

IV.C.3 - Ideal image detector - energy integrating type

From Lecture 05

- An ideal energy integrating detector will record a signal equal to the total energy of all photons incident on the detector surface.
- The detected signal for an ideal energy integrating detector, Se, can be written as:

$$S_e = A_d t \int_0^{E_{\text{max}}} E\phi(E) dE$$

Where

- t is the exposure time, sec
- ϕ is the photon fluence rate, photons/mm2/sec,
- \bullet $A_{\boldsymbol{d}}$ is the effective area of a detector element.

The majority of actual radiographic detectors are energy integrating; however, they are not 'ideal'.

b - Signal - actual detector, energy integrating - MONO-ENERGETIC.

 As a first step in deriving an expression for an actual detector, we write first the expression for monoenergetic x-rays.

$$S_E = \Phi_E \int_{0}^{E} ep(e, E) de$$

Note1: SE and ΦE are used to denote monoenergetic at E

· This can be used to define a signal detection efficiency.

Note2: For simplicity, we now write: $\Phi_E = A_d t \phi_E$

Note3: In a Monte Carlo analysis, the signal is determined by summing the energy deposited for H incident x-rays. The efficiency is trivially determined from this.

 $S_E = \sum_{i=1}^{\infty} e_i$ $\eta_{S_E} = \frac{S_E}{EH}$

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c - Noise - actual detector, energy integrating - MONO-ENERGETIC.

· The noise can be similarly written as a second moment integral.

$$\sigma_{\scriptscriptstyle E}^{\scriptscriptstyle 2} = \Phi_{\scriptscriptstyle E} \int_{\scriptscriptstyle E}^{\scriptscriptstyle E} e^{\scriptscriptstyle 2} p(e,E) de$$

· And the noise transfer efficiency similarly defined.

$$\eta_{\sigma^{(E)}}^2 = \frac{\sigma_E^2}{E^2 \Phi_E} = \int_0^E e^2 p(e, E) de / E^2$$

Note that this efficiency is the variance transfer.

Note: In a Monte Carlo analysis, the noise transfer and related efficiency is determined by accumulating the square of the energy deposited by each x-ray. $\eta_{\sigma_E}^2 = \frac{\sigma_E^2}{E^2 H}$

d - Signal and noise for a SPECTRUM of Xray Energies.

• For detectors with linear signals, the signal and noise are determined by separate integrals incorporating the efficiency.

$$\longrightarrow S = \int_{0}^{kV} \eta_{S}(E) E \Phi(E) dE$$

Note1: $\Phi(E)$ is now used to denote the energy spectrum.

$$\longrightarrow \sigma_s^2 = \int_0^k \eta_\sigma^2(E) E^2 \Phi(E) dE$$

• For <u>multiple</u> <u>channels</u> which <u>linearly</u> <u>accumulate</u> signal, the energy absorption and noise power <u>efficiencies</u> <u>are</u> <u>additive</u>.

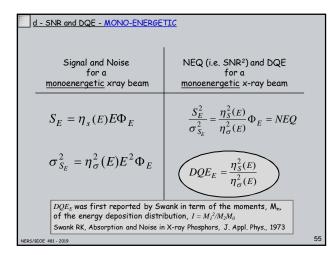
$$\eta_s(E) = \eta_{s_1}(E) + \eta_{s_2}(E) + ... \eta_{s_n}(E)$$

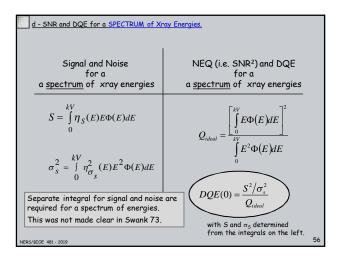
$$\eta_{\sigma}^{2}(E) = \eta_{\sigma_{1}}^{2}(E) + \eta_{\sigma_{2}}^{2}(E) + ... \eta_{\sigma_{n}}^{2}(E)$$

