receive credit. Ambiguous answers may be marked incorrect, even if one of the possible interpretations is correct.



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1. Six people called A , B , C , D , E , and F want to sit around a circular table. A and B refuse to sit next to each other. How many valid seating arrangements are there?

1. 72

Solution: There are a total of $(6 - 1)! = 120$ total configurations to seat the six people around the circular table. However, we must subtract out the cases in which A and B sit next to each other. We can treat A and B as one person, multiplying by 2 to account for the cases of AB and BA , and so there are $2 \times (5 - 1)! = 48$ ways to arrange the six people such that A and B are together. Thus, there are $120 - 48 = \boxed{72}$ ways to arrange the six people such that A and B are not together.