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In lecture LO5, we saw that a small object which perturbs the attenuation of the surrounding material results has a relative contrast given by the difference between the attenuation coefficient of the small detail (i.e. the target material) and the attenuation coefficient of the surrounding material (i.e. the background material). $C_r = (\mu_t - \mu_b) \delta_t \qquad \qquad \text{From Lecture 05}$ When considering poly-energetic beams, the energy dependent transmission and detector signal efficiency must be accounted for when determining C_r . In the derivation, there is a transmission term of the form $\exp(-\mu(E)\delta_t)$ that occurs within the integrations over pathlength and energy that lead to the signal in the target region, S_r , and the signal in the background region, S_b . For a small target, the attenuation difference comes from the difference in $\mu(E)$ over the region of the target, $\mu_i(E) - \mu_b(E)$. When $[\mu_i(E) - \mu_b(E)]\delta_i$ is small, these equation yield; $C_r = \frac{\int \eta_s(E) E \phi(E) [\mu_t(E) - \mu_b(E)] \delta_t dE}{\int \eta_s(E) E \phi(E) dE}$

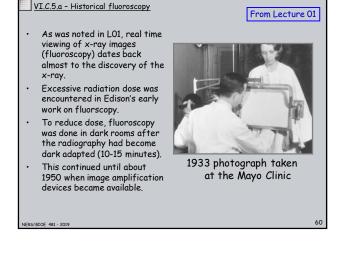
If we define the effective attenuation as a weighted average of $\mu(E)$, $\mu^{eff} = \frac{\int \eta_s(E) E \phi(E) \mu(E) dE}{\int \eta_s(E) E \phi(E) dE}$ then C_r can be expressed as, $C_r = (\mu_t^{eff} - \mu_b^{eff}) \delta_t$ The effective attenuation coefficient, μ_{eff} , is defined with respect to:

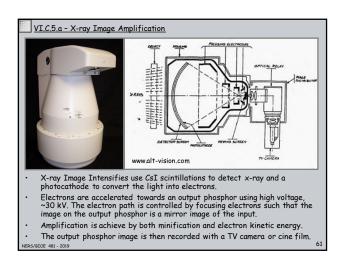
• An x-ray spectrum incident on a target, $\phi(E)$.

• A detector with energy dependent absorption, $\eta_s(E)$.

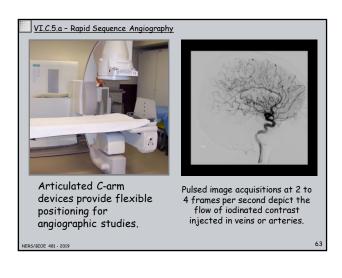
Note: Some textbooks may define an effective attenuation coefficient that applies to other problems. For example, the transmitted exposure may be considered rather than a detector signal.

VI.C.5 - Rapid Sequence Acquisitions & fluoroscopy (15 charts) 5) Rapid Sequence Acquisitions & fluoroscopy a. Traditional fluoroscopy with Image Intensifiers. b. Pulsed Digital fluoroscopy c. Digital Angiography

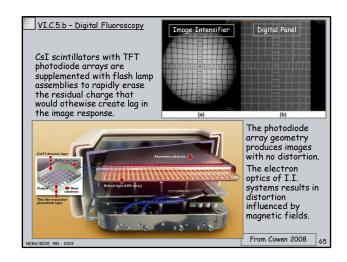


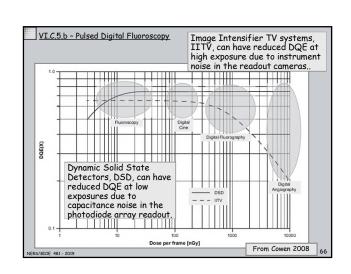


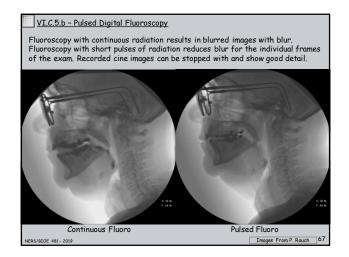


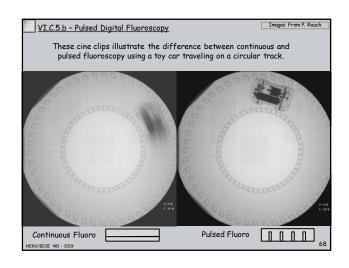


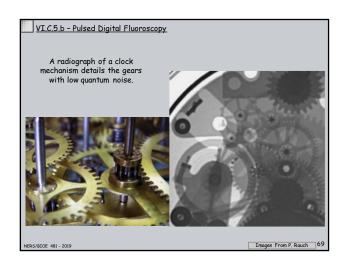


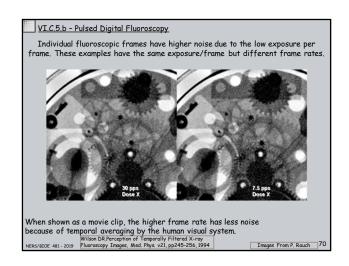


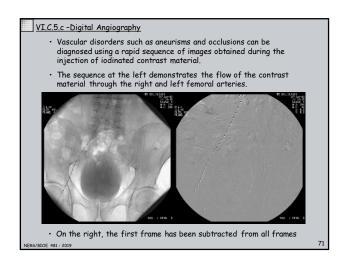


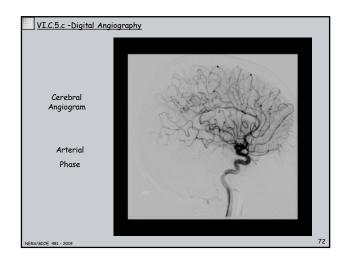


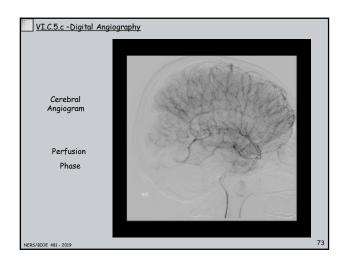


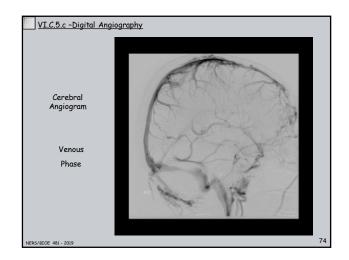


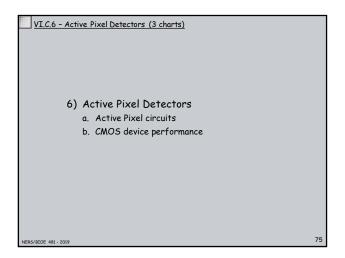


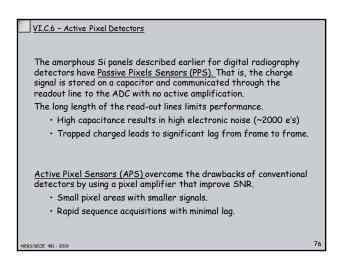


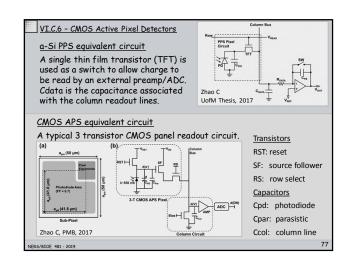


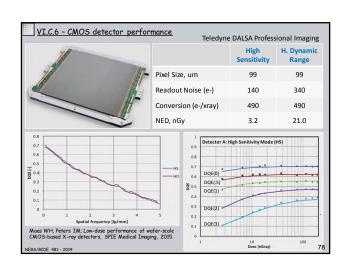


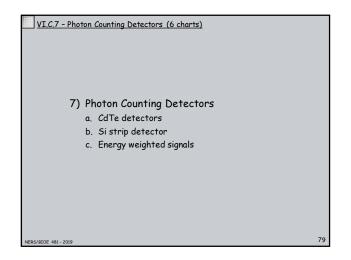


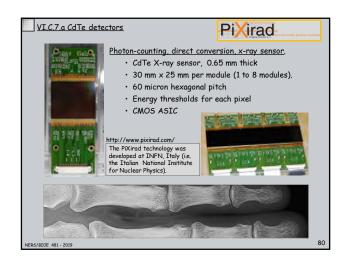


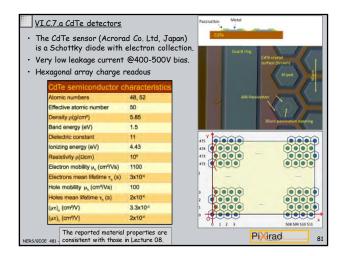


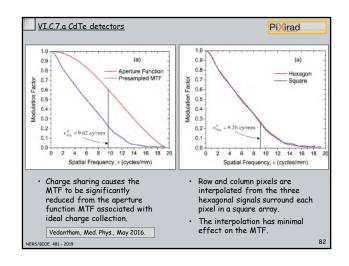


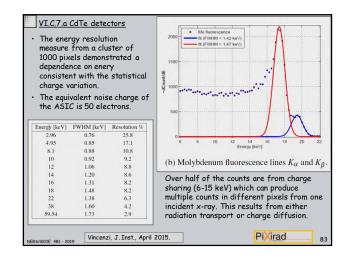




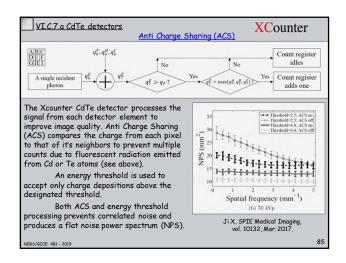


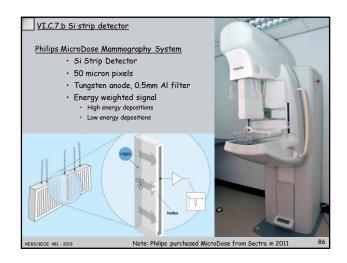


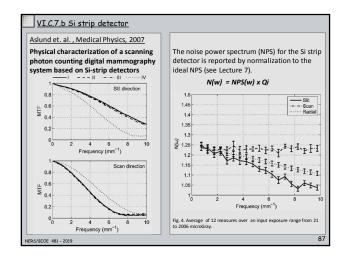


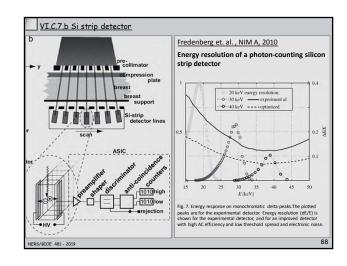




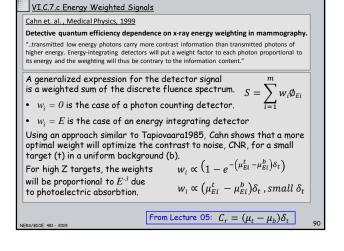








VI.C.7.b Si strip detector The simulated CNR improvement is Berglund et. al. , SPIE MI, 2014 shown as a function of weight. The CNR Energy weighting improves the image improvement and optimal weight were quality of spectral mammograms: larger for higher tube voltages. A weight Implementation on a photon-counting of ~1.8 is near optimal for all cases. mammography system. CNR improvement for energy weightin "We have implemented and evaluated so-called energy weighting on a commercially available spectral photoncounting mammography system. A practical formula for calculating the optimal weight from pixel values was derived. Computer simulations and phantom measurements revealed that the contrast-tonoise ratio was improved 50 micron calcification in breast tissue by 3%-5%, and automatic image analysis showed that the improvement 18 keV threshold @ 26 kV 20 keV threshold @ 32 kV was detectable in a set of screening 22 keV threshold @38 kV mammograms." /BIOE 481 - 2019



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